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Thermodynamics

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This course was adapted from the Department of Energy, Publication No. DOE-HDBK-1012/1-92, “Thermodynamics”, Volume 1, which is in the public domain.

OVERVIEW

The *Department of Energy Fundamentals Handbook* entitled *Thermodynamics, Heat Transfer, and Fluid Flow* was prepared as an information resource for personnel who are responsible for the operation of the Department's nuclear facilities. A basic understanding of the thermal sciences is necessary for DOE nuclear facility operators, maintenance personnel, and the technical staff to safely operate and maintain the facility and facility support systems. The information in the handbook is presented to provide a foundation for applying engineering concepts to the job. This knowledge will help personnel more fully understand the impact that their actions may have on the safe and reliable operation of facility components and systems.

The *Thermodynamics, Heat Transfer, and Fluid Flow* handbook consists of three modules that are contained in three volumes. The following is a brief description of the information presented in each module of the handbook.

Volume 1 of 3

Module 1 - Thermodynamics

This module explains the properties of fluids and how those properties are affected by various processes. The module also explains how energy balances can be performed on facility systems or components and how efficiency can be calculated.

Volume 2 of 3

Module 2 - Heat Transfer

This module describes conduction, convection, and radiation heat transfer. The module also explains how specific parameters can affect the rate of heat transfer.

Volume 3 of 3

Module 3 - Fluid Flow

This module describes the relationship between the different types of energy in a fluid stream through the use of Bernoulli's equation. The module also discusses the causes of head loss in fluid systems and what factors affect head loss.

The information contained in this handbook is by no means all encompassing. An attempt to present the entire subject of thermodynamics, heat transfer, and fluid flow would be impractical. However, the *Thermodynamics, Heat Transfer, and Fluid Flow* handbook does present enough information to provide the reader with a fundamental knowledge level sufficient to understand the advanced theoretical concepts presented in other subject areas, and to better understand basic system and equipment operations.

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REFERENCES

- VanWylen, G. J. and Sonntag, R. E., Fundamentals of Classical Thermodynamics SI Version, 2nd Edition, John Wiley and Sons, New York, ISBN 0-471-04188-2.
- Kreith, Frank, Principles of Heat Transfer, 3rd Edition, Intext Press, Inc., New York, ISBN 0-7002-2422-X.
- Holman, J. P., Thermodynamics, McGraw-Hill, New York.
- Streeter, Victor, L., Fluid Mechanics, 5th Edition, McGraw-Hill, New York, ISBN 07-062191-9.
- Rynolds, W. C. and Perkins, H. C., Engineering Thermodynamics, 2nd Edition, McGraw-Hill, New York, ISBN 0-07-052046-1.
- Meriam, J. L., Engineering Mechanics Statics and Dynamics, John Wiley and Sons, New York, ISBN 0-471-01979-8.
- Schneider, P. J. Conduction Heat Transfer, Addison-Wesley Pub. Co., California.
- Holman, J. P., Heat Transfer, 3rd Edition, McGraw-Hill, New York.
- Knudsen, J. G. and Katz, D. L., Fluid Dynamics and Heat Transfer, McGraw-Hill, New York.
- Kays, W. and London, A. L., Compact Heat Exchangers, 2nd Edition, McGraw-Hill, New York.
- Weibelt, J. A., Engineering Radiation Heat Transfer, Holt, Rinehart and Winston Publish., New York.
- Sparrow, E. M. and Cess, R. E., Radiation Heat Transfer, Brooks/Cole Publish. Co., Belmont, California.
- Hamilton, D. C. and Morgan, N. R., Radiant-Interchange Configuration Factors, Tech. Note 2836, National Advisory Committee for Aeronautics.

REFERENCES (Cont.)

- McDonald, A. T. and Fox, R. W., Introduction to Fluid mechanics, 2nd Edition, John Wiley and Sons, New York, ISBN 0-471-01909-7.
- Zucrow, M. J. and Hoffman, J. D., Gas Dynamics Vol.b1, John Wiley and Sons, New York, ISBN 0-471-98440-X.
- Crane Company, Flow of Fluids Through Valves, Fittings, and Pipe, Crane Co. Technical Paper No. 410, Chicago, Illinois, 1957.
- Esposito, Anthony, Fluid Power with Applications, Prentice-Hall, Inc., New Jersey, ISBN 0-13-322701-4.
- Beckwith, T. G. and Buck, N. L., Mechanical Measurements, Addison-Wesley Publish Co., California.
- Wallis, Graham, One-Dimensional Two-Phase Flow, McGraw-Hill, New York, 1969.
- Kays, W. and Crawford, M. E., Convective Heat and Mass Transfer, McGraw-Hill, New York, ISBN 0-07-03345-9.
- Collier, J. G., Convective Boiling and Condensation, McGraw-Hill, New York, ISBN 07-084402-X.
- Academic Program for Nuclear Power Plant Personnel, Volumes III and IV, Columbia, MD: General Physics Corporation, Library of Congress Card #A326517, 1982.
- Faires, Virgel Moring and Simmang, Clifford Max, Thermodynamics, MacMillan Publishing Co. Inc., New York.

THERMODYNAMIC PROPERTIES

Thermodynamic properties describe measurable characteristics of a substance. A knowledge of these properties is essential to the understanding of thermodynamics.

EO 1.1 DEFINE the following properties:

- a. **Specific volume**
- b. **Density**
- c. **Specific gravity**
- d. **Humidity**

EO 1.2 DESCRIBE the following classifications of thermodynamic properties:

- a. **Intensive properties**
 - b. **Extensive properties**
-

Mass and Weight

The *mass* (m) of a body is the measure of the amount of material present in that body. The *weight* (wt) of a body is the force exerted by that body when its mass is accelerated in a gravitational field. Mass and weight are related as shown in Equation 1-1.

$$wt = \frac{mg}{g_c} \quad (1-1)$$

where:

wt	=	weight (lbf)
m	=	mass (lbm)
g	=	acceleration of gravity = 32.17 ft/sec ²
g _c	=	gravitational constant = 32.17 lbm-ft/lbf-sec ²

Note that g_c has the same numerical value as the acceleration of gravity at sea level, but is not the acceleration of gravity. Rather, it is a dimensional constant employed to facilitate the use of Newton's Second Law of Motion with the English system of units.

The weight of a body is a force produced when the mass of the body is accelerated by a gravitational acceleration. The mass of a certain body will remain constant even if the gravitational acceleration acting upon that body changes.

According to Newton's Second Law of Motion, force (F) = ma , where a is acceleration. For example, on earth an object has a certain mass and a certain weight. When the same object is placed in outer space, away from the earth's gravitational field, its mass is the same, but it is now in a "weightless" condition (that is, gravitational acceleration and, thus, force equal zero).

The English system uses the pound-force (lbf) as the unit of weight. Knowing that acceleration has the units of ft/sec^2 and using Newton's second law, we can determine that the units of mass are $\text{lbf}\cdot\text{sec}^2/\text{ft}$. For simplification, $1 \text{ lbf}\cdot\text{sec}^2/\text{ft}$ is called a slug. The basic unit of mass in the English system is the slug. However, the slug is an almost meaningless unit for the average individual. The unit of mass generally used is the pound-mass (lbm). In order to allow lbm to be used as a unit of mass, we must divide Newton's second law by the gravitational constant (g_c).

$$\left(32.17 \frac{\text{lbm} \cdot \text{ft}}{\text{lbf} \cdot \text{sec}^2} \right) = g_c$$

Newton's second law can be expressed by Equation 1-2.

$$F = \frac{ma}{g_c} \tag{1-2}$$

Use of the gravitational constant, g_c , adapts Newton's second law such that $1 \text{ lbf} = 1 \text{ lbm}$ at the surface of the earth. It is important to note that this relationship is only true at the surface of the earth, where the acceleration due to gravity is $32.17 \text{ ft}/\text{sec}^2$. However, because all of our discussions will be based upon experiences and observations on earth, we will use the lbm as the unit of mass.

NOTE: In Equation 1-2, acceleration "a" is often written as "g" because, in this case, the acceleration is the gravitational acceleration due to the earth's gravitational field ($g = 32.17 \text{ ft}/\text{sec}^2$).

Example:

Using Equation 1-2, prove that $1 \text{ lbf} = 1 \text{ lbm}$ on earth.

Solution:

$$F = \frac{mg}{g_c}$$

$$1 \text{ lbf} = \frac{(1 \text{ lbm}) (32.17 \text{ ft}/\text{sec}^2)}{32.17 \frac{(\text{lbm} \cdot \text{ft})}{(\text{lbf} \cdot \text{sec}^2)}}$$

$$1 \text{ lbf} = 1 \text{ lbf} \text{ (an equality)}$$

Specific Volume

The *specific volume* (v) of a substance is the total volume (V) of that substance divided by the total mass (m) of that substance (volume per unit mass). It has units of cubic feet per pound-mass (ft^3/lbm).

$$v = \frac{V}{m} \quad (1-3)$$

where:

v = specific volume (ft^3/lbm)

V = volume (ft^3)

m = mass (lbm)

Density

The *density* (ρ) of a substance is the total mass (m) of that substance divided by the total volume (V) occupied by that substance (mass per unit volume). It has units of pound-mass per cubic feet (lbm/ft^3). The density (ρ) of a substance is the reciprocal of its specific volume (v).

$$\rho = \frac{m}{V} = \frac{1}{v} \quad (1-4)$$

where:

ρ = density (lbm/ft^3)

m = mass (lbm)

V = volume (ft^3)

v = specific volume (ft^3/lbm)

Specific Gravity

Specific gravity (S.G.) is a measure of the relative density of a substance as compared to the density of water at a standard temperature. Physicists use 39.2°F (4°C) as the standard, but engineers ordinarily use 60°F. In the International System of Units (SI Units), the density of water is 1.00 g/cm³ at the standard temperature. Therefore, the specific gravity (which is dimensionless) for a liquid has the same numerical value as its density in units of g/cm³. Since the density of a fluid varies with temperature, specific gravities must be determined and specified at particular temperatures.

Humidity

Humidity is the amount of moisture (water vapor) in the air. It can be expressed as absolute humidity or relative humidity. *Absolute humidity* is the mass of water vapor divided by a unit volume of air (grams of water/cm³ of air). *Relative humidity* is the amount of water vapor present in the air divided by the maximum amount that the air could contain at that temperature. Relative humidity is expressed as a percentage. The relative humidity is 100% if the air is saturated with water vapor and 0% if no water vapor is present in the air at all.

Intensive and Extensive Properties

Thermodynamic properties can be divided into two general classes, intensive and extensive properties. An *intensive property* is independent of the amount of mass. The value of an *extensive property* varies directly with the mass. Thus, if a quantity of matter in a given state is divided into two equal parts, each part will have the same value of intensive property as the original and half the value of the extensive property. Temperature, pressure, specific volume, and density are examples of intensive properties. Mass and total volume are examples of extensive properties.

Summary

The important information from this chapter is summarized below.

Thermodynamic Properties Summary

The following properties were defined:

- Specific volume (v) is the total volume (V) of a substance divided by the total mass (m) of that substance.
- Density (ρ) is the total mass (m) of a substance divided by the total volume (V) occupied by that substance.
- Specific gravity (S.G.) is a measure of the relative density of a substance as compared to the density of water at a standard temperature.
- Humidity is the amount of moisture (water vapor) in the air. It can be measured in absolute or relative units.

The following classifications of thermodynamic properties were described:

- Intensive properties are those that are independent of the amount of mass.
- Extensive properties are those that vary directly with the mass.

TEMPERATURE AND PRESSURE MEASUREMENTS

Several types of temperature and pressure measurements are used during discussions of thermodynamics. Operators must recognize the different types and their interrelationships in order to understand thermodynamics.

- EO 1.3** **DEFINE** the thermodynamic properties temperature and pressure.
- EO 1.4** **DESCRIBE** the Fahrenheit, Celsius, Kelvin, and Rankine temperature scales including:
- a. **Absolute zero temperature**
 - b. **The freezing point of water at atmospheric pressure**
 - c. **The boiling point of water at atmospheric pressure**
- EO 1.5** **CONVERT** temperatures between the Fahrenheit, Celsius, Kelvin, and Rankine scales.
- EO 1.6** **DESCRIBE** the relationship between absolute pressure, gauge pressure, and vacuum.
- EO 1.7** **CONVERT** pressures between the following units:
- a. **Pounds per square inch**
 - b. **Inches of water**
 - c. **Inches of mercury**
 - d. **Millimeters of mercury**
 - e. **Microns of mercury**
-

Temperature

Temperature is a measure of the molecular activity of a substance. The greater the movement of molecules, the higher the temperature. It is a relative measure of how "hot" or "cold" a substance is and can be used to predict the direction of heat transfer.

Temperature Scales

The two temperature scales normally employed for measurement purposes are the Fahrenheit (F) and Celsius (C) scales. These scales are based on a specification of the number of increments between the freezing point and boiling point of water at standard atmospheric pressure. The Celsius scale has 100 units between these points, and the Fahrenheit scale has 180 units. The zero points on the scales are arbitrary.

The freezing point of water was selected as the zero point of the Celsius scale. The coldest temperature achievable with a mixture of ice and salt water was selected as the zero point of the Fahrenheit scale. The temperature at which water boils was set at 100 on the Celsius scale and 212 on the Fahrenheit scale. The relationship between the scales is represented by the following equations.

$$^{\circ}\text{F} = 32.0 + (9/5)^{\circ}\text{C} \quad (1-5)$$

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32.0)(5/9) \quad (1-6)$$

It is necessary to define an absolute temperature scale having only positive values. The absolute temperature scale that corresponds to the Celsius scale is called the Kelvin (K) scale, and the absolute scale that corresponds to the Fahrenheit scale is called the Rankine (R) scale. The zero points on both absolute scales represent the same physical state. This state is where there is no molecular motion of individual atoms. The relationships between the absolute and relative temperature scales are shown in the following equations.

$$^{\circ}\text{R} = ^{\circ}\text{F} + 460 \quad (1-7)$$

$$^{\circ}\text{K} = ^{\circ}\text{C} + 273 \quad (1-8)$$

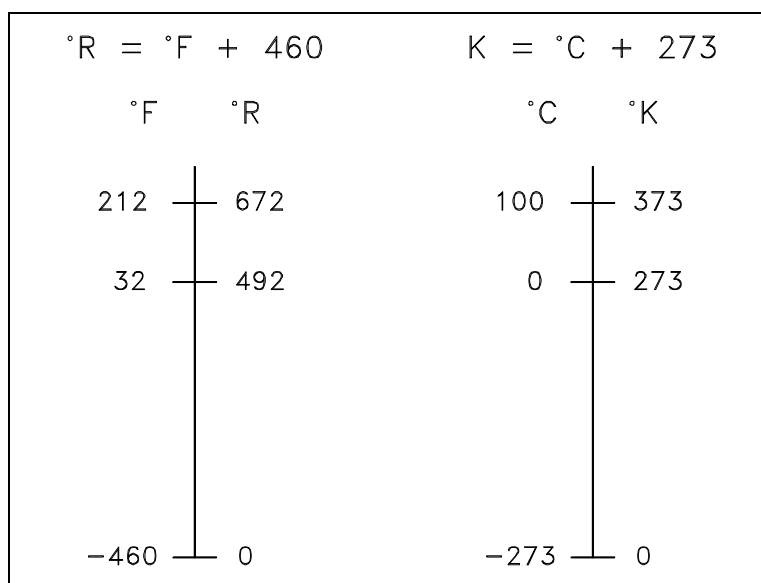


Figure 1 Comparison of Temperature Scales

The conversion of one temperature scale to another is sometimes required at nuclear facilities, and the operator should be acquainted with the process. The following two examples will be helpful.

Example 1: Temperature Scale Conversion

What is the Rankine equivalent of 80°C?

Solution:

$$^{\circ}\text{F} = (9/5) ^{\circ}\text{C} + 32$$

$$= (9/5)(80) + 32$$

$$= 176 ^{\circ}\text{F}$$

$$^{\circ}\text{R} = ^{\circ}\text{F} + 460$$

$$= 176 + 460$$

$$= 636 ^{\circ}\text{R}$$

Example 2: Temperature Scale Conversion

What is the Kelvin equivalent of 80°F?

Solution:

$$^{\circ}\text{C} = (5/9) (^{\circ}\text{F} - 32)$$

$$= (5/9) (80 - 32)$$

$$= 26.7^{\circ}\text{C}$$

$$^{\circ}\text{K} = ^{\circ}\text{C} + 273$$

$$= 26.7 + 273$$

$$= 299.7 ^{\circ}\text{K}$$

Pressure

Pressure is a measure of the force exerted per unit area on the boundaries of a substance (or system). It is caused by the collisions of the molecules of the substance with the boundaries of the system. As molecules hit the walls, they exert forces that try to push the walls outward. The forces resulting from all of these collisions cause the pressure exerted by a system on its surroundings. Pressure is frequently measured in units of lbf/in² (psi).

Pressure Scales

When pressure is measured relative to a perfect vacuum, it is called absolute pressure (psia); when measured relative to atmospheric pressure (14.7 psi), it is called gauge pressure (psig). The latter pressure scale was developed because almost all pressure gauges register zero when open to the atmosphere. Therefore, pressure gauges measure the difference between the pressure of the fluid to which they are connected and that of the surrounding air.

If the pressure is below that of the atmosphere, it is designated as a vacuum. A perfect vacuum would correspond to absolute zero pressure. All values of absolute pressure are positive, because a negative value would indicate tension, which is considered impossible in any fluid. Gauge pressures are positive if they are above atmospheric pressure and negative if they are below atmospheric pressure. Figure 2 shows the relationships between absolute, gauge, vacuum, and atmospheric pressures, as do Equations 1-9 and 1-10.

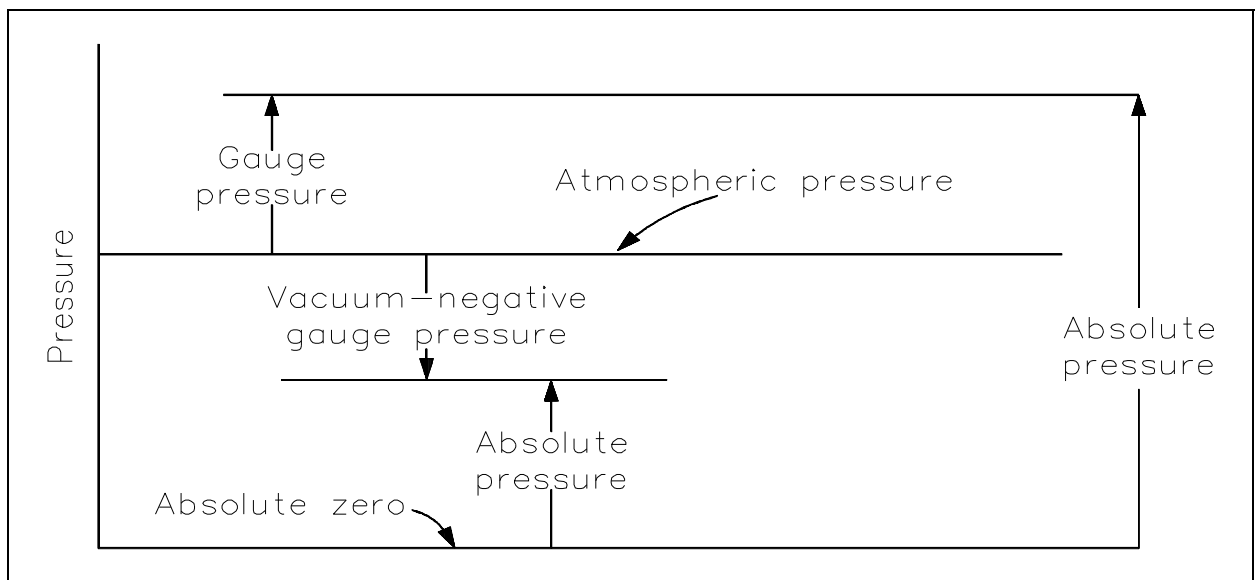


Figure 2 Pressure Relationships

$$P_{\text{abs}} = P_{\text{atm}} + P_{\text{gauge}} \quad (1-9)$$

$$P_{\text{abs}} = P_{\text{atm}} - P_{\text{vac}} \quad (1-10)$$

P_{atm} is atmospheric pressure, which is also called the barometric pressure. P_{gauge} is the gauge pressure, and P_{vac} is vacuum. Once again, the following examples relating the various pressures will be helpful in understanding the idea of gauge versus absolute pressures.

Example 1: Pressure Relationships

How deep can a diver descend in ocean water (density = 64 lbm/ft³) without damaging his watch, which will withstand an absolute pressure of 80 psia? ($P = \text{density} \cdot \text{height}$)

Solution:

Assume: $P_{\text{atm}} = 14.7 \text{ psia}$

$$P_{\text{abs}} = P_{\text{atm}} + P_{\text{gauge}}$$

$$80 \text{ psia} = 14.7 + P_{\text{gauge}}$$

$$P_{\text{gauge}} = (80 - 14.7) = 65.3 \text{ psig}$$

$$P_{\text{gauge}} = \text{density} \cdot \text{height} = \rho H$$

$$(65.3)(144 \text{ in}^2/\text{ft}^2) = (64 \text{ lbm}/\text{ft}^3)H$$

$$H = (65.3)(144)/(64)$$

$$H = 146.9 \text{ ft}$$

Example 2: Pressure Relationships

What is the absolute pressure at the bottom of a swimming pool 6 feet deep that is filled with fresh water? $P_{\text{atm}} = 14.7$ psia

Solution:

$$\begin{aligned}P_{\text{abs}} &= P_{\text{atm}} + P_{\text{gauge}} \\&= 14.7 + \rho H \\&= 14.7 + [(62.4 \text{ lbm/ft}^3)(6 \text{ ft})/(144 \text{ in.}^2/\text{ft}^2)] \\&= 14.7 + 2.6 \\P_{\text{abs}} &= 17.3 \text{ psia}\end{aligned}$$

In addition to pounds per square inch, pressure can be measured with reference to the force that exists in a column of fluid at a certain height. The most common of these are inches of water, inches of mercury, millimeters of mercury, and microns of mercury. Conversion factors are listed below.

$$14.7 \text{ psia} = 408 \text{ inches of water}$$

$$14.7 \text{ psia} = 29.9 \text{ inches of mercury}$$

$$1 \text{ inch of mercury} = 25.4 \text{ millimeters of mercury}$$

$$1 \text{ millimeter of mercury} = 10^3 \text{ microns of mercury}$$

Summary

The important information from this chapter is summarized below.

Temperature and Pressure Scales Summary

The following properties were defined as follows.

- Temperature is a measure of the molecular activity of a substance.
- Pressure is a measure of the force per unit area exerted on the boundaries of a substance (or system).

The relationship between the Fahrenheit, Celsius, Kelvin, and Rankine temperature scales was described.

- Absolute zero = $-460\text{ }^{\circ}\text{F}$ or $-273\text{ }^{\circ}\text{C}$
- Freezing point of water = $32\text{ }^{\circ}\text{F}$ or $0\text{ }^{\circ}\text{C}$
- Boiling point of water = $212\text{ }^{\circ}\text{F}$ or $100\text{ }^{\circ}\text{C}$

Conversions between the different scales can be made using the following formulas.

- $^{\circ}\text{F} = 32 + (9/5)^{\circ}\text{C}$
- $^{\circ}\text{C} = (^{\circ}\text{F} - 32)(5/9)$
- $^{\circ}\text{R} = ^{\circ}\text{F} + 460$
- $^{\circ}\text{K} = ^{\circ}\text{C} + 273$

Relationships between absolute pressure, gauge pressure, and vacuum can be shown using the following formulas.

- $P_{\text{abs}} = P_{\text{atm}} + P_{\text{gauge}}$
- $P_{\text{abs}} = P_{\text{atm}} - P_{\text{vac}}$

Temperature and Pressure Scales Summary (Cont.)

Converting between the different pressure units can be done using the following conversions.

- 14.7 psia = 408 inches of water
- 14.7 psia = 29.9 inches of mercury
- 1 inch of mercury = 25.4 millimeters of mercury
- 1 millimeter of mercury = 10^3 microns of mercury

ENERGY, WORK, AND HEAT

Heat and work are the two ways in which energy can be transferred across the boundary of a system. One of the most important discoveries in thermodynamics was that work could be converted into an equivalent amount of heat and that heat could be converted into work.

- EO 1.8 DEFINE the following:**
- a. **Heat**
 - b. **Latent heat**
 - c. **Sensible heat**
 - d. **Units used to measure heat**

- EO 1.9 DEFINE the following thermodynamic properties:**
- a. **Specific enthalpy**
 - b. **Entropy**
-

Energy

Energy is defined as the capacity of a system to perform work or produce heat.

Potential Energy

Potential energy (PE) is defined as the energy of position. Using English system units, it is defined by Equation 1-11.

$$PE = \frac{mgz}{g_c} \quad (1-11)$$

where:

- PE = potential energy (ft-lbf)
- m = mass (lbm)
- z = height above some reference level (ft)
- g = acceleration due to gravity (ft/sec²)
- g_c = gravitational constant = 32.17 ft-lbm/lbf-sec²

In most practical engineering calculations, the acceleration due to gravity (g) is numerically equal to the gravitational constant (g_c); thus, the potential energy (PE) in foot-pounds-force is numerically equal to the product of the mass (m) in pounds-mass times the height (z) in feet above some reference level.

Example:

Determine the potential energy of 50 lbm of water in a storage tank 100 ft above the ground.

Solution:

Using Equation 1-11

$$PE = \frac{mgz}{g_c}$$

$$PE = \frac{(50 \text{ lbm}) (32.17 \text{ ft/sec}^2) (100 \text{ ft})}{32.17 \text{ ft-lbm/lbf-sec}^2}$$

$$PE = 5000 \text{ ft-lbf}$$

Kinetic Energy

Kinetic energy (KE) is the energy of motion. Using English system units, it is defined by Equation 1-12.

$$KE = \frac{mv^2}{2g_c} \quad (1-12)$$

where:

KE = kinetic energy (ft-lbf)

m = mass (lbm)

v = velocity (ft/sec)

g_c = gravitational constant = 32.17 ft-lbm/lbf-sec²

Example:

Determine the kinetic energy of 7 lbm of steam flowing through a pipe at a velocity of 100 ft/sec.

Solution:

Using Equation 1-12.

$$KE = \frac{mv^2}{2g_c}$$

$$KE = \frac{(7 \text{ lbm}) (100 \text{ ft/sec})^2}{2(32.17 \text{ ft-lbm/lbf-sec}^2)}$$

$$KE = \frac{(7 \text{ lbm}) (10,000 \text{ ft}^2/\text{sec}^2)}{(64.34 \text{ ft-lbm/lbf-sec}^2)}$$

$$KE = 1088 \text{ ft-lbf}$$

Specific Internal Energy

Potential energy and kinetic energy are macroscopic forms of energy. They can be visualized in terms of the position and the velocity of objects. In addition to these macroscopic forms of energy, a substance possesses several microscopic forms of energy. Microscopic forms of energy include those due to the rotation, vibration, translation, and interactions among the molecules of a substance. None of these forms of energy can be measured or evaluated directly, but techniques have been developed to evaluate the change in the total sum of all these microscopic forms of energy. These microscopic forms of energy are collectively called *internal energy*, customarily represented by the symbol U . In engineering applications, the unit of internal energy is the *British thermal unit* (Btu), which is also the unit of heat.

The specific internal energy (u) of a substance is its internal energy per unit mass. It equals the total internal energy (U) divided by the total mass (m).

$$u = \frac{U}{m} \quad (1-13)$$

where:

u = specific internal energy (Btu/lbm)

U = internal energy (Btu)

m = mass (lbm)

Example:

Determine the specific internal energy of 12 lbm of steam if the total internal energy is 23,000 Btu.

Solution:

Using Equation 1-13.

$$u = \frac{U}{m}$$

$$u = \frac{23,000 \text{ Btu}}{12 \text{ lbm}}$$

$$u = 1916.67 \text{ Btu/lbm}$$

Specific P-V Energy

In addition to the internal energy (U), another form of energy exists that is important in understanding energy transfer systems. This form of energy is called P-V energy because it arises from the pressure (P) and the volume (V) of a fluid. It is numerically equal to PV, the product of pressure and volume. Because energy is defined as the capacity of a system to perform work, a system where pressure and volume are permitted to expand performs work on its surroundings. Therefore, a fluid under pressure has the capacity to perform work. In engineering applications, the units of P-V energy, also called flow energy, are the units of pressure times volume (pounds-force per square foot times cubic feet), which equals foot-pounds force (ft-lbf).

The specific P-V energy of a substance is the P-V energy per unit mass. It equals the total P-V divided by the total mass m, or the product of the pressure P and the specific volume v, and is written as Pv.

$$Pv = \frac{PV}{m} \tag{1-14}$$

where:

P = pressure (lbf/ft²)

V = volume (ft³)

v = specific volume (ft³/lbm) = $\frac{V}{m}$

m = mass (lbm)

Example:

Determine the specific P-V energy of 15 lbm of steam at 1000 psi in an 18 ft³ tank.

Solution:

Using Equation 1-14

$$Pv = \frac{PV}{m}$$

$$Pv = \frac{(1000 \text{ lbf/in.}^2) (144 \text{ in.}^2/\text{ft}^2) (18 \text{ ft}^3)}{15 \text{ lbm}}$$

$$Pv = 172,800 \text{ ft-lbf/lbm}$$

Specific Enthalpy

Specific enthalpy (h) is defined as $h = u + Pv$, where u is the specific internal energy (Btu/lbm) of the system being studied, P is the pressure of the system (lbf/ft²), and v is the specific volume (ft³/lbm) of the system. Enthalpy is usually used in connection with an "open" system problem in thermodynamics. Enthalpy is a property of a substance, like pressure, temperature, and volume, but it cannot be measured directly. Normally, the enthalpy of a substance is given with respect to some reference value. For example, the specific enthalpy of water or steam is given using the reference that the specific enthalpy of water is zero at .01°C and normal atmospheric pressure. The fact that the absolute value of specific enthalpy is unknown is not a problem, however, because it is the change in specific enthalpy (Δh) and not the absolute value that is important in practical problems. Steam tables include values of enthalpy as part of the information tabulated.

Work

Kinetic energy, potential energy, internal energy, and P-V energy are forms of energy that are properties of a system. *Work* is a form of energy, but it is energy in transit. Work is not a property of a system. Work is a process done by or on a system, but a system contains no work. This distinction between the forms of energy that are properties of a system and the forms of energy that are transferred to and from a system is important to the understanding of energy transfer systems.

Work is defined for mechanical systems as the action of a force on an object through a distance. It equals the product of the force (F) times the displacement (d).

$$W = Fd \quad (1-15)$$

where:

$$W = \text{work (ft-lbf)}$$

$$F = \text{force (lbf)}$$

$$d = \text{displacement (ft)}$$

Example:

Determine the amount of work done if a force of 150 lbf is applied to an object until it has moved a distance of 30 feet.

Solution:

Using Equation 1-15

$$W = Fd$$

$$W = (150 \text{ lbf})(30 \text{ ft})$$

$$W = 4500 \text{ ft-lbf}$$

In dealing with work in relation to energy transfer systems, it is important to distinguish between work done by the system on its surroundings and work done on the system by its surroundings. Work is done by the system when it is used to turn a turbine and thereby generate electricity in a turbine-generator. Work is done on the system when a pump is used to move the working fluid from one location to another. A positive value for work indicates that work is done by the system on its surroundings; a negative value indicates that work is done on the system by its surroundings.

Heat

Heat, like work, is energy in transit. The transfer of energy as heat, however, occurs at the molecular level as a result of a temperature difference. The symbol Q is used to denote heat. In engineering applications, the unit of heat is the British thermal unit (Btu). Specifically, this is called the 60 degree Btu because it is measured by a one degree temperature change from 59.5 to 60.5°F.

As with work, the amount of heat transferred depends upon the path and not simply on the initial and final conditions of the system. Also, as with work, it is important to distinguish between heat added to a system from its surroundings and heat removed from a system to its surroundings. A positive value for heat indicates that heat is added to the system by its surroundings. This is in contrast to work that is positive when energy is transferred from the system and negative when transferred to the system. The symbol q is sometimes used to indicate the heat added to or removed from a system per unit mass. It equals the total heat (Q) added or removed divided by the mass (m). The term "specific heat" is not used for q since specific heat is used for another parameter. The quantity represented by q is referred to simply as the heat transferred per unit mass.

$$q = \frac{Q}{m} \quad (1-16)$$

where:

q = heat transferred per unit mass (Btu/lbm)

Q = heat transferred (Btu)

m = mass (lbm)

Example:

Determine the heat transferred per unit mass if 1500 Btu's are transferred to 40 lbm of water.

Solution:

Using Equation 1-16

$$q = \frac{Q}{m}$$

$$q = \frac{1500 \text{ Btu}}{40 \text{ lbm}}$$

$$q = 37.5 \text{ Btu/lbm}$$

The best way to quantify the definition of heat is to consider the relationship between the amount of heat added to or removed from a system and the change in the temperature of the system. Everyone is familiar with the physical phenomena that when a substance is heated, its temperature increases, and when it is cooled, its temperature decreases. The heat added to or removed from a substance to produce a change in its temperature is called *sensible heat*. The units of heat are often defined in terms of the changes in temperature it produces.

Another type of heat is called *latent heat*. Latent heat is the amount of heat added to or removed from a substance to produce a change in phase. When latent heat is added, no temperature change occurs. There are two types of latent heat. The first is the *latent heat of fusion*. This is the amount of heat added or removed to change phase between solid and liquid. The second type of latent heat is the *latent heat of vaporization*. This is the amount of heat added or removed to change phase between liquid and vapor. The latent heat of vaporization is sometimes called the latent heat of condensation.

Different substances are affected to different magnitudes by the addition of heat. When a given amount of heat is added to different substances, their temperatures increase by different amounts. The ratio of the heat (Q) added to or removed from a substance to the change in temperature (ΔT) produced is called the *heat capacity* (C_p) of the substance. The heat capacity of a substance per unit mass is called the *specific heat* (c_p) of the substance. The subscript p indicates that the heat capacity and specific heat apply when the heat is added or removed at constant pressure.

$$C_p = \frac{Q}{\Delta T}$$

$$c_p = \frac{Q}{m\Delta T} \quad (1-17)$$

$$c_p = \frac{q}{\Delta T}$$

where:

C_p = heat capacity at constant pressure (Btu/°F)

c_p = specific heat at constant pressure (Btu/lbm-°F)

Q = heat transferred (Btu)

q = heat transferred per unit mass (Btu/lbm)

m = mass (lbm)

ΔT = temperature change (°F)

One lbm of water is raised 1°F and one Btu of heat is added. This implies that the specific heat (c_p) of water is one Btu/lbm-°F. The c_p of water is equal to one Btu/lbm-°F only at 39.1°F.

By rearranging Equation 1-17 we obtain $Q = mc_p\Delta T$, which is used to calculate latent heat. By substituting mass flow rate in lbm/hr, \dot{m} , for m , we obtain $\dot{Q} = \dot{m}c_p\Delta T$. This equation is used to calculate heat transfer in Btu/hr and will be useful in later chapters.

Example:

How much heat is required to raise the temperature of 5 lbm of water from 50°F to 150°F? (Assume the specific heat (c_p) for water is constant at 1.0 Btu/lbm-°F.)

Solution:

$$c_p = \frac{Q}{m\Delta T}$$

$$Q = c_p m \Delta T$$

$$Q = (1.0 \text{ Btu/lbm-}^\circ\text{F})(5 \text{ lbm})(150^\circ\text{F} - 50^\circ\text{F})$$

$$Q = (1.0 \text{ Btu/lbm-}^\circ\text{F})(5 \text{ lbm})(100^\circ\text{F})$$

$$Q = 500 \text{ Btu}$$

From the previous discussions on heat and work, it is evident that there are many similarities between them. Heat and work are both transient phenomena. Systems never possess heat or work, but either or both may occur when a system undergoes a change of energy state. Both heat and work are boundary phenomena in that both are observed at the boundary of the system. Both represent energy crossing the system boundary.

Entropy

Entropy (S) is a property of a substance, as are pressure, temperature, volume, and enthalpy. Because entropy is a property, changes in it can be determined by knowing the initial and final conditions of a substance. Entropy quantifies the energy of a substance that is no longer available to perform useful work. Because entropy tells so much about the usefulness of an amount of heat transferred in performing work, the steam tables include values of specific entropy ($s = S/m$) as part of the information tabulated. Entropy is sometimes referred to as a measure of the inability to do work for a given heat transferred. Entropy is represented by the letter S and can be defined as ΔS in the following relationships.

$$\Delta S = \frac{\Delta Q}{T_{\text{abs}}} \quad (1-18)$$

$$\Delta s = \frac{\Delta q}{T_{\text{abs}}} \quad (1-19)$$

where:

$$\Delta S = \text{the change in entropy of a system during some process (Btu/}^\circ\text{R)}$$

ΔQ	=	the amount of heat transferred to or from the system during the process (Btu)
T_{abs}	=	the absolute temperature at which the heat was transferred ($^{\circ}\text{R}$)
Δs	=	the change in specific entropy of a system during some process (Btu/lbm $^{\circ}\text{R}$)
Δq	=	the amount of heat transferred to or from the system during the process (Btu/lbm)

Like enthalpy, entropy cannot be measured directly. Also, like enthalpy, the entropy of a substance is given with respect to some reference value. For example, the specific entropy of water or steam is given using the reference that the specific entropy of water is zero at 32°F. The fact that the absolute value of specific entropy is unknown is not a problem because it is the change in specific entropy (Δs) and not the absolute value that is important in practical problems.

Energy and Power Equivalences

The various forms of energy involved in energy transfer systems (such as potential energy, kinetic energy, internal energy, P-V energy, work and heat) may be measured in numerous basic units. In general, three types of units are used to measure energy: (1) mechanical units, such as the foot-pound-force (ft-lbf); (2) thermal units, such as the British thermal unit (Btu); and (3) electrical units, such as the watt-second (W-sec). In the mks and cgs systems, the mechanical units of energy are the joule (j) and the erg, the thermal units are the kilocalorie (kcal) and the calorie (cal), and the electrical units are the watt-second (W-sec) and the erg. Although the units of the various forms of energy are different, they are equivalent.

Some of the most important experiments in science were those conducted by J. P. Joule in 1843, who showed quantitatively that there was a direct correspondence between mechanical and thermal energy. These experiments showed that one kilocalorie equals 4,186 joules. These same experiments, when performed using English system units, show that one British thermal unit (Btu) equals 778.3 ft-lbf. These experiments established the equivalence of mechanical and thermal energy. Other experiments established the equivalence of electrical energy with both mechanical and thermal energy. For engineering applications, these equivalences are expressed by the following relationships.

$$1 \text{ ft-lbf} = 1.286 \times 10^{-3} \text{ Btu} = 3.766 \times 10^{-7} \text{ kW-hr}$$

$$1 \text{ Btu} = 778.3 \text{ ft-lbf} = 2.928 \times 10^{-4} \text{ kW-hr}$$

$$1 \text{ kW-hr} = 3.413 \times 10^3 \text{ Btu} = 2.655 \times 10^6 \text{ ft-lbf}$$

There is one additional unit of energy encountered in engineering applications. It is the horsepower-hour (hp-hr). It is a mechanical unit of energy defined by the following relationship:

$$1 \text{ hp-hr} = 1.980 \times 10^6 \text{ ft-lbf}$$

These relationships can be used to convert between the various English system units for the various forms of energy.

Most computations involving the energy of the working fluid in an energy transfer system are performed in Btu's. Forms of mechanical energy (such as potential energy, kinetic energy, and mechanical work) and other forms of energy (such as P-V energy) are usually given in foot-pounds-force. These are converted to Btu's by using $1 \text{ Btu} = 778.3 \text{ ft-lbf}$.

This conversion factor is often used. In fact, a constant called the mechanical equivalent of heat, usually denoted by the symbol J and sometimes referred to as *Joule's constant*, is defined as:

$$J = 778 \frac{\text{ft-lbf}}{\text{Btu}}.$$

Power is defined as the time rate of doing work. It is equivalent to the rate of the energy transfer. Power has units of energy per unit time. As with energy, power may be measured in numerous basic units, but the units are equivalent. In the English system, the mechanical units of power are foot-pounds-force per second or per hour (ft-lbf/sec or ft-lbf/hr) and horsepower (hp). The thermal units of power are British thermal units per hour (Btu/hr), and the electrical units of power are watts (W) or kilowatts (kW). For engineering applications, the equivalence of these units is expressed by the following relationships.

$$1 \text{ ft-lbf/sec} = 4.6263 \text{ Btu/hr} = 1.356 \times 10^{-3} \text{ kW}$$

$$1 \text{ Btu/hr} = 0.2162 \text{ ft-lbf/sec} = 2.931 \times 10^{-4} \text{ kW}$$

$$1 \text{ kW} = 3.413 \times 10^3 \text{ Btu/hr} = 737.6 \text{ ft-lbf/sec}$$

Horsepower is related to foot-pounds-force per second (ft-lbf/sec) by the following relationship:

$$1 \text{ hp} = 550.0 \text{ ft-lbf/sec}$$

These relationships can be used to convert the English system units for power.

Summary

The important information from this chapter is summarized below.

Energy, Work, and Heat Summary

- Heat is described as energy in transit. This transfer occurs on a molecular level as a result of temperature differences. The unit of heat is the British thermal unit (Btu).

Latent heat = the amount of heat added or removed to produce only a phase change.

Sensible heat = the heat added or removed that causes a temperature change.

- The following properties were defined:

Specific enthalpy (h) is defined as $h = u + Pv$, where u is the specific internal energy (Btu/lbm) of the system being studied, P is the pressure of the system (lbf/ft²), and v is the specific volume (ft³/lbm) of the system.

Entropy is sometimes referred to as a measure of the inability to do work for a given heat transferred.

THERMODYNAMIC SYSTEMS AND PROCESSES

Defining an appropriate system can greatly simplify a thermodynamic analysis. A thermodynamic system is any three-dimensional region of space that is bounded by one or more surfaces. The bounding surfaces may be real or imaginary and may be at rest or in motion. The boundary may change its size or shape. The region of physical space that lies outside the selected boundaries of the system is called the surroundings or the environment.

EO 1.10 **DESCRIBE the following types of thermodynamic systems:**

- a. **Isolated system**
- b. **Closed system**
- c. **Open system**

EO 1.11 **DEFINE the following terms concerning thermodynamic systems:**

- a. **Thermodynamic surroundings**
- b. **Thermodynamic equilibrium**
- c. **Control volume**
- d. **Steady-state**

EO 1.12 **DESCRIBE the following terms concerning thermodynamic processes:**

- a. **Thermodynamic process**
- b. **Cyclic process**
- c. **Reversible process**
- d. **Irreversible process**
- e. **Adiabatic process**
- f. **Isentropic process**
- g. **Throttling process**
- h. **Polytropic process**

Thermodynamic Systems and Surroundings

Thermodynamics involves the study of various systems. A *system* in thermodynamics is nothing more than the collection of matter that is being studied. A system could be the water within one side of a heat exchanger, the fluid inside a length of pipe, or the entire lubricating oil system for a diesel engine. Determining the boundary to solve a thermodynamic problem for a system will depend on what information is known about the system and what question is asked about the system.

Everything external to the system is called the *thermodynamic surroundings*, and the system is separated from the surroundings by the *system boundaries*. These boundaries may either be fixed or movable. In many cases, a thermodynamic analysis must be made of a device, such as a heat exchanger, that involves a flow of mass into and/or out of the device. The procedure that is followed in such an analysis is to specify a control surface, such as the heat exchanger tube walls. Mass, as well as heat and work (and momentum), may flow across the control surface.

Types of Thermodynamic Systems

Systems in thermodynamics are classified as isolated, closed, or open based on the possible transfer of mass and energy across the system boundaries. An *isolated system* is one that is not influenced in any way by the surroundings. This means that no energy in the form of heat or work may cross the boundary of the system. In addition, no mass may cross the boundary of the system.

A thermodynamic system is defined as a quantity of matter of fixed mass and identity upon which attention is focused for study. A *closed system* has no transfer of mass with its surroundings, but may have a transfer of energy (either heat or work) with its surroundings.

An *open system* is one that may have a transfer of both mass and energy with its surroundings.

Thermodynamic Equilibrium

When a system is in equilibrium with regard to all possible changes in state, the system is in *thermodynamic equilibrium*. For example, if the gas that comprises a system is in thermal equilibrium, the temperature will be the same throughout the entire system.

Control Volume

A *control volume* is a fixed region in space chosen for the thermodynamic study of mass and energy balances for flowing systems. The boundary of the control volume may be a real or imaginary envelope. The *control surface* is the boundary of the control volume.

Steady State

Steady state is that circumstance in which there is no accumulation of mass or energy within the control volume, and the properties at any point within the system are independent of time.

Thermodynamic Process

Whenever one or more of the properties of a system change, a change in the state of the system occurs. The path of the succession of states through which the system passes is called the *thermodynamic process*. One example of a thermodynamic process is increasing the temperature of a fluid while maintaining a constant pressure. Another example is increasing the pressure of a confined gas while maintaining a constant temperature. Thermodynamic processes will be discussed in more detail in later chapters.

Cyclic Process

When a system in a given initial state goes through a number of different changes in state (going through various processes) and finally returns to its initial values, the system has undergone a *cyclic process or cycle*. Therefore, at the conclusion of a cycle, all the properties have the same value they had at the beginning. Steam (water) that circulates through a closed cooling loop undergoes a cycle.

Reversible Process

A *reversible process* for a system is defined as a process that, once having taken place, can be reversed, and in so doing leaves no change in either the system or surroundings. In other words the system and surroundings are returned to their original condition before the process took place. In reality, there are no truly reversible processes; however, for analysis purposes, one uses reversible to make the analysis simpler, and to determine maximum theoretical efficiencies. Therefore, the reversible process is an appropriate starting point on which to base engineering study and calculation.

Although the reversible process can be approximated, it can never be matched by real processes. One way to make real processes approximate reversible process is to carry out the process in a series of small or infinitesimal steps. For example, heat transfer may be considered reversible if it occurs due to a small temperature difference between the system and its surroundings. For example, transferring heat across a temperature difference of 0.00001 °F "appears" to be more reversible than for transferring heat across a temperature difference of 100 °F. Therefore, by cooling or heating the system in a number of infinitesimally small steps, we can approximate a reversible process. Although not practical for real processes, this method is beneficial for thermodynamic studies since the rate at which processes occur is not important.

Irreversible Process

An *irreversible process* is a process that cannot return both the system and the surroundings to their original conditions. That is, the system and the surroundings would not return to their

original conditions if the process was reversed. For example, an automobile engine does not give back the fuel it took to drive up a hill as it coasts back down the hill.

There are many factors that make a process irreversible. Four of the most common causes of irreversibility are friction, unrestrained expansion of a fluid, heat transfer through a finite temperature difference, and mixing of two different substances. These factors are present in real, irreversible processes and prevent these processes from being reversible.

Adiabatic Process

An *adiabatic process* is one in which there is no heat transfer into or out of the system. The system can be considered to be perfectly insulated.

Isentropic Process

An *isentropic process* is one in which the entropy of the fluid remains constant. This will be true if the process the system goes through is reversible and adiabatic. An isentropic process can also be called a constant entropy process.

Polytropic Process

When a gas undergoes a reversible process in which there is heat transfer, the process frequently takes place in such a manner that a plot of the Log P (pressure) vs. Log V (volume) is a straight line. Or stated in equation form $PV^n = \text{a constant}$. This type of process is called a *polytropic process*. An example of a polytropic process is the expansion of the combustion gasses in the cylinder of a water-cooled reciprocating engine.

Throttling Process

A *throttling process* is defined as a process in which there is no change in enthalpy from state one to state two, $h_1 = h_2$; no work is done, $W = 0$; and the process is adiabatic, $Q = 0$. To better understand the theory of the ideal throttling process let's compare what we can observe with the above theoretical assumptions.

An example of a throttling process is an ideal gas flowing through a valve in midposition. From experience we can observe that: $P_{in} > P_{out}$, $vel_{in} < vel_{out}$ (where P = pressure and vel = velocity). These observations confirm the theory that $h_{in} = h_{out}$. Remember $h = u + Pv$ (v = specific volume), so if pressure decreases then specific volume must increase if enthalpy is to remain constant (assuming u is constant). Because mass flow is constant, the change in specific volume is observed as an increase in gas velocity, and this is verified by our observations.

The theory also states $W = 0$. Our observations again confirm this to be true as clearly no "work" has been done by the throttling process. Finally, the theory states that an ideal throttling process is adiabatic. This cannot clearly be proven by observation since a "real" throttling process is not ideal and will have some heat transfer.

Summary

The important information from this chapter is summarized below.

Thermodynamic Systems and Processes Summary

- A thermodynamic system is a collection of matter and space with its boundaries defined in such a way that the energy transfer across the boundaries can be best understood.
- Surroundings are everything not in the system being studied.
- Systems are classified into one of three groups:
 - Isolated system - neither mass nor energy can cross the boundaries
 - Closed system - only energy can cross the boundaries
 - Open system - both mass and energy can cross the boundaries
- A control volume is a fixed region of space that is studied as a thermodynamic system.
- Steady state refers to a condition where the properties at any given point within the system are constant over time. Neither mass nor energy are accumulating within the system.
- A thermodynamic process is the succession of states that a system passes through. Processes can be described by any of the following terms:
 - Cyclic process - a series of processes that results in the system returning to its original state
 - Reversible process - a process that can be reversed resulting in no change in the system or surroundings
 - Irreversible process - a process that, if reversed, would result in a change to the system or surroundings
 - Adiabatic process - a process in which there is no heat transfer across the system boundaries
 - Isentropic process - a process in which the entropy of the system remains unchanged
 - Polytropic process - the plot of $\log P$ vs. $\log V$ is a straight line, $PV^n = \text{constant}$
 - Throttling process - a process in which enthalpy is constant $h_1 = h_2$, work = 0, and which is adiabatic, $Q=0$.

CHANGE OF PHASE

The phase change of materials in a system is very important to thermodynamics. It is possible to design systems to take advantage of the phase changes between solid and liquid or between liquid and vapor to enhance the performance of the system.

EO 1.13 DISTINGUISH between intensive and extensive properties.

EO 1.14 DEFINE the following terms:

- a. **Saturation**
- b. **Subcooled liquid**
- c. **Superheated vapor**
- d. **Critical Point**
- e. **Triple Point**
- f. **Vapor pressure curve**
- g. **Quality**
- h. **Moisture Content**

EO 1.15 DESCRIBE the processes of sublimation, vaporization, condensation, and fusion.

Classification of Properties

As discussed earlier in this module, properties are classified as either intensive or extensive. Properties are *intensive* if independent of the amount of mass present and *extensive* if a function of the amount of mass present. Properties such as pressure, temperature, and density are intensive, whereas volume and mass are extensive. An extensive property may be made intensive by dividing the particular property by the total mass. Total volume (V), which is an extensive property, can be changed to specific volume, which is an intensive property, by dividing by the mass of the system, $v = V/m$. Any specific property (specific volume, specific enthalpy, specific entropy), is an intensive property, as indicated in Figure 3.

The use of intensive and extensive properties is demonstrated in the following discussion. Consider as a system 1 lbm of water contained in the piston-cylinder arrangement of Figure 4. Suppose that the piston and weight maintain a pressure of 14.7 psia in the cylinder and that the initial temperature is 60°F, part (a) of Figure 4. As heat is transferred to the water, the temperature increases. The specific volume increases slightly, and the pressure remains constant. When the temperature reaches 212°F, additional heat transfer results in a change in phase (boiling), as indicated in part (b).

That is, some of the liquid becomes vapor and both the temperature and pressure remain constant, but the specific volume increases considerably. When the last drop of liquid is vaporized, further transfer of heat results in an increase in both temperature and specific volume of the vapor, part (c). In this example, temperature and pressure are intensive, and therefore do not depend upon the amount of mass present. By examining the specific volume (an intensive property) of the water in the piston instead of the volume (an extensive property), we can examine how any portion of the water in the piston changes. Volume by itself tells us nothing about the water in the piston. However, by knowing the specific volume we can tell if the water is a liquid or steam.

It is customary to define some intensive properties associated with extensive properties. For example, the volume per unit mass is called the specific volume,

$$v \equiv \frac{V}{M}$$

and the internal energy per unit mass is called the specific internal energy.

$$u \equiv \frac{U}{M}$$

Intensive properties are useful because they can be tabulated or graphed without reference to the amount of material under study.

Figure 3 Intensive Properties

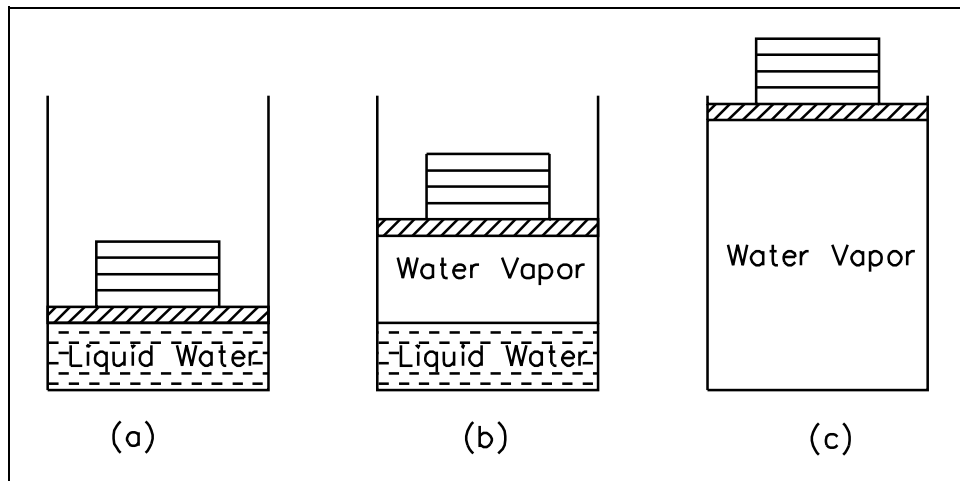


Figure 4 Piston-cylinder Arrangement

Saturation

The term *saturation* defines a condition in which a mixture of vapor and liquid can exist together at a given temperature and pressure. The temperature at which vaporization (boiling) starts to occur for a given pressure is called the *saturation temperature* or *boiling point*. The pressure at which vaporization (boiling) starts to occur for a given temperature is called the *saturation pressure*. For water at 212°F, the saturation pressure is 14.7 psia and, for water at 14.7 psia, the saturation temperature is 212°F. For a pure substance there is a definite relationship between saturation pressure and saturation temperature. The higher the pressure, the higher the saturation temperature. The graphical representation of this relationship between temperature and pressure at saturated conditions is called the *vapor pressure curve*. A typical vapor pressure curve is shown in Figure 5. The vapor/liquid mixture is at saturation when the conditions of pressure and temperature fall on the curve.

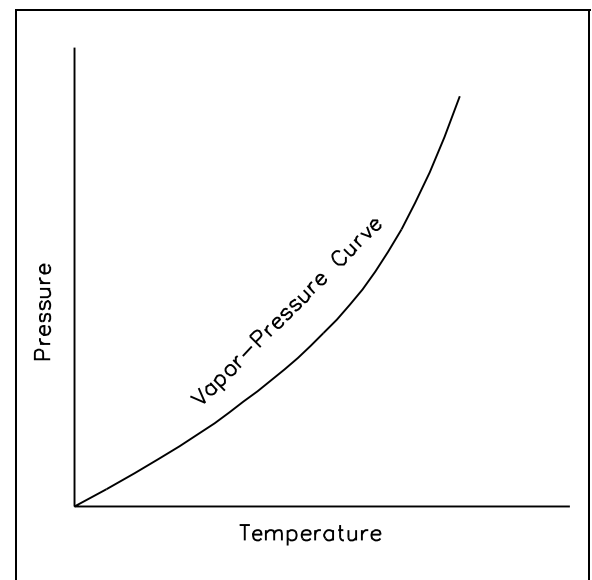


Figure 5 Vapor Pressure Curve

Saturated and Subcooled Liquids

If a substance exists as a liquid at the saturation temperature and pressure, it is called a *saturated liquid*.

If the temperature of the liquid is lower than the saturation temperature for the existing pressure, it is called either a *subcooled liquid* (implying that the temperature is lower than the saturation temperature for the given pressure) or a *compressed liquid* (implying that the pressure is greater than the saturation pressure for the given temperature). Both terms have the same meaning, so either term may be used.

Quality

When a substance exists as part liquid and part vapor at saturation conditions, its *quality* (x) is defined as the ratio of the mass of the vapor to the total mass of both vapor and liquid. Thus, if the mass of vapor is 0.2 lbm and the mass of the liquid is 0.8 lbm, the quality is 0.2 or 20%. Quality is an intensive property. Quality has meaning when the substance is in a saturated state only, at saturation pressure and temperature. The area under the bell-shaped curve on figure 6 shows the region in which quality is important.

$$x = \frac{m_{\text{vapor}}}{(m_{\text{liquid}} + m_{\text{vapor}})} \quad (1-20)$$

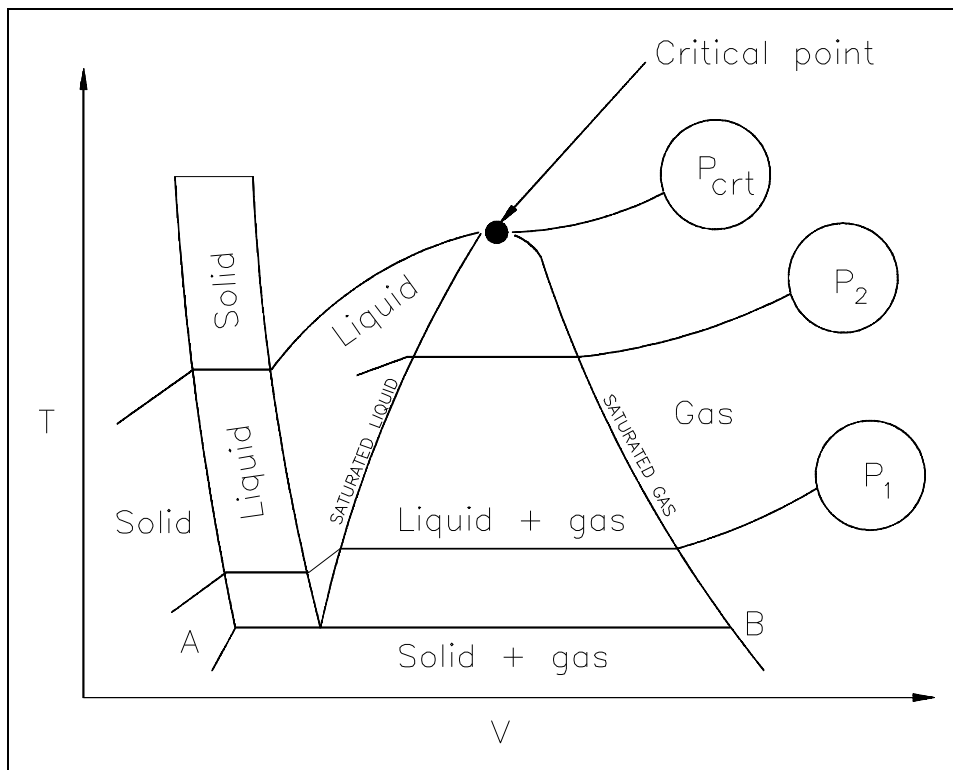


Figure 6 T-V Diagram Showing the Saturation Region

Moisture Content

The *moisture content* of a substance is the opposite of its quality. Moisture (M) is defined as the ratio of the mass of the liquid to the total mass of both liquid and vapor. The moisture of the mixture in the previous paragraph would be 0.8 or 80%. The following equations show how to calculate the moisture of a mixture and the relationship between quality and moisture.

$$M = \frac{m_{\text{liquid}}}{(m_{\text{liquid}} + m_{\text{vapor}})} \quad (1-21)$$

$$M = 1 - x$$

Saturated and Superheated Vapors

If a substance exists entirely as vapor at saturation temperature, it is called *saturated vapor*. Sometimes the term dry saturated vapor is used to emphasize that the quality is 100%. When the vapor is at a temperature greater than the saturation temperature, it is said to exist as *superheated vapor*. The pressure and temperature of superheated vapor are independent properties, since the temperature may increase while the pressure remains constant. Actually, the substances we call gases are highly superheated vapors.

Constant Pressure Heat Addition

Consider the plot on the temperature-volume diagram of Figure 7, viewing the constant-pressure line that represents the states through which the water of the previous discussion passes as it is heated from the initial state of 14.7 psia and 60°F. Let state A represent the initial state and state B represent the start of the saturated liquid line (212°F). Therefore, line AB represents the process in which the liquid is heated from the initial temperature to the saturation temperature.

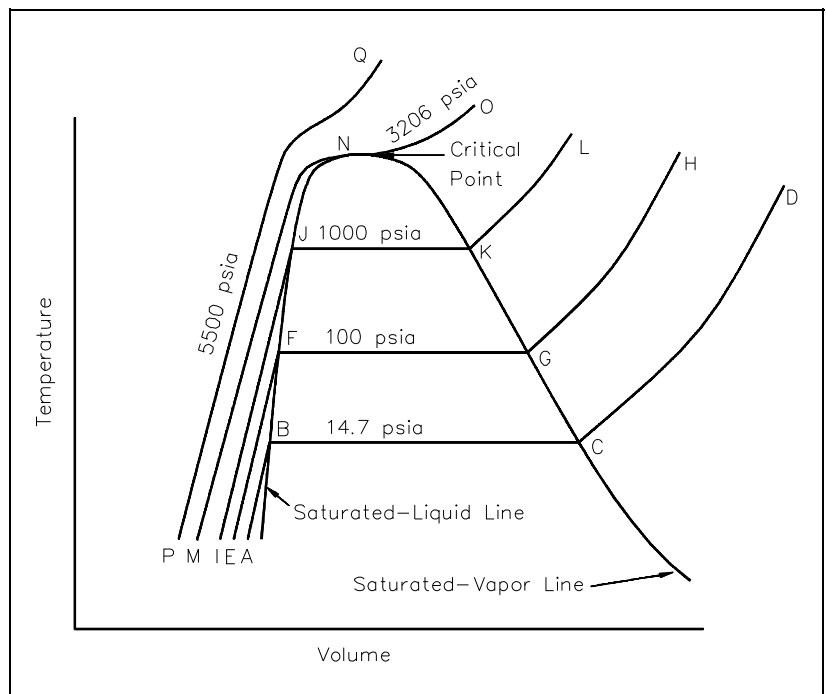


Figure 7 T-V Diagram

Point C is the saturated vapor state, and line BC is the constant-temperature process in which the change of phase from liquid to vapor occurs. Line CD represents the process in which the steam is super-heated at constant pressure. Temperature and volume both increase during the process.

Now let the process take place at a constant pressure of 100 psia, beginning from an initial temperature of 60°F. Point E represents the initial state, the specific volume being slightly less than 14.7 psia and 60°F. Vaporization now begins at point F, where the temperature is 327.8°F. Point G is the saturated-vapor state, and line GH is the constant-pressure process in which the steam is superheated.

In a similar manner, a constant pressure of 1000 psia is represented by line IJKL, the saturation temperature being 544.6°F.

Critical Point

At a pressure of 3206.2 psia, represented by line MNO, there is no constant-temperature vaporization process. Rather, point N is a point of inflection, with the slope being zero. This point is called the *critical point*, and at the critical point the saturated-liquid and saturated-vapor states are identical. The temperature, pressure, and specific volume at the critical point are called the critical temperature, critical pressure, and critical volume.

A constant pressure process greater than the critical pressure is represented by line PQ. There is no definite change in phase from liquid to vapor and no definite point at which there is a change from the liquid phase to the vapor phase. For pressures greater than the critical pressure, the substance is usually called a liquid when the temperature is less than the critical temperature (705.47°F) and a vapor or gas when the temperature is greater than the critical temperature. In the figure, line NJFB represents the saturated liquid line, and the line NKGC represents the saturated vapor line.

Fusion

Consider one further experiment with the piston-cylinder arrangement of Figure 4. Suppose the cylinder contained 1 lbm of ice at 0°F, 14.7 psia. When heat is transferred to the ice, the pressure remains constant, the specific volume increases slightly, and the temperature increases until it reaches 32°F, at which point the ice melts while the temperature remains constant. In this state the ice is called a saturated solid. For most substances, the specific volume increases during this melting process, but for water the specific volume of the liquid is less than the specific volume of the solid. This causes ice to float on water. When all the ice is melted, any further heat transfer causes an increase in temperature of the liquid. The process of melting is also referred to as *fusion*. The heat added to melt ice into a liquid is called the latent heat of fusion.

Sublimation

If the initial pressure of the ice at 0°F is 0.0505 psia, heat transfer to the ice first results in an increase in temperature to 20°F. At this point, however, the ice passes directly from the solid phase to the vapor phase in the process known as *sublimation*. Sublimation is a special term used for cases in which the transition between the solid phase and the vapor phase occurs directly, without passing through the liquid phase. Further heat transfer would result in superheating the vapor.

Triple Point

Finally, consider an initial pressure of the ice of 0.08854 psia. Again, as a result of heat transfer, the temperature will increase until it reaches 32°F. At this point, however, further heat transfer may result in some of the ice becoming vapor and some becoming liquid because it is possible to have the three phases in equilibrium. This is called the *triple point*, defined as the state in which all three phases may be present in equilibrium.

Figure 8 is a pressure-temperature diagram for water that shows how the solid, liquid, and vapor phases may exist together in equilibrium. Along the sublimation line, the solid and vapor phases are in equilibrium, along the fusion line, the solid and liquid phases are in equilibrium; and along the vaporization line, the liquid and vapor phases are in equilibrium. The only point at which all three phases may exist in equilibrium is the triple point. The temperature and pressure for the triple point of water are 32.02°F and 0.08865 psia. The vaporization line ends at the critical point because there is no distinct change from the liquid phase to the vapor phase above the critical point.

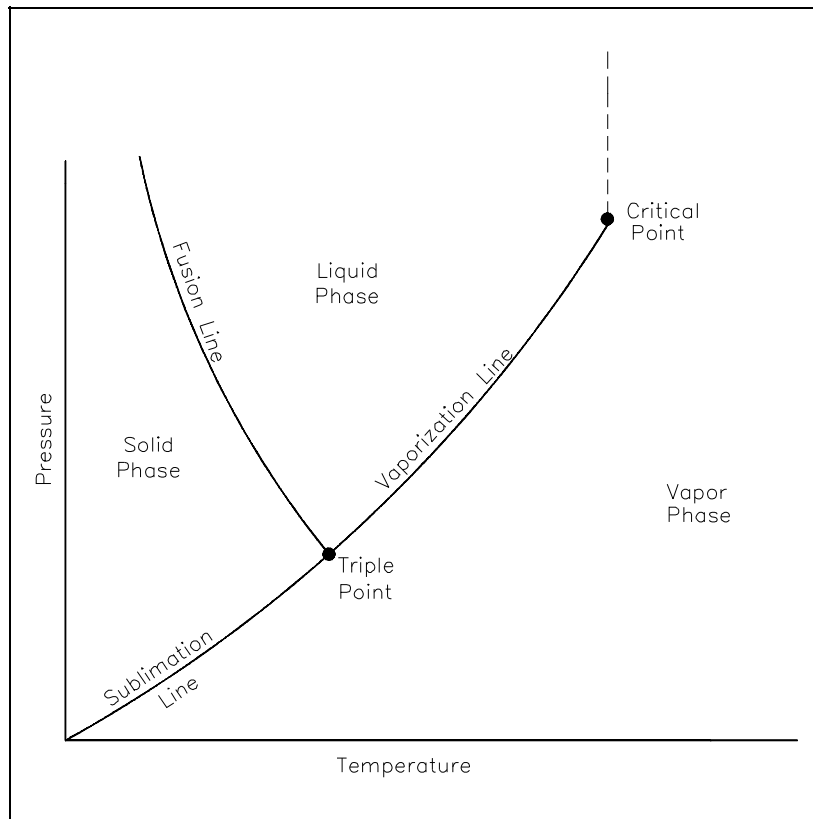


Figure 8 Pressure-Temperature Diagram

Condensation

All the processes discussed on the preceding pages (vaporization, sublimation, and fusion) occur during a heat addition to a substance. If heat is removed from a substance, the opposite of the described processes will occur.

As previously described, a heat addition at a constant pressure to a saturated liquid will cause the liquid to evaporate (change phase from liquid to vapor). If heat is removed at a constant pressure from a saturated vapor, *condensation* will occur and the vapor will change phase to liquid. So the processes of vaporization and condensation are the exact opposite of each other.

Similarly, freezing is the opposite process of melting and fusion. Sublimation also has an opposite process in which a gas goes directly to solid, but this process is not normally referred to with a unique term.

Summary

The important information from this chapter is summarized on the following page.

Change of Phase Summary

- Classification of Properties

Intensive properties are independent of mass (temperature, pressure, or any specific property)

Extensive properties are a function of the mass of the system (mass, volume)

- The following terms were defined in this chapter:

Saturation	-	combination of temperature and pressure at which a mixture of vapor and liquid can exist at equilibrium
Subcooled liquid	-	a liquid at a temperature below saturation temperature for its pressure
Superheated vapor	-	a vapor at a temperature above saturation temperature for its pressure
Critical point	-	the temperature and pressure above which there is no distinction between the liquid and vapor phases
Triple point	-	the temperature and pressure at which all three phases can exist in equilibrium
Vapor pressure curve	-	a graphical representation of the relationship between temperature and pressure at saturated conditions
Quality	-	the fraction of the total mass of a mixture that is in the vapor phase
Moisture Content	-	the fraction of the total mass of a mixture that is in the liquid phase

Change of Phase Summary (Cont.)

- The following terms are labels for processes that occur when a substance changes between the three phases of matter: solid, liquid, and vapor.

Sublimation - change of phase from solid to vapor

Vaporization - change of phase from liquid to vapor

Condensation - change of phase from vapor to liquid

Fusion or melting - change of phase from solid to liquid

PROPERTY DIAGRAMS AND STEAM TABLES

Property diagrams and steam tables are used in studying the theoretical and actual properties and efficiencies of a given system.

- EO 1.16** **Given a Mollier diagram and sufficient information to indicate the state of the fluid, DETERMINE any unknown properties for the fluid.**
- EO 1.17** **Given a set of steam tables and sufficient information to indicate the state of the fluid, DETERMINE any unknown properties for the fluid.**
- EO 1.18** **DETERMINE the change in the enthalpy of a fluid as it passes through a system component, given the state of the fluid at the inlet and outlet of the component and either steam tables or a Mollier diagram.**
-

Property Diagrams

The phases of a substance and the relationships between its properties are most commonly shown on *property diagrams*. A large number of different properties have been defined, and there are some dependencies between properties. For example, at standard atmospheric pressure and temperature above 212°F, water exists as steam and not a liquid; it exists as a liquid at temperatures between 32°F and 212°F; and, it exists as ice at temperatures below 32°F. In addition, the properties of ice, water, and steam are related. Saturated steam at 212°F and standard atmospheric pressure has a specific volume of 26.8 ft³/lbm. At any other temperature and pressure, saturated steam has a different specific volume. For example, at 544°F and 1000 psia pressure, its specific volume is 0.488 ft³/lbm.

There are five basic properties of a substance that are usually shown on property diagrams. These are: pressure (P), temperature (T), specific volume (v), specific enthalpy (h), and specific entropy (s). When a mixture of two phases, such as water and steam, is involved, a sixth property, quality (x), is also used.

There are six different types of commonly encountered property diagrams. These are: Pressure-Temperature (P-T) diagrams, Pressure-Specific Volume (P-v) diagrams, Pressure-Enthalpy (P-h) diagrams, Enthalpy-Temperature (h-T) diagrams, Temperature-entropy (T-s) diagrams, and Enthalpy-Entropy (h-s) or Mollier diagrams.

Pressure-Temperature (P-T) Diagram

A P-T diagram is the most common way to show the phases of a substance. Figure 9 is the P-T diagram for pure water. A P-T diagram can be constructed for any pure substance. The line that separates the solid and vapor phases is called the sublimation line. The line that separates the solid and liquid phases is called the fusion line. The line that separates the liquid and vapor phases is called the vaporization line. The point where the three lines meet is called the triple point. The triple point is the only point at which all three phases can exist in equilibrium. The point where the vaporization line ends is called the critical point. At temperatures and pressures greater than those at the critical point, no substance can exist as a liquid no matter how great a pressure is exerted upon it.

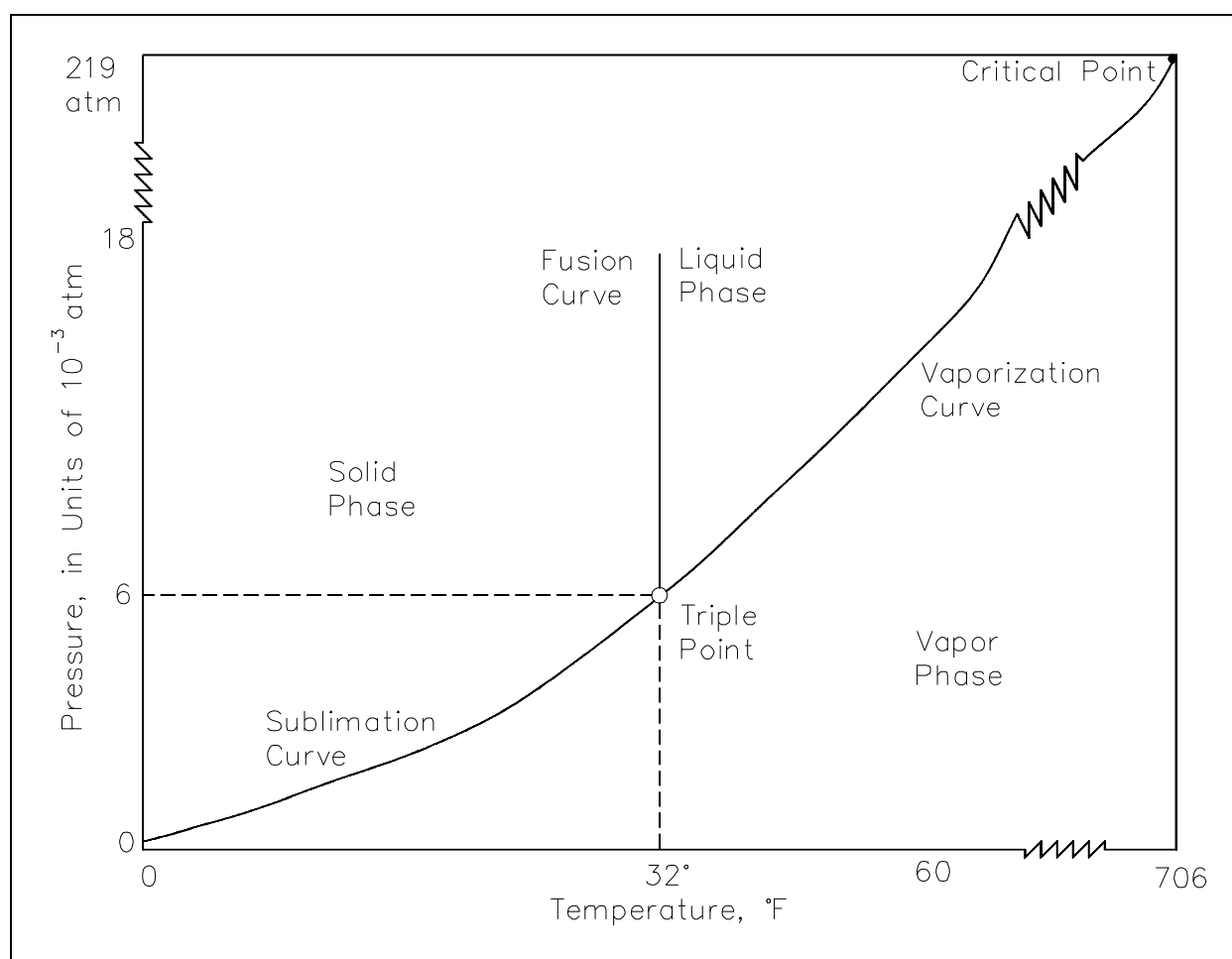


Figure 9 P-T Diagram for Water

Pressure-Specific Volume (P-v) Diagram

A P-v diagram is another common type of property diagram. Figure 10 is the P-v diagram for pure water. A P-v diagram can be constructed for any pure substance. A P-v diagram is different from a P-T diagram in one particularly important way. There are regions on a P-v diagram in which two phases exist together. In the liquid-vapor region in Figure 10, water and steam exist together.

For example, at point A, water with a specific volume (v_f), given by point B, exists together with steam with a specific volume (v_g), given by point C. The dotted lines on Figure 10 are lines of constant temperature. The quality of the mixture at any point in the liquid-vapor region can be found because the specific volumes of water, steam, and the mixture are all known. The quality can be found using the following relationship.

$$v = xv_g + (1 - x)v_f$$

$$x = \frac{v - v_f}{v_g - v_f} = \frac{v - v_f}{v_{fg}}$$

where:

v = specific volume of the mixture (ft^3/lbm)

x = quality of the mixture (no units)

v_g = specific volume of the vapor (ft^3/lbm)

v_f = specific volume of the liquid (ft^3/lbm)

v_{fg} = specific volume change of vaporization (ft^3/lbm) or $v_{fg} = v_g - v_f$

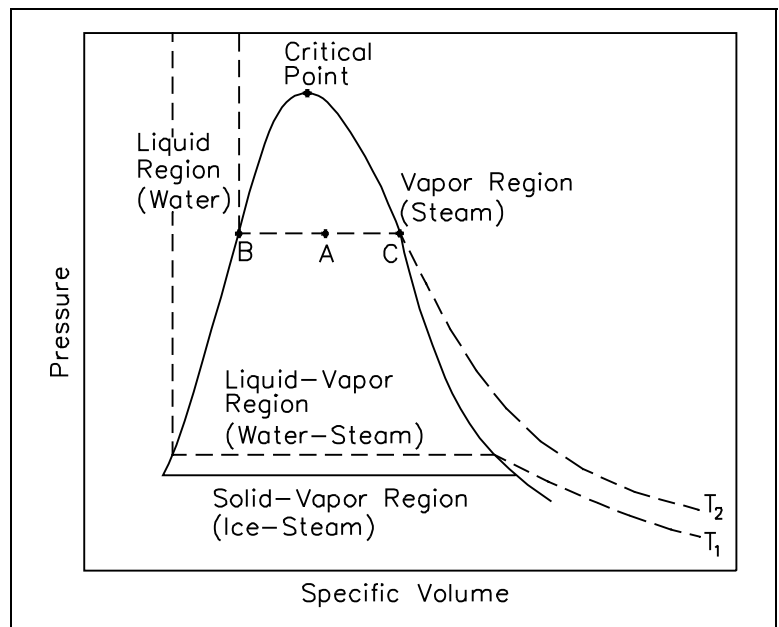


Figure 10 P-v Diagram for Water

Pressure-Enthalpy (P-h) Diagram

A P-h diagram exhibits the same features as a P-v diagram. Figure 11 is the P-h diagram for pure water. A P-h diagram can be constructed for any pure substance. Like the P-v diagram, there are regions on a P-h diagram in which two phases exist together. In the liquid-vapor region in Figure 11, water and steam exist together. For example, at point A, water with an enthalpy (h_f), given by point B, exists together with steam with an enthalpy (h_g), given by point C. The quality of the mixture at any point in the liquid-vapor region can be found using the following relationship.

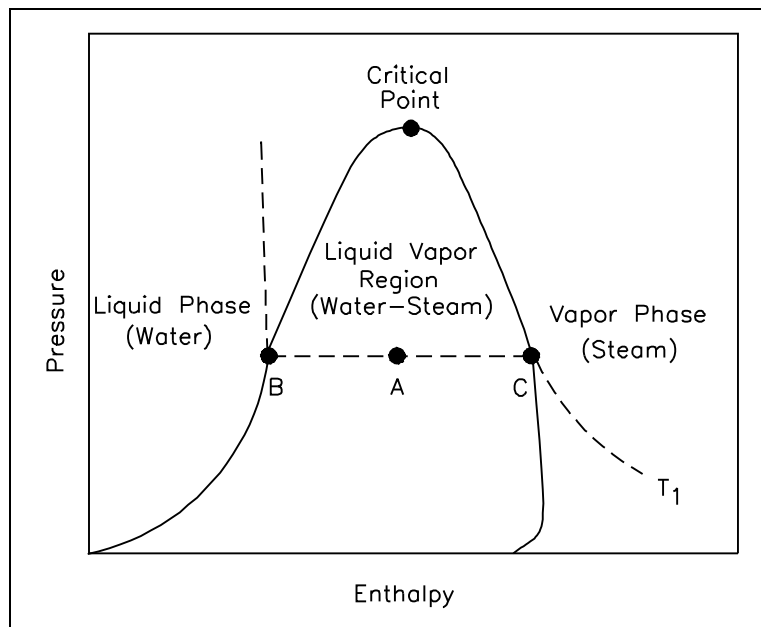


Figure 11 P-h Diagram for Water

$$h = xh_g + (1 - x)h_f$$

$$x = \frac{h - h_f}{h_{fg}}$$

where:

h = specific enthalpy of the mixture (Btu/lbm)

x = quality of the mixture (no units)

h_g = specific enthalpy of the saturated vapor (Btu/lbm)

h_f = specific enthalpy of the saturated liquid (Btu/lbm)

h_{fg} = specific enthalpy change of vaporization (Btu/lbm) or $h_{fg} = h_g - h_f$

Enthalpy-Temperature (h-T) Diagram

An h-T diagram exhibits the same features as on the previous property diagrams. Figure 12 is the h-T diagram for pure water. An h-T diagram can be constructed for any pure substance. As in the previous property diagrams, there are regions on the h-T diagram in which two phases exist together. The region between the saturated liquid line and the saturated vapor line represents the area of two phases existing at the same time. The vertical distance between the two saturation lines represents the latent heat of vaporization. If pure water existed at point A on the saturated liquid line and an amount of heat was added equal to the latent heat of vaporization, then the water would change phase from a saturated liquid to a saturated vapor (point B), while maintaining a constant temperature. As shown in Figure 12, operation outside the saturation lines results in a subcooled liquid or superheated steam.

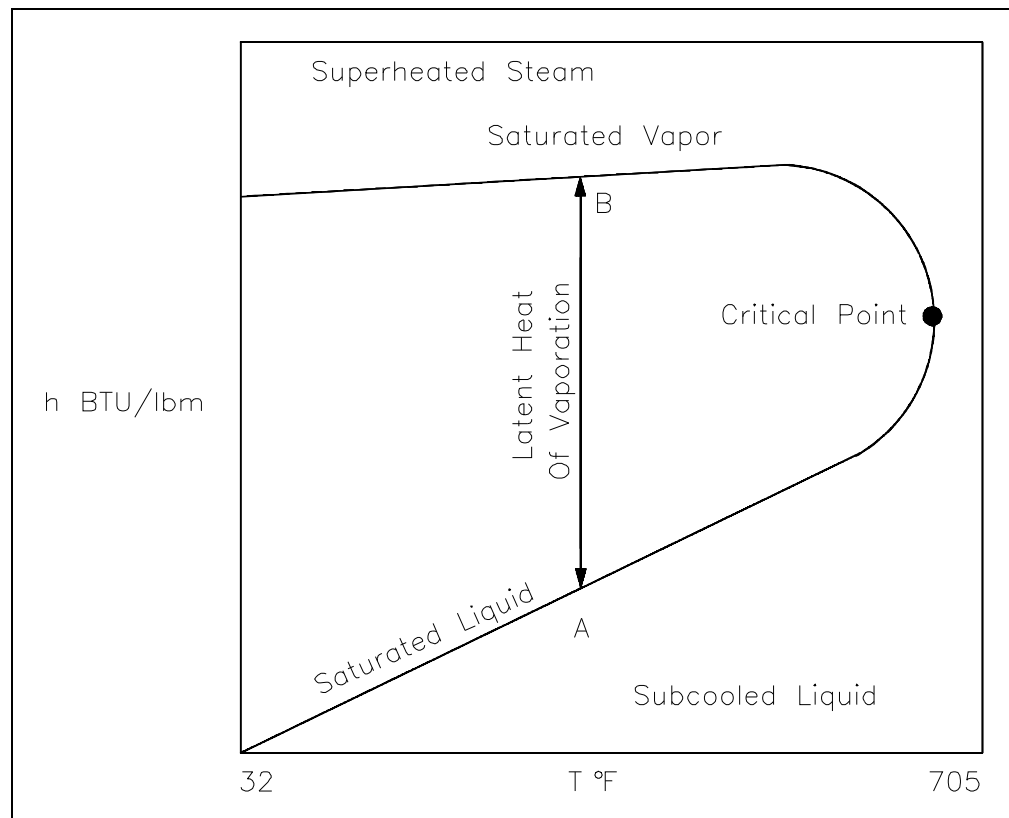


Figure 12 h-T Diagram for Water

The quality of the mixture at any point in the liquid-vapor region can be found using the same relationship as shown for the P-h diagram.

$$x = \frac{h - h_f}{h_{fg}}$$

Temperature-Entropy (T-s) Diagram

A T-s diagram is the type of diagram most frequently used to analyze energy transfer system cycles. This is because the work done by or on the system and the heat added to or removed from the system can be visualized on the T-s diagram. By the definition of entropy, the heat transferred to or from a system equals the area under the T-s curve of the process. Figure 13 is the T-s diagram for pure water. A T-s diagram can be constructed for any pure substance. It exhibits the same features as P-v diagrams.

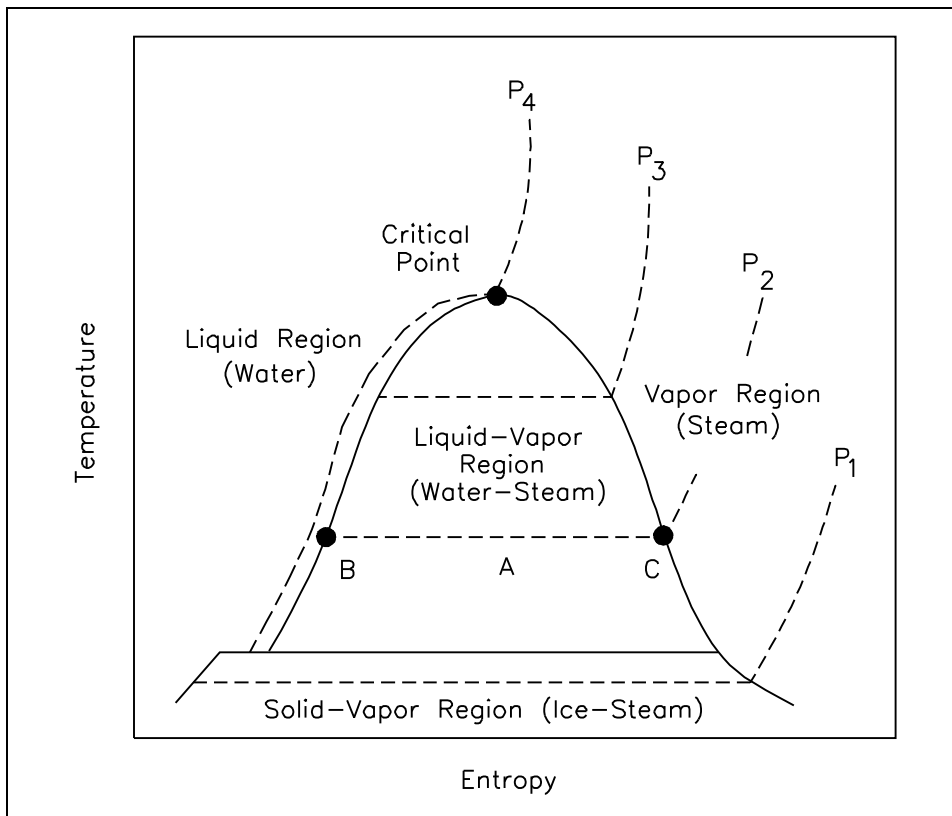


Figure 13 T-s Diagram for Water

In the liquid-vapor region in Figure 13, water and steam exist together. For example, at point A, water with an entropy (s_f) given by point B, exists together with steam with an entropy (s_g) given by point C. The quality of the mixture at any point in the liquid-vapor region can be found using the following relationship.

$$s = xs_g + (1 - x)s_f$$

$$x = \frac{s - s_f}{s_{fg}}$$

where:

s = specific entropy of the mixture (Btu/lbm-°R)

x = quality of the mixture (no units)

s_g = specific entropy of the saturated vapor (Btu/lbm-°R)

s_f = specific entropy of the saturated liquid (Btu/lbm-°R)

s_{fg} = specific entropy change of vaporization (Btu/lbm-°R) or $s_{fg} = s_g - s_f$

Enthalpy-Entropy (h-s) or Mollier Diagram

The Mollier diagram, shown in Figure A-1 of Appendix A, is a chart on which enthalpy (h) versus entropy (s) is plotted. It is sometimes known as the h-s diagram and has an entirely different shape from the T-s diagrams. The chart contains a series of constant temperature lines, a series of constant pressure lines, a series of constant moisture or quality lines, and a series of constant superheat lines. The Mollier diagram is used only when quality is greater than 50% and for superheated steam.

Steam Tables

Steam tables consist of two sets of tables of the energy transfer properties of water and steam: saturated steam tables and superheated steam tables. Portions of the tables are shown in Figure A-2 of Appendix A. Both sets of tables are tabulations of pressure (P), temperature (T), specific volume (v), specific enthalpy (h), and specific entropy (s). The following notation is used in steam tables. Some tables use v for v (specific volume) because there is little possibility of confusing it with velocity.

T = temperature (°F)

P = pressure (psi)

v = specific volume (ft³/lbm)

v_f = specific volume of saturated liquid (ft³/lbm)

v_g = specific volume of saturated vapor (ft³/lbm)

v_{fg}	=	specific volume change of vaporization (ft ³ /lbm)
h	=	specific enthalpy (Btu/lbm)
h_f	=	specific enthalpy of saturated liquid (Btu/lbm)
h_g	=	specific enthalpy of saturated vapor (Btu/lbm)
h_{fg}	=	specific enthalpy change of vaporization (Btu/lbm)
s	=	specific entropy (Btu/lbm-°R)
s_f	=	specific entropy of saturated liquid (Btu/lbm-°R)
s_g	=	specific entropy of saturated vapor (Btu/lbm-°R)
s_{fg}	=	specific entropy change of vaporization (Btu/lbm-°R)
Sh	=	number of degrees of superheat (°F)

The saturated steam tables give the energy transfer properties of saturated water and saturated steam for temperatures from 32 to 705.47°F (the critical temperature) and for the corresponding pressure from 0.08849 to 3208.2 psi. Normally, the saturated steam tables are divided into two parts: temperature tables, which list the properties according to saturation temperature (T_{sat}); and pressure tables, which list them according to saturation pressure (P_{sat}). Figure A-2 shows a portion of a typical saturated steam temperature table and a portion of a typical saturated steam pressure table. The values of enthalpy and entropy given in these tables are measured relative to the properties of saturated liquid at 32°F. Hence, the enthalpy (h_f) of saturated liquid and the entropy (s_f) of saturated liquid have values of approximately zero at 32°F.

Most practical applications using the saturated steam tables involve steam-water mixtures. The key property of such mixtures is steam quality (x), defined as the mass of steam present per unit mass of steam-water mixture, or steam moisture content (y), defined as the mass of water present per unit mass of steam-water mixture. The following relationships exist between the quality of a liquid-vapor mixture and the specific volumes, enthalpies, or entropies of both phases and of the mixture itself. These relationships are used with the saturated steam tables.

$$v = xv_g + (1 - x)v_f$$

$$x = \frac{v - v_f}{v_{fg}}$$

$$h = xh_g + (1 - x)h_f$$

$$x = \frac{h - h_f}{h_{fg}}$$

$$s = xs_g + (1 - x)s_f$$

$$x = \frac{s - s_f}{s_{fg}}$$

In order to solve problems in Thermodynamics, information concerning the "state" of the substance studied must be obtained. Usually, two properties (for example, v , p , T , h , s) of the substance must be known in order to determine the other needed properties. These other properties are usually obtained utilizing either the Mollier diagram (if the substance is steam) or the saturated and superheated steam tables, as shown in the Figures A-1 and A-2.

The following two examples illustrate the use of the Mollier diagram and the steam tables.

Example 1: Use of Mollier Chart.

Superheated steam at 700 psia and 680°F is expanded at constant entropy to 140 psia. What is the change in enthalpy?

Solution:

Use the Mollier Chart. Locate point 1 at the intersection of the 700 psia and the 680°F line. Read $h = 1333$ Btu/lbm.

Follow the entropy line downward vertically to the 140 psia line and read $h = 1178$ Btu/lbm.

$$\Delta h = 1178 - 1333 = -155 \text{ Btu/lbm}$$

Example 2: Use of steam tables

What are the specific volume, enthalpy, and entropy of steam having a quality of 90% at 400 psia?

Solution:

From the steam tables at 400 psia:

$$v_f = 0.01934 \qquad v_g = 1.14162 \qquad h_f = 424.2$$

$$h_{fg} = 780.4 \qquad s_f = 0.6217 \qquad s_{fg} = 0.8630$$

$$v = v_f + x(v_{fg})$$

$$v = 0.01934 + (0.9)(1.14162) = 1.0468 \text{ ft}^3/\text{lbm}$$

$$h = h_f + x(h_{fg})$$

$$h = 424.2 + (0.9)(780.4) = 1126.56 \text{ Btu/lbm}$$

$$s = s_f + x(s_{fg})$$

$$s = 0.6217 + (0.9)(0.8630) = 1.3984 \text{ Btu/lbm-}^\circ\text{R}$$

If the substance is not water vapor, the "state" of the substance is usually obtained through the use of T-s (temperature-entropy) and h-s (enthalpy-entropy) diagrams, available in most thermodynamics texts for common substances. The use of such diagrams is demonstrated by the following two examples.

Example 3: Use of the h-s diagram

Mercury is used in a nuclear facility. What is the enthalpy of the mercury if its pressure is 100 psia and its quality is 70%?

Solution:

From the mercury diagram, Figure A-3 of Appendix A, locate the pressure of 100 psia. Follow that line until reaching a quality of 70%. The intersection of the two lines gives an enthalpy that is equal to $h = 115 \text{ Btu/lbm}$.

Example 4: Use of the T-s diagram

Carbon dioxide is used in a particular process in which the pressure is 100 psia and the temperature is 100°F. What is the enthalpy value of the gas?

Solution:

From the carbon dioxide diagram, Figure A-4 of Appendix A, locate the pressure of 100 psia. Follow that line until reaching a temperature of 100°F. The intersection of the two lines gives an enthalpy that is equal to $h = 316$ Btu/lbm.

Once the various states have been fixed for the particular process the substance has passed through (for example, going from a saturated liquid state to a compressed liquid state across a pump), energy exchanges may be determined as was shown in Example 1. The energy exchanges are never 100 percent efficient, as already discussed. The degree of efficiency obtained by the system depends upon the process through which the system has passed. Generally, the efficiency of a component depends upon how much friction exists in the flow of the substance, the pressure drops within the system, the inlet and outlet temperatures, and various other factors. The properties affecting the efficiency of the system are determined by use of the charts and diagrams mentioned in this section.

When power cycles are utilized for large systems, the efficiency of each component should be maximized in order to have the highest possible overall efficiency for the system. Each component affects the system efficiency in a different manner. To maximize efficiency, the practical approach to large systems is to have multistage expansion with reheat between stages and regenerators in the system where applicable.

Summary

The important information from this chapter is summarized below.

Property Diagrams and Steam Tables Summary

- The Mollier diagram can be used to determine various properties of a fluid.

Mollier diagram is an h versus s plot.

Can only be used when quality is greater than 50% and for superheated steam.

Contains a series of constant temperature, constant pressure, constant moisture content, and constant superheat lines.

- The steam tables can be used to determine various properties of water using the following equations.

$$v = xv_g + (1 - x)v_f$$

$$h = xh_g + (1 - x)h_f$$

$$s = xs_g + (1 - x)s_f$$

$$x = \frac{v - v_f}{v_{fg}}$$

$$x = \frac{h - h_f}{h_{fg}}$$

$$x = \frac{s - s_f}{s_{fg}}$$

- The change in enthalpy of a fluid as it passes through a component can be determined using a Mollier diagram on steam tables.

FIRST LAW OF THERMODYNAMICS

The First Law of Thermodynamics is a balance of the various forms of energy as they pertain to the specified thermodynamic system (control volume) being studied.

- EO 1.19** **STATE the First Law of Thermodynamics.**
- EO 1.20** **Using the First Law of Thermodynamics, ANALYZE an open system including all energy transfer processes crossing the boundaries.**
- EO 1.21** **Using the First Law of Thermodynamics, ANALYZE cyclic processes for a thermodynamic system.**
- EO 1.22** **Given a defined system, PERFORM energy balances on all major components in the system.**
- EO 1.23** **Given a heat exchanger, PERFORM an energy balance across the two sides of the heat exchanger.**
- EO 1.24** **IDENTIFY the path(s) on a T-s diagram that represents the thermodynamic processes occurring in a fluid system.**
-

First Law of Thermodynamics

The First Law of Thermodynamics states:

Energy can neither be created nor destroyed, only altered in form.

For any system, energy transfer is associated with mass and energy crossing the control boundary, external work and/or heat crossing the boundary, and the change of stored energy within the control volume. The mass flow of fluid is associated with the kinetic, potential, internal, and "flow" energies that affect the overall energy balance of the system. The exchange of external work and/or heat complete the energy balance.

The First Law of Thermodynamics is referred to as the Conservation of Energy principle, meaning that energy can neither be created nor destroyed, but rather transformed into various forms as the fluid within the control volume is being studied. The energy balance spoken of here is maintained within the system being studied. The system is a region in space (control volume) through which the fluid passes. The various energies associated with the fluid are then observed as they cross the boundaries of the system and the balance is made.

As discussed in previous chapters of this module, a system may be one of three types: isolated, closed, or open. The open system, the most general of the three, indicates that mass, heat, and external work are allowed to cross the control boundary. The balance is expressed in words as: all energies into the system are equal to all energies leaving the system plus the change in storage of energies within the system. Recall that energy in thermodynamic systems is composed of kinetic energy (KE), potential energy (PE), internal energy (U), and flow energy (P_L); as well as heat and work processes.

$$\Sigma (\text{all energies in}) = \Sigma (\text{all energies out}) + \Delta(\text{energy stored in system})$$

$$\Sigma E_{in} = \Sigma E_{out} + \Delta E \text{ storage}$$

For most industrial plant applications that most frequently use cycles, there is no change in storage (i.e. heat exchangers do not swell while in operation).

In equation form, the balance appears as indicated on Figure 14.

where:

$$\dot{Q} = \text{heat flow into the system (Btu/hr)}$$

$$\dot{m}_{in} = \text{mass flow rate into the system (lbm/hr)}$$

$$u_{in} = \text{specific internal energy into the system (Btu/lbm)}$$

$$P_{in}v_{in} = \text{pressure-specific volume energy into the system (ft-lbf/lbm)}$$

$$\frac{\bar{V}_{in}^2}{2g_c} = \text{kinetic energy into the system (ft-lbf /lbm) where}$$

$$\bar{V}_{in} = \text{average velocity of fluid (ft/sec)}$$

$$g_c = \text{the gravitational constant (32.17 ft-lbm/lbf-sec}^2\text{)}$$

$$\frac{g}{g_c} Z_{in} = \text{potential energy of the fluid entering the system (ft-lbf/lbm) where}$$

$$Z_{in} = \text{height above reference level (ft)}$$

$$g = \text{acceleration due to gravity (ft/sec}^2\text{)}$$

$$g_c = \text{the gravitational constant (32.17 ft-lbm/lbf-sec}^2\text{)}$$

- \dot{W} = work flow out of the system (ft-lbf/hr)
- \dot{m}_{out} = mass flow rate out of the system (lbm/hr)
- u_{out} = specific internal energy out of the system (Btu/lbm)
- $P_{out} v_{out}$ = pressure-specific volume energy out of the system (ft-lbf/lbm)
- $\frac{\bar{V}_{out}^2}{2g_c}$ = kinetic energy out the system (ft-lbf/lbm)
- $\frac{g}{g_c} Z_{out}$ = potential energy out of the system (ft-lbf/lbm)

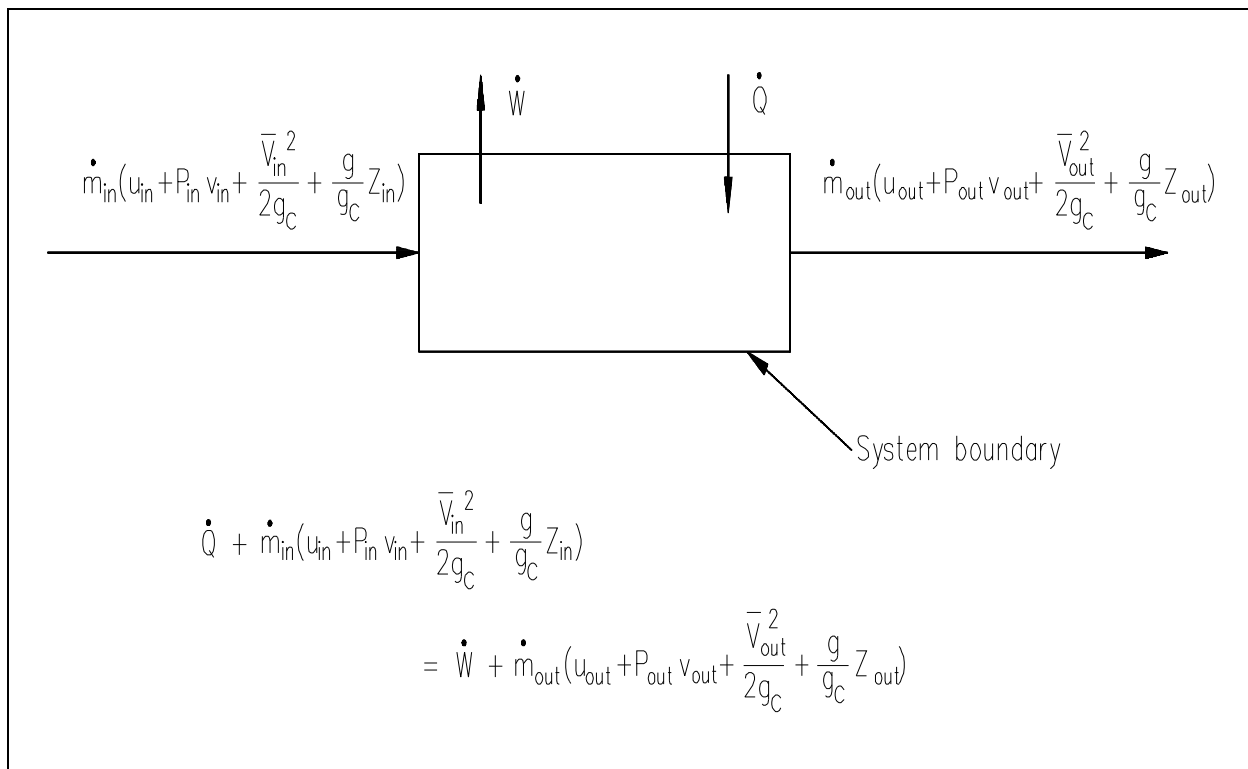


Figure 14 First Law of Thermodynamics

Heat and/or work can be directed into or out of the control volume. But, for convenience and as a standard convention, the net energy exchange is presented here with the net heat exchange assumed to be into the system and the net work assumed to be out of the system. If no mass crosses the boundary, but work and/or heat do, then the system is referred to as a "closed" system. If mass, work and heat do not cross the boundary (that is, the only energy exchanges taking place are within the system), then the system is referred to as an isolated system. Isolated and closed systems are nothing more than specialized cases of the open system. In this text, the open system approach to the First Law of Thermodynamics will be emphasized because it is more general. Also, almost all practical applications of the first law require an open system analysis.

An understanding of the control volume concept is essential in analyzing a thermodynamic problem or constructing an energy balance. Two basic approaches exist in studying Thermodynamics: the control mass approach and the control volume approach. The former is referred to as the LeGrange approach and the latter as the Eulerian approach. In the control mass concept, a "clump" of fluid is studied with its associated energies. The analyzer "rides" with the clump wherever it goes, keeping a balance of all energies affecting the clump.

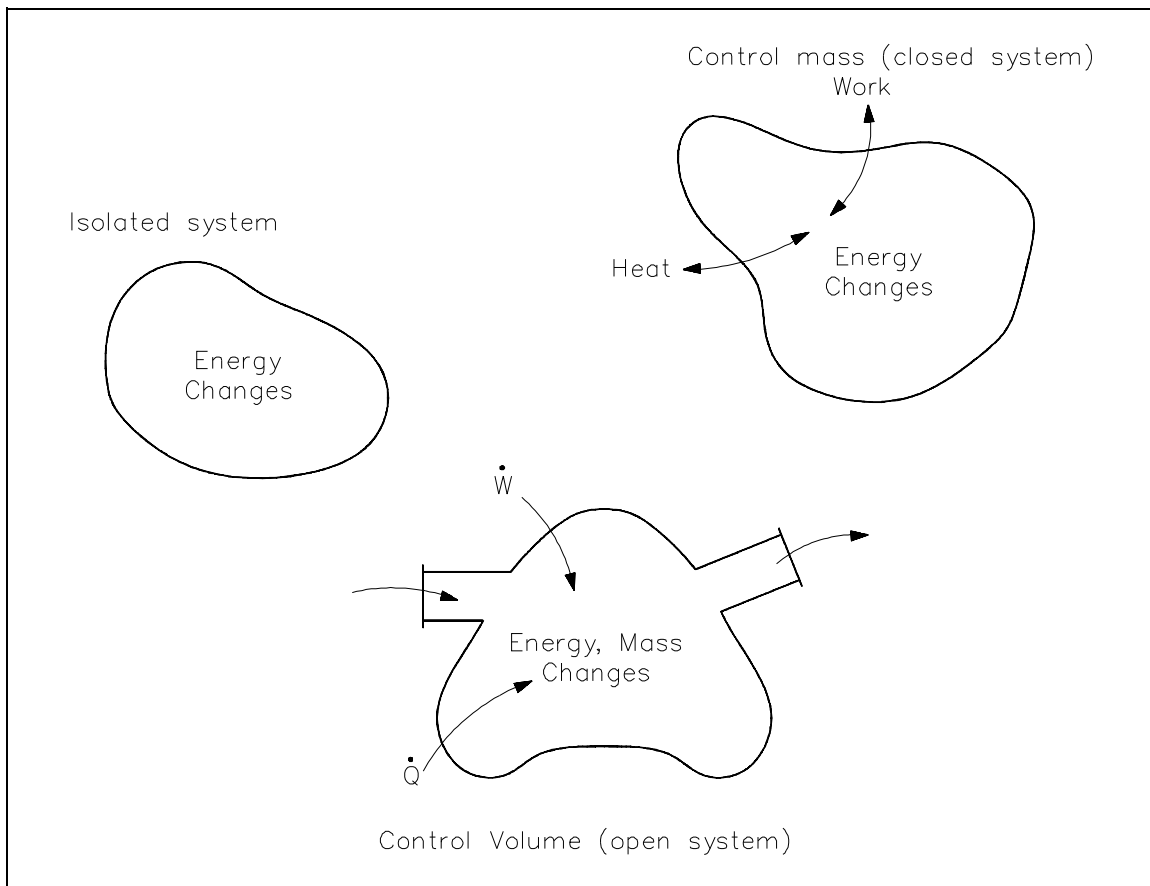


Figure 15 Control Volume Concepts

The control volume approach is one in which a fixed region in space is established with specified control boundaries, as shown in Figure 15. The energies that cross the boundary of this control volume, including those with the mass crossing the boundary, are then studied and the balance performed. The control volume approach is usually used today in analyzing thermodynamic systems. It is more convenient and requires much less work in keeping track of the energy balances. Examples of control volume applications are included in Figures 16-18.

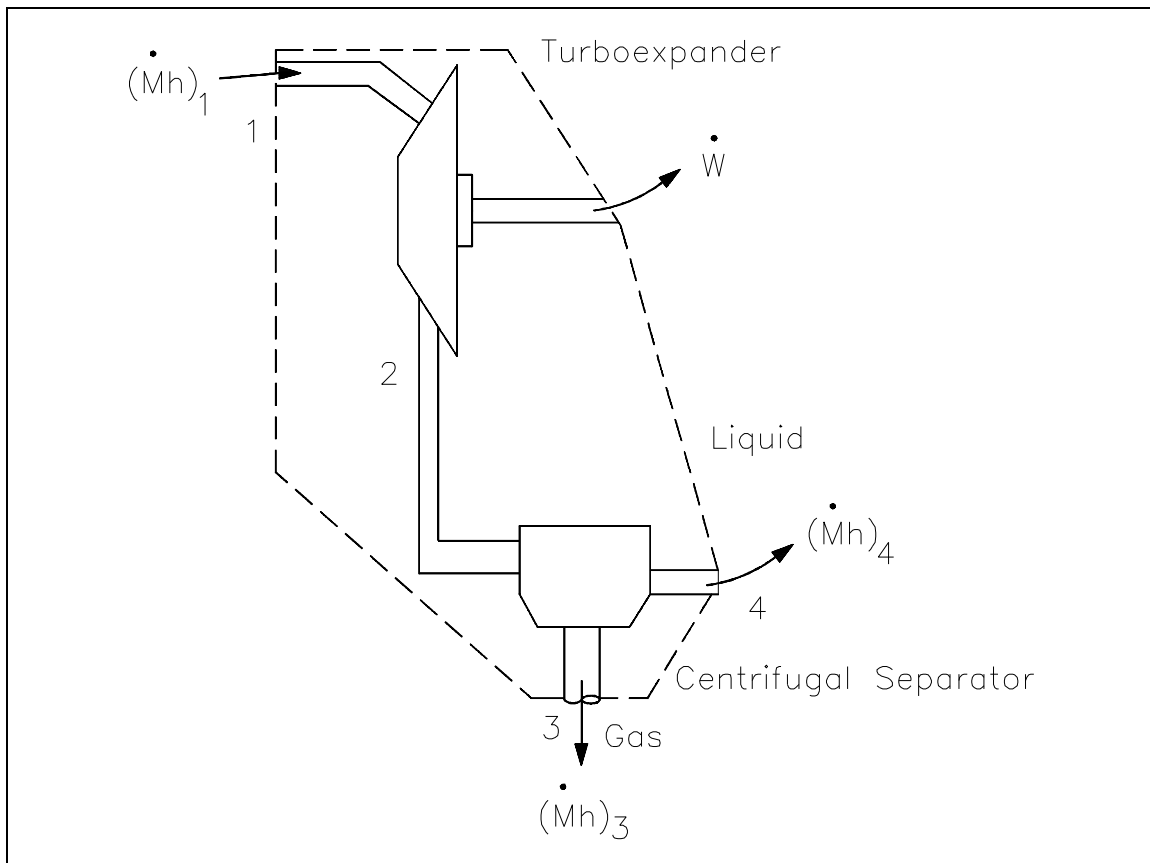


Figure 16 Open System Control Volumes

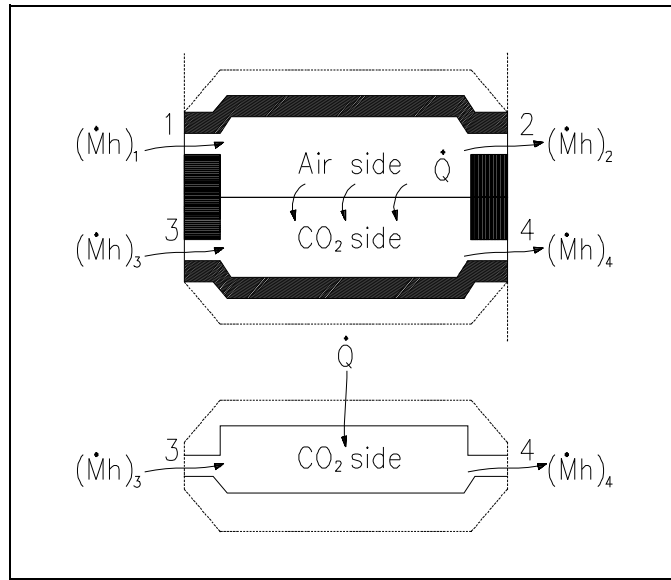


Figure 17 Open System Control Volumes (Cont.)

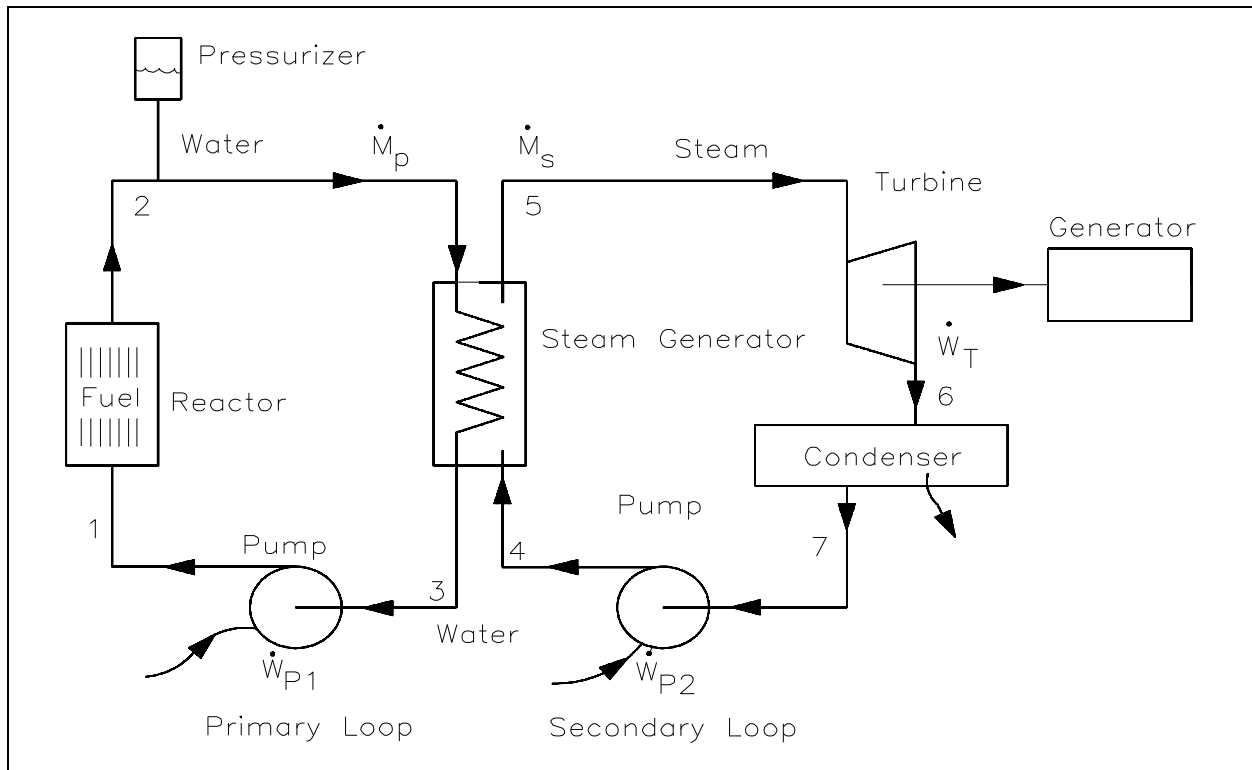


Figure 18 Multiple Control Volumes in Same System

The forms of energy that may cross the control volume boundary include those associated with the mass (m) crossing the boundary. Mass in motion has potential (PE), kinetic (KE), and internal energy (U). In addition, since the flow is normally supplied with some driving power (a pump for example), there is another form of energy associated with the fluid caused by its pressure. This form of energy is referred to as flow energy (Pv-work). The thermodynamic terms thus representing the various forms of energy crossing the control boundary with the mass are given as $m(u + Pv + ke + pe)$.

In open system analysis, the u and Pv terms occur so frequently that another property, enthalpy, has been defined as $h = u + Pv$. This results in the above expression being written as $m(h + ke + pe)$. In addition to the mass and its energies, externally applied work (W), usually designated as shaft work, is another form of energy that may cross the system boundary.

In order to complete and satisfy the conservation of energy relationship, energy that is caused by neither mass nor shaft work is classified as heat energy (Q). Then we can describe the relationship in equation form as follows.

$$\dot{m}(h_{in} + pe_{in} + ke_{in}) + \dot{Q} = \dot{m}(h_{out} + pe_{out} + ke_{out}) + \dot{W} \quad (1-22)$$

where:

- \dot{m} = mass flow rate of working fluid (lbm/hr)
- h_{in} = specific enthalpy of the working fluid entering the system (Btu/lbm)
- h_{out} = specific enthalpy of the working fluid leaving the system (Btu/lbm)
- pe_{in} = specific potential energy of working fluid entering the system (ft-lbf/lbm)
- pe_{out} = specific potential energy of working fluid leaving the system (ft-lbf/lbm)
- ke_{in} = specific kinetic energy of working fluid entering the system (ft-lbf/lbm)
- ke_{out} = specific kinetic energy of working fluid leaving the system (ft-lbf/lbm)
- \dot{W} = rate of work done by the system (ft-lbf/hr)
- \dot{Q} = heat rate into the system (Btu/hr)

Example 1 illustrates the use of the control volume concept while solving a first law problem involving most of the energy terms mentioned previously.

Example 1: Open System Control Volume

The enthalpies of steam entering and leaving a steam turbine are 1349 Btu/lbm and 1100 Btu/lbm, respectively. The estimated heat loss is 5 Btu/lbm of steam. The flow enters the turbine at 164 ft/sec at a point 6.5 ft above the discharge and leaves the turbine at 262 ft/sec. Determine the work of the turbine.

Solution:

$$\dot{m}_{in}(h_{in} + pe_{in} + ke_{in}) + \dot{Q} = \dot{m}_{out}(h_{out} + pe_{out} + ke_{out}) + \dot{W}$$

1) Divide by \dot{m} since, $\dot{m}_{in} = \dot{m}_{out} = \dot{m}$.

$$(h_{in} + pe_{in} + ke_{in}) + q = (h_{out} + pe_{out} + ke_{out}) + w$$

where:

q = heat added to the system per pound (Btu/lbm)

w = work done by the system per pound (ft-lbf/lbm)

2) Use Joule's constant $J = 778 \text{ ft-lbf/Btu}$ for conversions and substitute known values.

$$1349 \text{ Btu/lbm} + (6.5/778) \text{ Btu/lbm} + [(164)^2/2(32.17)(778)] \text{ Btu/lbm} + (-5 \text{ Btu/lbm}) = 1100 \text{ Btu/lbm} + 0 \text{ pe}_{out} + [(262)^2/2(32.17)(778)] \text{ Btu/lbm} + w$$

Note: The minus sign indicates heat out of the turbine.

3) Solve for work, w .

$$1349 \text{ Btu/lbm} + 8.3548 \times 10^{-3} \text{ Btu/lbm} + 0.5368 \text{ Btu/lbm} - 5 \text{ Btu/lbm} = 1100 \text{ Btu/lbm} + 1.37 \text{ Btu/lbm} + w$$

$$1344.54 \text{ Btu/lbm} = 1101.37 \text{ Btu/lbm} + w$$

$$w = 1344.54 \text{ Btu/lbm} - 1101.37 \text{ Btu/lbm}$$

$$w = 243.17 \text{ Btu/lbm}$$

This example demonstrates that potential and kinetic energy terms are insignificant for a turbine, since the Δp_e and Δk_e values are less than 1 Btu/lbm.

When the system (the fluid being studied) changes its properties (temperature, pressure, volume) from one value to another as a consequence of work or heat or internal energy exchange, then it is said that the fluid has gone through a "process." In some processes, the relationships between pressure, temperature, and volume are specified as the fluid goes from one thermodynamic state to another. The most common processes are those in which the temperature, pressure, or volume is held constant during the process. These would be classified as isothermal, isobaric, or isovolumetric processes, respectively. Iso means "constant or one." If the fluid passes through various processes and then eventually returns to the same state it began with, the system is said to have undergone a cyclic process. One such cyclic process used is the Rankine cycle, two examples of which are shown in Figure 19.

The processes that comprise the cycle are described below.

- ab: Liquid is compressed with no change in entropy (by ideal pump).
- bc: Constant pressure transfer of heat in the boiler. Heat is added to the compressed liquid, two-phase, and superheat states.
- cd: Constant entropy expansion with shaft work output (in ideal turbine).
- da: Constant pressure transfer of heat in the sink. Unavailable heat is rejected to the heat sink (condenser).

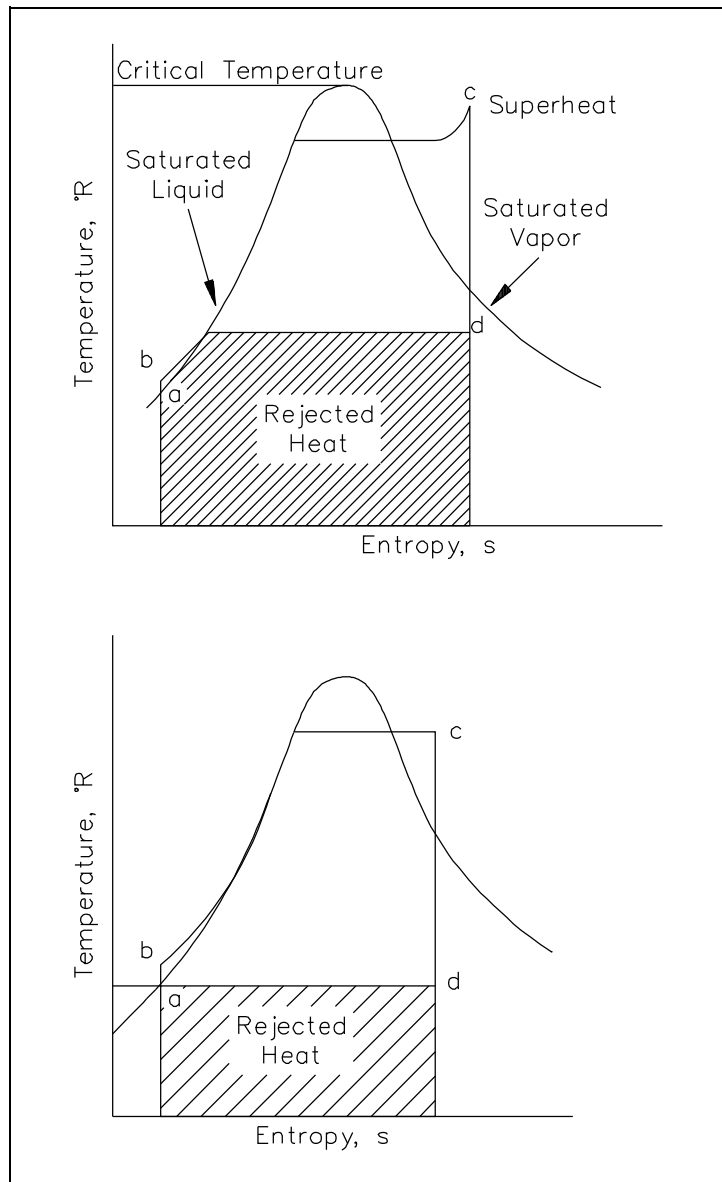


Figure 19 T-s Diagram with Rankine Cycles

Note the individual processes the fluid must go through before completing the complete cycle. Rankine cycles will be discussed in greater detail later in this module. Figure 20 shows a typical steam plant cycle. Heat is supplied to the steam generator (boiler) where liquid is converted to steam or vapor. The vapor is then expanded adiabatically in the turbine to produce a work output. Vapor leaving the turbine then enters the condenser where heat is removed and the vapor is condensed into the liquid state. The condensation process is the heat-rejection mechanism for the cycle. Saturated liquid is delivered to the condensate pump and then the feed pump where its pressure is raised to the saturation pressure corresponding to the steam generator temperature, and the high pressure liquid is delivered to the steam generator where the cycle repeats itself.

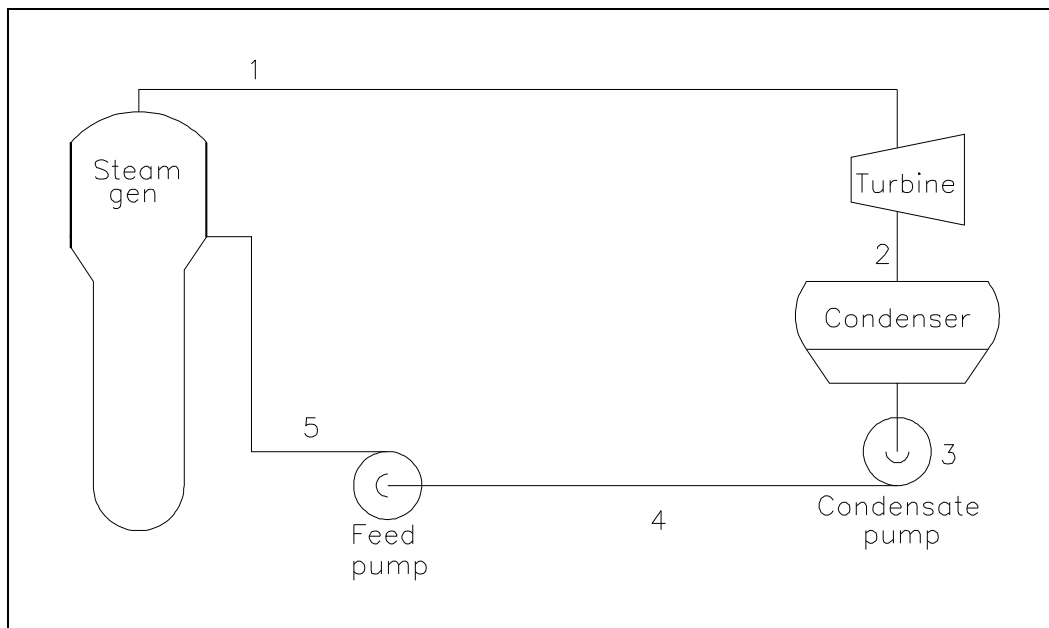


Figure 20 Typical Steam Plant Cycle

With the example complete, it seems appropriate to discuss the various components of a typical steam plant system. Although such a system is extremely complex, only the major components will be discussed. A typical steam plant system consists of: a heat source to produce the thermal energy (e.g. nuclear or fossil fuel); a steam generator to change the thermal energy into steam energy (a complete steam plant usually exists in connection with the steam generator in converting the steam into eventual electrical energy); pumps to transfer the fluid back to the heat source (reactor coolant pumps in a nuclear reactor); a pressurizer to ensure that the primary system maintains its desired pressure; and the necessary piping to ensure the fluid passes through each stage of its cyclic process. Of necessity, the steam plant is a large "closed" system. However, each component of the system is thermodynamically analyzed as an open system as the fluid passes through it. Of primary importance is the process of dissipating the energy created by the heat source. This process takes place in the steam generator, which acts as a giant two-phase heat generator.

The hot fluid from the heat source passes through the primary side of the steam generator where its energy is passed to the secondary side of the heat exchanger in such a manner as to create steam. The fluid, with its energy removed from the primary side, leaves the steam generator at a lower temperature, and is pumped back to the heat source to be "re-heated." Each major component of a steam plant can be treated as a separate open system problem. A thermodynamic analysis, using the various forms of energies discussed, can be applied to the particular component in studying its behavior. A simplified example of the thermodynamics involved in the steam generator is shown below.

Example 2: Open System - Steam Plant Component

Primary fluid enters the heat exchanger of a nuclear facility at 610°F and leaves at 540°F. The flow rate is approximately 1.38×10^8 lbm/hr. If the specific heat of the fluid is taken as 1.5 Btu/lbm°F, what is the heat transferred out of the steam generator?

Solution:

$$\dot{m}_{in}(h + pe + ke_{in}) + \dot{Q} = \dot{m}_{out}(h + pe + ke_{out}) + \dot{W}$$

- 1) Neglecting pe and ke and assuming no work is done on the system.

$$\dot{m}(h_{in}) + \dot{Q} = \dot{m}(h_{out})$$

$$\dot{Q} = \dot{m}(h_{out} - h_{in})$$

- 2) Substituting $\dot{Q} = \dot{m}c_p\Delta T$ where c_p = specific heat capacity (Btu/lbm-°F).

$$= \dot{m}(c_p)(T_{out} - T_{in})$$

$$= 1.38 \times 10^8 \text{ lbm/hr} (1.5 \text{ Btu/lbm-°F}) (540 - 610^\circ\text{F})$$

$$\dot{Q} = -1.45 \times 10^{10} \text{ Btu/hr}$$

The minus sign indicating heat out of the heat exchanger, which is consistent with the physical case. This example demonstrates that for a heat exchanger, the heat transfer rate can be calculated using the equation $\dot{Q} = \dot{m}(h_{out}-h_{in})$, or $\dot{Q} = \dot{m}c_p\Delta T$. It is important to note that the later equation can only be used when no phase change occurs since $\Delta T = 0$ during a phase change. The first equation can be used for a phase change heat transfer process as well as for latent heat calculations.

The pumps used for returning the fluid to the heat source can be analyzed as a thermodynamic system also. One such example is illustrated in Example 3.

Example 3: Open System - Coolant

A power pump is used to return the fluid from the heat exchanger back to the core. The flow rate through the pump is about 3.0×10^7 lbm/hr with the fluid entering the pump as saturated liquid at 540°F. The pressure rise across the pump is 90 psia. What is the work of the pump, neglecting heat losses and changes in potential and kinetic energy?

Solution:

$$\dot{m}(h_{in} + pe_{in} + ke_{in}) + \dot{Q} = \dot{m}(h_{out} + pe_{out} + ke_{out}) + \dot{W}$$

- 1) Assume $\dot{Q} = 0$ and neglect changes in pe and ke

$$\dot{m}(h_{in}) = \dot{m}(h_{out}) + \dot{W}$$

- 2) $\dot{W} = \dot{m} (h_{in} - h_{out})$ where \dot{W} is the rate of doing work by the pump

$$h_{in} = u_{in} + vP_{in}$$

$$h_{out} = u_{out} + vP_{out}$$

$$(h_{in} - h_{out}) = (u_{in} - u_{out}) + (vP_{in} - vP_{out}) = \Delta u + (vP_{in} - vP_{out})$$

- 3) Since no heat is transferred, $\Delta u = 0$ and the specific volume out of the pump is the same as the specific volume entering since water is incompressible.

$$(h_{in} - h_{out}) = v(P_{in} - P_{out})$$

- 4) Substituting the expression for work, $\dot{W} = \dot{m} (h_{in} - h_{out})$ we have:

$$\dot{W} = \dot{m} v(P_{in} - P_{out}).$$

- 5) Using 0.02146 for specific volume.

$$\dot{W} = 3.0 \times 10^7 \text{ lbm/hr} (0.02146 \text{ ft}^3/\text{lbm}) (-90 \text{ psia}) (144 \text{ in}^2/\text{ft}^2)/778 \text{ ft-lbf/Btu}$$

$$\dot{W} = -10.7 \times 10^6 \text{ Btu/hr or } -4,204 \text{ hp}$$

Note: The minus sign indicating work put into the fluid by the pump. 1 hp = 2545 Btu/hr.

A thermodynamic balance across the reactor core gives an indication of the amount of heat removed by the coolant that is given off by the fuel rods.

Example 4: Thermodynamic Balance across Heat Source

In a particular facility, the temperature leaving the reactor core is 612°F, while that entering the core is 542°F. The coolant flow through the heat source is 1.32×10^8 lbm/hr. The c_p of the fluid averages 1.47 Btu/lbm°F. How much heat is being removed from the heat source? The pe and ke energies are small compared to other terms and may be neglected.

Solution:

$$\dot{m}(h + pe + ke)_{in} + \dot{Q} = \dot{m}(h + pe + ke)_{out} + \dot{W}$$

$$\dot{Q} = \dot{m}(h_{out} - h_{in})$$

1) Substituting $\dot{Q} = \dot{m}c_p\Delta T$ where c_p = specific heat capacity.

$$\dot{Q} = \dot{m}(c_p) (T_{out} - T_{in})$$

$$\dot{Q} = 1.32 \times 10^8 \text{ lbm/hr} (1.47 \text{ Btu/lbm } ^\circ\text{F}) (612 - 542^\circ\text{F})$$

$$\dot{Q} = 1.36 \times 10^{10} \text{ Btu/hr}$$

For this example $\dot{Q} = \dot{m}c_p\Delta T$ has been used to calculate the heat transfer rate since no phase change has occurred. However, $\dot{Q} = \dot{m} (h_{out}-h_{in})$ could also have been used had the problem data included inlet and outlet enthalpies.

The individual principal components of a reactor system have been thermodynamically analyzed. If all components were combined into an overall system, the system could be analyzed as a "closed" system problem. Such an analysis is illustrated in the following example.

Example 5: Overall Thermodynamic Balance

A nuclear facility (primary side) is to be studied as a complete system. The heat produced by the heat source is 1.36×10^{10} Btu/hr. The heat removed by the heat exchanger (steam generator) is 1.361×10^{10} Btu/hr. What is the required pump power to maintain a stable temperature?

Solution:

\dot{W}_p = pump work, \dot{Q}_c = heat produced by the heat source, \dot{Q}_s = heat transferred into steam generator

$$\dot{m}(h + pe + ke) + \dot{W}_p + \dot{Q}_c = \dot{Q}_s + \dot{m}(h + pe + ke)$$

- 1) For a closed system, the mass entering and leaving the system is zero, therefore, \dot{m} is constant. The energy entering and leaving the system is zero, and you can assume that the ke and pe are constant so that:

$$\dot{Q}_c + \dot{W}_p = \dot{Q}_s$$

- 2)
$$\begin{aligned} \dot{W}_p &= \dot{Q}_s - \dot{Q}_c \\ &= 1.361 \times 10^{10} \text{ Btu/hr} - 1.36 \times 10^{10} \text{ Btu/hr} \\ &= 1.0 \times 10^7 \text{ Btu/hr} \end{aligned}$$

$$\dot{W}_p = 3,929 \text{ hp}$$

Of the examples just completed, emphasis should be placed on the heat exchanger analysis. Both the primary side and the secondary side have their own energy balances as the heat energy is transferred from one fluid to the other. In calculating heat exchanger heat transfer rates, we found that we could use the equations $\dot{Q} = \dot{m}_p \Delta T$.

Perhaps a short analysis of the secondary side of the heat exchanger will aid in understanding the heat exchanger's importance in the energy conversion process.

Example 6: Secondary Side of Heat Exchanger

Steam flows through a condenser at 2.0×10^6 kg/hr, entering as saturated vapor at 40°C ($h = 2574$ kJ/kg), and leaving at the same pressure as subcooled liquid at 30°C ($h = 125.8$ kJ/kg). Cooling water is available at 18°C ($h = 75.6$ kJ/kg). Environmental requirements limit the exit temperature to 25°C ($h = 104.9$ kJ/kg). Determine the required cooling water flow rate.

Solution:

Thermal balance gives the following:

$$\dot{Q}_{\text{stm}} = - \dot{Q}_{\text{cw}}$$

$$\dot{m}_{\text{stm}}(h_{\text{out}} - h_{\text{in}})_{\text{stm}} = - \dot{m}_{\text{cw}}(h_{\text{out}} - h_{\text{in}})_{\text{cw}}$$

$$\dot{m}_{\text{cw}} = - \dot{m}_{\text{stm}}(h_{\text{out}} - h_{\text{in}})_{\text{stm}} / (h_{\text{out}} - h_{\text{in}})_{\text{cw}}$$

$$= 2.0 \times 10^6 \text{ kg/hr} (125.8 - 2574 \text{ kJ/kg}) / (104.9 - 75.6 \text{ kJ/kg})$$

$$\dot{m}_{\text{cw}} = 1.67 \times 10^8 \text{ kg/hr}$$

In this example, we calculated the flow rate using the equation $\dot{Q} = \dot{m}\Delta h$ since a phase change occurred when the steam was condensed to liquid water. $\dot{Q} = \dot{m}c_p\Delta T$ would not have worked since $\Delta T=0$ for a phase change. Had we attempted to solve the problem using $\dot{Q} = \dot{m}c_p\Delta T$, we would have discovered that an error occurs since the $\Delta T = 10^\circ\text{C}$ is the ΔT needed to subcool the liquid from saturation at 40°C to a subcooled value of 30°C . Therefore, the heat transfer process to condense the steam to a saturated liquid has not been taken into account.

Summary

The important information from this chapter is summarized below.

First Law of Thermodynamics Summary

- The First Law of Thermodynamics states that energy can neither be created nor destroyed, only altered in form.
- In analyzing an open system using the First Law of Thermodynamics, the energy into the system is equal to the energy leaving the system.
- If the fluid passes through various processes and then eventually returns to the same state it began with, the system is said to have undergone a cyclic process. The first law is used to analyze a cyclic process.
- The energy entering any component is equal to the energy leaving that component at steady state.
- The amount of energy transferred across a heat exchanger is dependent upon the temperature of the fluid entering the heat exchanger from both sides and the flow rates of these fluids.
- A T-s diagram can be used to represent thermodynamic processes.

SECOND LAW OF THERMODYNAMICS

The Second Law of Thermodynamics is used to determine the maximum efficiency of any process. A comparison can then be made between the maximum possible efficiency and the actual efficiency obtained.

- EO 1.25** **STATE** the Second Law of Thermodynamics.
- EO 1.26** **Using** the Second Law of Thermodynamics, **DETERMINE** the maximum possible efficiency of a system.
- EO 1.27** **Given** a thermodynamic system, **CONDUCT** an analysis using the Second Law of Thermodynamics.
- EO 1.28** **Given** a thermodynamic system, **DESCRIBE** the method used to determine:
- a. **The maximum efficiency of the system**
 - b. **The efficiency of the components within the system**
- EO 1.29** **DIFFERENTIATE** between the path for an ideal process and that for a real process on a T-s or h-s diagram.
- EO 1.30** **Given** a T-s or h-s diagram for a system **EVALUATE**:
- a. **System efficiencies**
 - b. **Component efficiencies**
- EO 1.31** **DESCRIBE** how individual factors affect system or component efficiency.
-

Second Law of Thermodynamics

One of the earliest statements of the Second Law of Thermodynamics was made by R. Clausius in 1850. He stated the following.

It is impossible to construct a device that operates in a cycle and produces no effect other than the removal of heat from a body at one temperature and the absorption of an equal quantity of heat by a body at a higher temperature.

With the Second Law of Thermodynamics, the limitations imposed on any process can be studied to determine the maximum possible efficiencies of such a process and then a comparison can be made between the maximum possible efficiency and the actual efficiency achieved. One of the areas of application of the second law is the study of energy-conversion systems. For example, it is not possible to convert all the energy obtained from a nuclear reactor into electrical energy. There must be losses in the conversion process. The second law can be used to derive an expression for the maximum possible energy conversion efficiency taking those losses into account. Therefore, the second law denies the possibility of completely converting into work all of the heat supplied to a system operating in a cycle, no matter how perfectly designed the system may be. The concept of the second law is best stated using Max Planck's description:

It is impossible to construct an engine that will work in a complete cycle and produce no other effect except the raising of a weight and the cooling of a heat reservoir.

The Second Law of Thermodynamics is needed because the First Law of Thermodynamics does not define the energy conversion process completely. The first law is used to relate and to evaluate the various energies involved in a process. However, no information about the direction of the process can be obtained by the application of the first law. Early in the development of the science of thermodynamics, investigators noted that while work could be converted completely into heat, the converse was never true for a cyclic process. Certain natural processes were also observed always to proceed in a certain direction (e.g., heat transfer occurs from a hot to a cold body). The second law was developed as an explanation of these natural phenomena.

Entropy

One consequence of the second law is the development of the physical property of matter termed entropy (S). Entropy was introduced to help explain the Second Law of Thermodynamics. The change in this property is used to determine the direction in which a given process will proceed. Entropy can also be explained as a measure of the unavailability of heat to perform work in a cycle. This relates to the second law since the second law predicts that not all heat provided to a cycle can be transformed into an equal amount of work, some heat rejection must take place. The change in entropy is defined as the ratio of heat transferred during a reversible process to the absolute temperature of the system.

$$\Delta S = \frac{\Delta Q}{T_{\text{abs}}} \quad (\text{For a reversible process})$$

where

ΔS = the change in entropy of a system during some process (Btu/°R)

ΔQ = the amount of heat added to the system during the process (Btu)

T_{abs} = the absolute temperature at which the heat was transferred (°R)

The second law can also be expressed as $\Delta S \geq 0$ for a closed cycle. In other words, entropy must increase or stay the same for a cyclic system; it can never decrease.

Entropy is a property of a system. It is an extensive property that, like the total internal energy or total enthalpy, may be calculated from specific entropies based on a unit mass quantity of the system, so that $S = ms$. For pure substances, values of the specific entropy may be tabulated along with specific enthalpy, specific volume, and other thermodynamic properties of interest. One place to find this tabulated information is in the steam tables described in a previous chapter (refer back to Figure 19).

Specific entropy, because it is a property, is advantageously used as one of the coordinates when representing a reversible process graphically. The area under a reversible process curve on the T-s diagram represents the quantity of heat transferred during the process.

Thermodynamic problems, processes, and cycles are often investigated by substitution of reversible processes for the actual irreversible process to aid the student in a second law analysis. This substitution is especially helpful because only reversible processes can be depicted on the diagrams (h-s and T-s, for example) used for the analysis. Actual or irreversible processes cannot be drawn since they are not a succession of equilibrium conditions. Only the initial and final conditions of irreversible processes are known; however, some thermodynamics texts represent an irreversible process by dotted lines on the diagrams.

Carnot's Principle

With the practice of using reversible processes, Sadi Carnot in 1824 advanced the study of the second law by disclosing a principle consisting of the following propositions.

1. No engine can be more efficient than a reversible engine operating between the same high temperature and low temperature reservoirs. Here the term heat reservoir is taken to mean either a heat source or a heat sink.
2. The efficiencies of all reversible engines operating between the same constant temperature reservoirs are the same.
3. The efficiency of a reversible engine depends only upon the temperatures of the heat source and heat receiver.

Carnot Cycle

The above principle is best demonstrated with a simple cycle (shown in Figure 21) and an example of a proposed heat power cycle. The cycle consists of the following reversible processes.

- 1-2: adiabatic compression from T_C to T_H due to work performed on fluid.
- 2-3: isothermal expansion as fluid expands when heat is added to the fluid at temperature T_H .
- 3-4: adiabatic expansion as the fluid performs work during the expansion process and temperature drops from T_H to T_C .
- 4-1: isothermal compression as the fluid contracts when heat is removed from the fluid at temperature T_C .

This cycle is known as a Carnot Cycle. The heat input (Q_H) in a Carnot Cycle is graphically represented on Figure 21 as the area under line 2-3. The heat rejected (Q_C) is graphically represented as the area under line 1-4. The difference between the heat added and the heat rejected is the net work (sum of all work processes), which is represented as the area of rectangle 1-2-3-4.

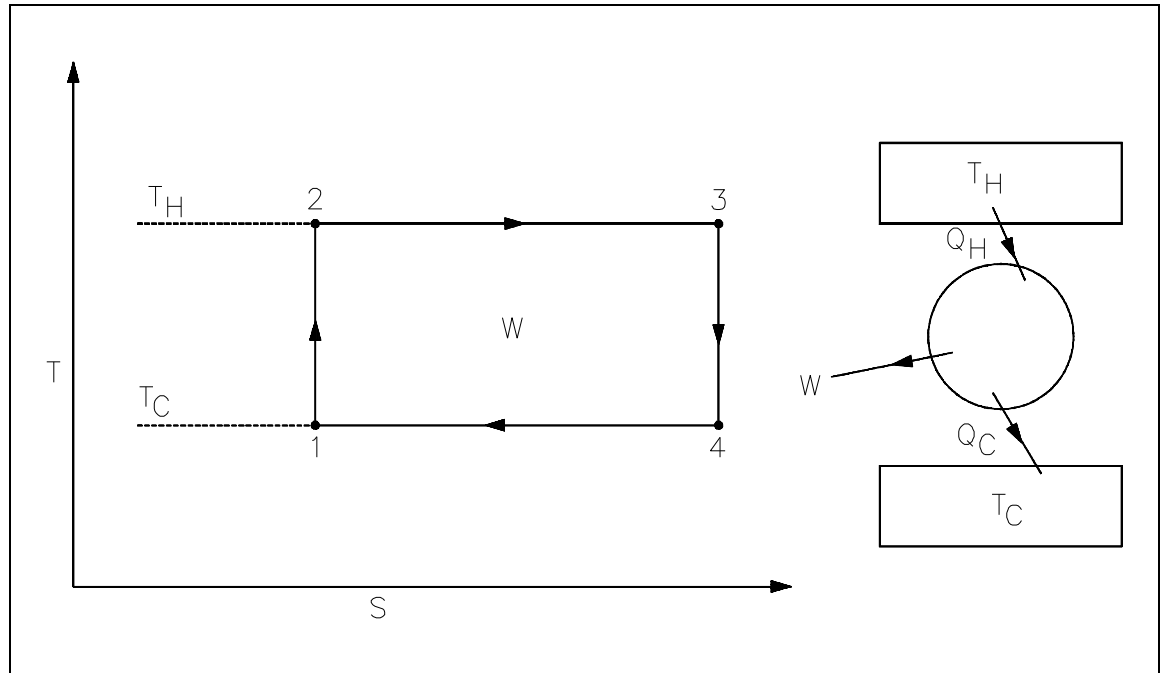


Figure 21 Carnot Cycle Representation

The efficiency (η) of the cycle is the ratio of the net work of the cycle to the heat input to the cycle. This ratio can be expressed by the following equation.

$$\begin{aligned}\eta &= (Q_H - Q_C)/Q_H = (T_H - T_C)/T_H \\ &= 1 - (T_C/T_H)\end{aligned}\quad (1-23)$$

where:

- η = cycle efficiency
- T_C = designates the low-temperature reservoir ($^{\circ}\text{R}$)
- T_H = designates the high-temperature reservoir ($^{\circ}\text{R}$)

Equation 1-23 shows that the maximum possible efficiency exists when T_H is at its largest possible value or when T_C is at its smallest value. Since all practical systems and processes are really irreversible, the above efficiency represents an upper limit of efficiency for any given system operating between the same two temperatures. The system's maximum possible efficiency would be that of a Carnot efficiency, but because Carnot efficiencies represent reversible processes, the actual system will not reach this efficiency value. Thus, the Carnot efficiency serves as an unattainable upper limit for any real system's efficiency. The following example demonstrates the above principles.

Example 1: Carnot Efficiency

An inventor claims to have an engine that receives 100 Btu of heat and produces 25 Btu of useful work when operating between a source at 140°F and a receiver at 0°F. Is the claim a valid claim?

Solution:

$$T_H = 140^\circ\text{F} + 460 = 600^\circ\text{R}$$

$$T_C = 0^\circ\text{F} + 460 = 460^\circ\text{R}$$

$$\eta = (600-460)/600 \times 100 = 23.3\%$$

$$\text{Claimed efficiency} = 25/100 = 25\%$$

Therefore, the claim is invalid.

The most important aspect of the second law for our practical purposes is the determination of maximum possible efficiencies obtained from a power system. Actual efficiencies will always be less than this maximum. The losses (friction, for example) in the system and the fact that systems are not truly reversible preclude us from obtaining the maximum possible efficiency. An illustration of the difference that may exist between the ideal and actual efficiency is presented in Figure 22 and the following example.

Example 2: Actual vs. Ideal Efficiency

The actual efficiency of a steam cycle is 18.0%. The facility operates from a steam source at 340°F and rejects heat to atmosphere at 60°F. Compare the Carnot efficiency to the actual efficiency.

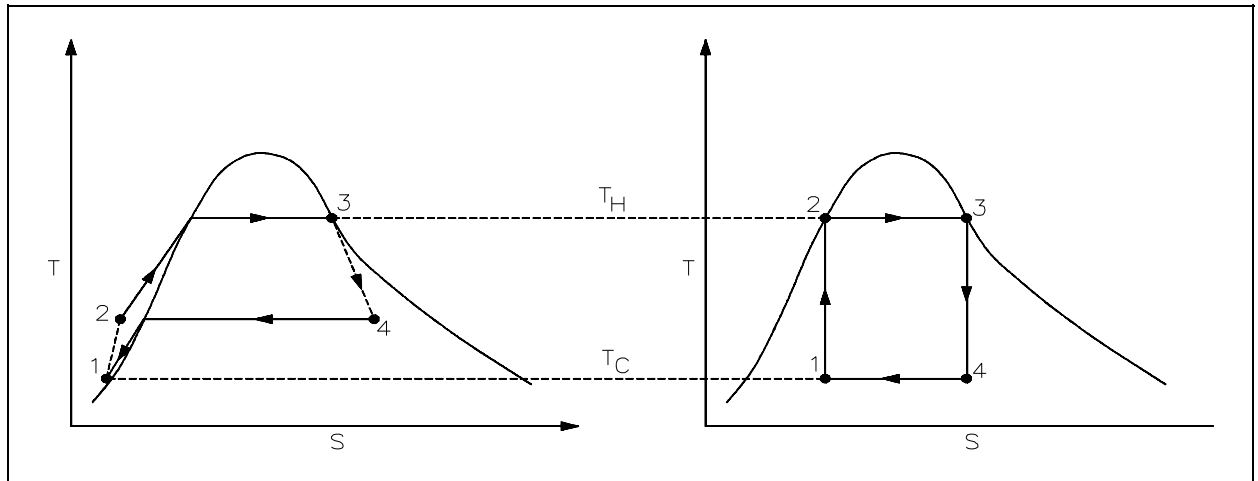


Figure 22 Real Process Cycle Compared to Carnot Cycle

Solution:

$$\begin{aligned}
 \eta &= 1 - (T_c / T_h) \\
 \eta &= 1 - (60 + 460)/(340 + 460) \\
 &= 1 - 520/800 \\
 &= 35\% \quad \text{as compared to 18.0\% actual efficiency.}
 \end{aligned}$$

An open system analysis was performed using the First Law of Thermodynamics in the previous chapter. The second law problems are treated in much the same manner; that is, an isolated, closed, or open system is used in the analysis depending upon the types of energy that cross the boundary. As with the first law, the open system analysis using the second law equations is the more general case, with the closed and isolated systems being "special" cases of the open system. The solution to second law problems is very similar to the approach used in the first law analysis.

Figure 23 illustrates the control volume from the viewpoint of the second law. In this diagram, the fluid moves through the control volume from section in to section out while work is delivered external to the control volume. We assume that the boundary of the control volume is at some environmental temperature and that all of the heat transfer (Q) occurs at this boundary. We have already noted that entropy is a property, so it may be transported with the flow of the fluid into and out of the control volume, just like enthalpy or internal energy. The entropy flow into the control volume resulting from mass transport is, therefore, $\dot{m}_{in}s_{in}$, and the entropy flow out of the control volume is $\dot{m}_{out}s_{out}$, assuming that the properties are uniform at

sections in and out. Entropy may also be added to the control volume because of heat transfer at the boundary of the control volume.

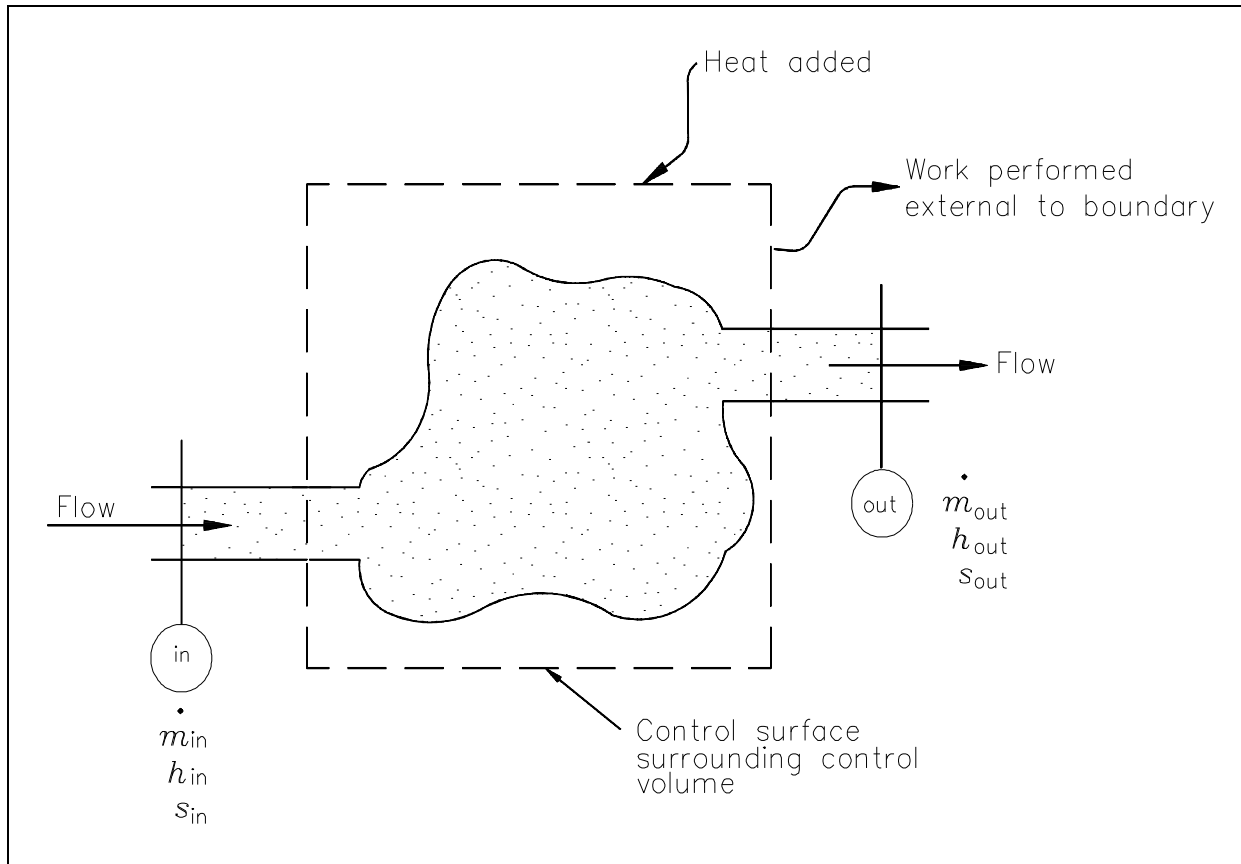


Figure 23 Control Volume for Second Law Analysis

A simple demonstration of the use of this form of system in second law analysis will give the student a better understanding of its use.

Example 3: Open System Second Law

Steam enters the nozzle of a steam turbine with a velocity of 10 ft/sec at a pressure of 100 psia and temperature of 500°F at the nozzle discharge. The pressure and temperature are 1 atm at 300°F. What is the increase in entropy for the system if the mass flow rate is 10,000 lbm/hr?

Solution:

$$\dot{m}s_{in} + \dot{p} = \dot{m}s_{out} \quad \text{where } \dot{p} = \text{entropy added to the system}$$

$$\dot{p} = \dot{m} (s_{out} - s_{in})$$

$$s_{in} = 1.7088 \text{ Btu/lbm } ^\circ\text{R} \quad (\text{from steam tables})$$

$$s_{out} = 1.8158 \text{ Btu/lbm}^\circ\text{R} \quad (\text{from steam tables})$$

$$\dot{p}/\dot{m} = s_{out} - s_{in} = 1.8158 - 1.7088 \text{ Btu/lbm}^\circ\text{R}$$

$$\dot{p}/\dot{m} = 0.107 \text{ Btu/lbm } ^\circ\text{R}$$

$$\dot{p} = 10,000 (0.107)$$

$$\dot{p} = 1070 \text{ Btu/hr } ^\circ\text{R.} = \text{entropy added to the system}$$

It should always be kept in mind that the Second Law of Thermodynamics gives an upper limit (which is never reached in physical systems) to how efficiently a thermodynamic system can perform. A determination of that efficiency is as simple as knowing the inlet and exit temperatures of the overall system (one that works in a cycle) and applying Carnot's efficiency equation using these temperatures in absolute degrees.

Diagrams of Ideal and Real Processes

Any ideal thermodynamic process can be drawn as a path on a property diagram, such as a T-s or an h-s diagram. A real process that approximates the ideal process can also be represented on the same diagrams (usually with the use of dashed lines).

In an ideal process involving either a reversible expansion or a reversible compression, the entropy will be constant. These isentropic processes will be represented by vertical lines on either T-s or h-s diagrams, since entropy is on the horizontal axis and its value does not change. A real expansion or compression process operating between the same pressures as the ideal process will look much the same, but the dashed lines representing the real process will slant slightly towards the right since the entropy will increase from the start to the end of the process. Figures 24 and 25 show ideal and real expansion and compression processes on T-s and h-s diagrams.

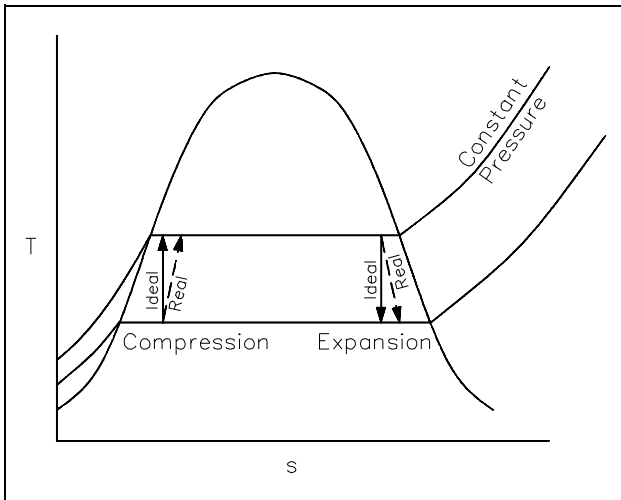


Figure 24 Expansion and Compression Processes on T-s Diagram

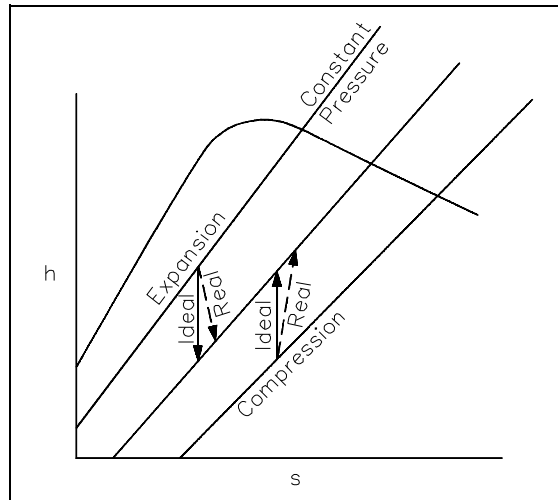


Figure 25 Expansion and Compression Processes on h-s Diagram

Power Plant Components

In order to analyze a complete power plant steam power cycle, it is first necessary to analyze the elements which make up such cycles. (See Figure 26) Although specific designs differ, there are three basic types of elements in power cycles, (1) turbines, (2) pumps and (3) heat exchangers. Associated with each of these three types of elements is a characteristic change in the properties of the working fluid.

Previously we have calculated system efficiency by knowing the temperature of the heat source and the heat sink. It is also possible to calculate the efficiencies of each individual component.

The efficiency of each type of component can be calculated by comparing the actual work produced by the component to the work that would have been produced by an ideal component operating isentropically between the same inlet and outlet conditions.

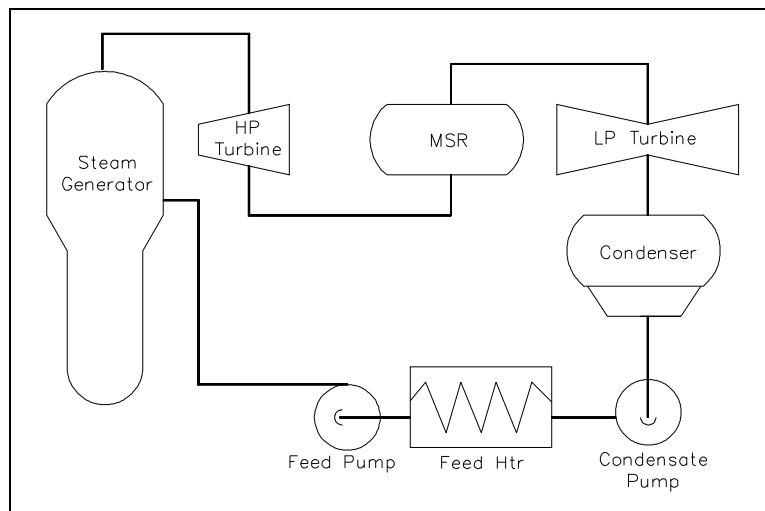


Figure 26 Steam Cycle

A steam turbine is designed to extract energy from the working fluid (steam) and use it to do work in the form of rotating the turbine shaft. The working fluid does work as it expands through the turbine. The shaft work is then converted to electrical energy by the generator. In the application of the first law, general energy equation to a simple turbine under steady flow conditions, it is found that the decrease in the enthalpy of the working fluid $H_{in} - H_{out}$ equals the work done by the working fluid in the turbine (W_t).

$$H_{in} - H_{out} = W_t \quad (1-24)$$

$$\dot{m}(h_{in} - h_{out}) = \dot{w}_t \quad (1-25)$$

where:

- H_{in} = enthalpy of the working fluid entering the turbine (Btu)
- H_{out} = enthalpy of the working fluid leaving the turbine (Btu)
- W_t = work done by the turbine (ft-lb_f)
- \dot{m} = mass flow rate of the working fluid (lb_m/hr)
- h_{in} = specific enthalpy of the working fluid entering the turbine (Btu/lbm)
- h_{out} = specific enthalpy of the working fluid leaving the turbine (Btu/lbm)
- \dot{w}_t = power of turbine (Btu/hr)

These relationships apply when the kinetic and potential energy changes and the heat losses of the working fluid while in the turbine are negligible. For most practical applications, these are valid assumptions. However, to apply these relationships, one additional definition is necessary. The steady flow performance of a turbine is idealized by assuming that in an ideal case the working fluid does work reversibly by expanding at a constant entropy. This defines the so-called ideal turbine. In an ideal turbine, the entropy of the working fluid entering the turbine S_{in} equals the entropy of the working fluid leaving the turbine.

$$S_{in} = S_{out}$$

$$s_{in} = s_{out}$$

where:

- S_{in} = entropy of the working fluid entering the turbine (Btu/°R)
- S_{out} = entropy of the working fluid leaving the turbine (Btu/°R)
- s_{in} = specific entropy of the working fluid entering the turbine (Btu/lbm -°R)
- s_{out} = specific entropy of the working fluid leaving the turbine (Btu/lbm -°R)

The reason for defining an ideal turbine is to provide a basis for analyzing the performance of turbines. An ideal turbine performs the maximum amount of work theoretically possible.

An actual turbine does less work because of friction losses in the blades, leakage past the blades and, to a lesser extent, mechanical friction. Turbine efficiency η_t , sometimes called isentropic turbine efficiency because an ideal turbine is defined as one which operates at constant entropy, is defined as the ratio of the actual work done by the turbine $W_{t, \text{actual}}$ to the work that would be done by the turbine if it were an ideal turbine $W_{t, \text{ideal}}$.

$$\eta_t = \frac{W_{t, \text{actual}}}{W_{t, \text{ideal}}} \quad (1-26)$$

$$\eta = \frac{(h_{\text{in}} - h_{\text{out}})_{\text{actual}}}{(h_{\text{in}} - h_{\text{out}})_{\text{ideal}}} \quad (1-27)$$

where:

- η_t = turbine efficiency (no units)
- $W_{t, \text{actual}}$ = actual work done by the turbine (ft-lbf)
- $W_{t, \text{ideal}}$ = work done by an ideal turbine (ft-lbf)
- $(h_{\text{in}} - h_{\text{out}})_{\text{actual}}$ = actual enthalpy change of the working fluid (Btu/lbm)
- $(h_{\text{in}} - h_{\text{out}})_{\text{ideal}}$ = actual enthalpy change of the working fluid in an ideal turbine (Btu/lbm)

In many cases, the turbine efficiency η_t has been determined independently. This permits the actual work done to be calculated directly by multiplying the turbine efficiency η_t by the work done by an ideal turbine under the same conditions. For small turbines, the turbine efficiency is generally 60% to 80%; for large turbines, it is generally about 90%.

The actual and idealized performances of a turbine may be compared conveniently using a T-s diagram. Figure 27 shows such a comparison. The ideal case is a constant entropy. It is represented by a vertical line on the T-s diagram. The actual turbine involves an increase in entropy. The smaller the increase in entropy, the closer the turbine efficiency η_t is to 1.0 or 100%.

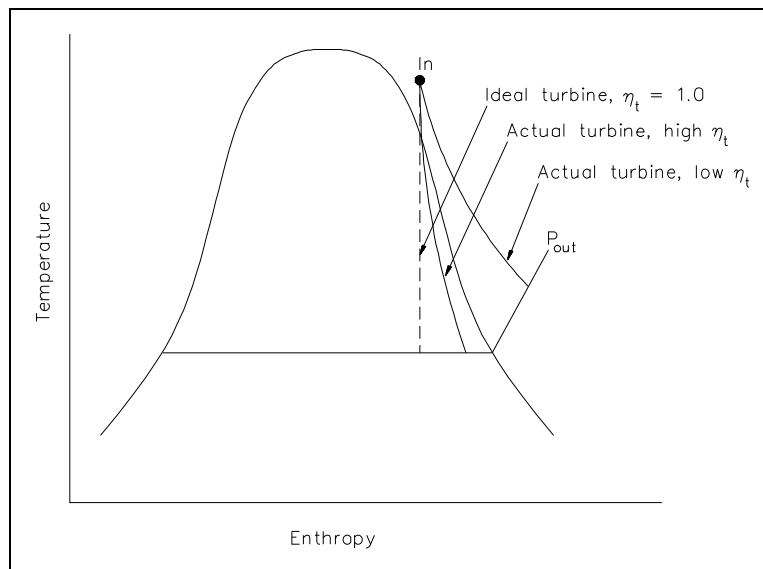


Figure 27 Comparison of Ideal and Actual Turbine Performances

A pump is designed to move the working fluid by doing work on it. In the application of the first law general energy equation to a simple pump under steady flow conditions, it is found that the increase in the enthalpy of the working fluid $H_{out} - H_{in}$ equals the work done by the pump, W_p , on the working fluid.

$$H_{out} - H_{in} = W_p \quad (1-28)$$

$$\dot{m}(h_{out} - h_{in}) = \dot{w}_p \quad (1-29)$$

where:

- H_{out} = enthalpy of the working fluid leaving the pump (Btu)
- H_{in} = enthalpy of the working fluid entering the pump (Btu)
- W_p = work done by the pump on the working fluid (ft-lbf)
- \dot{m} = mass flow rate of the working fluid (lbm/hr)
- h_{out} = specific enthalpy of the working fluid leaving the pump (Btu/lbm)
- h_{in} = specific enthalpy of the working fluid entering the pump (Btu/lbm)
- \dot{w}_p = power of pump (Btu/hr)

These relationships apply when the kinetic and potential energy changes and the heat losses of the working fluid while in the pump are negligible. For most practical applications, these are valid assumptions. It is also assumed that the working fluid is incompressible. For the ideal case, it can be shown that the work done by the pump W_p is equal to the change in enthalpy across the ideal pump.

$$W_{p \text{ ideal}} = (H_{out} - H_{in})_{ideal} \quad (1-30)$$

$$\dot{w}_{p \text{ ideal}} = \dot{m} (h_{out} - h_{in})_{ideal} \quad (1-31)$$

where:

- W_p = work done by the pump on the working fluid (ft-lbf)
- H_{out} = enthalpy of the working fluid leaving the pump (Btu)
- H_{in} = enthalpy of the working fluid entering the pump (Btu)
- \dot{w}_p = power of pump (Btu/hr)
- \dot{m} = mass flow rate of the working fluid (lbm/hr)
- h_{out} = specific enthalpy of the working fluid leaving the pump (Btu/lbm)
- h_{in} = specific enthalpy of the working fluid entering the pump (Btu/lbm)

The reason for defining an ideal pump is to provide a basis for analyzing the performance of actual pumps. A pump requires more work because of unavoidable losses due to friction and fluid turbulence. The work done by a pump W_p is equal to the change in enthalpy across the actual pump.

$$W_{p, \text{ actual}} = (H_{\text{out}} - H_{\text{in}})_{\text{actual}} \quad (1-32)$$

$$\dot{w}_{p, \text{ actual}} = \dot{m} (h_{\text{out}} - h_{\text{in}})_{\text{actual}} \quad (1-33)$$

Pump efficiency, η_p , is defined as the ratio of the work required by the pump if it were an ideal pump $w_{p, \text{ ideal}}$ to the actual work required by the pump $w_{p, \text{ actual}}$.

$$\eta_p = \frac{W_{p, \text{ ideal}}}{W_{p, \text{ actual}}} \quad (1-34)$$

Example:

A pump operating at 75% efficiency has an inlet specific enthalpy of 200 Btu/lbm. The exit specific enthalpy of the ideal pump is 600 Btu/lbm. What is the exit specific enthalpy of the actual pump?

Solution:

Using Equation 1-34:

$$\eta_p = \frac{W_{p, \text{ ideal}}}{W_{p, \text{ actual}}}$$

$$W_{p, \text{ actual}} = \frac{W_{p, \text{ ideal}}}{\eta_p}$$

$$(h_{\text{out}} - h_{\text{in}})_{\text{actual}} = \frac{(h_{\text{out}} - h_{\text{in}})_{\text{ideal}}}{\eta_p}$$

$$h_{\text{out, actual}} = \frac{(h_{\text{out}} - h_{\text{in}})_{\text{ideal}}}{\eta_p} + h_{\text{in, actual}}$$

$$h_{\text{out, actual}} = \frac{(600 \text{ Btu/lbm} - 200 \text{ Btu/lbm})}{.75} + 200 \text{ Btu/lbm}$$

$$h_{\text{out, actual}} = 533.3 \text{ Btu/lbm} + 200 \text{ Btu/lbm}$$

$$h_{\text{out, actual}} = 733.3 \text{ Btu/lbm}$$

Pump efficiency, η_p , relates the work required by an ideal pump to the actual work required by the pump; it relates the minimum amount of work theoretically possible to the actual work required by the pump. However, the work required by a pump is normally only an intermediate form of energy. Normally a motor or turbine is used to run the pump. Pump efficiency does not account for losses in this motor or turbine. An additional efficiency factor, motor efficiency η_m , is defined as the ratio of the actual work required by the pump to the electrical energy input to the pump motor, when both are expressed in the same units.

$$\eta_m = \frac{W_{p, \text{ actual}}}{W_{m, \text{ in}} C}$$

where:

η_m	=	motor efficiency (no units)
$W_{p, \text{ actual}}$	=	actual work required by the pump (ft-lbf)
$W_{m, \text{ in}}$	=	electrical energy input to the pump motor (kw-hr)
C	=	conversion factor = 2.655×10^6 ft-lbf/kw-hr

Like pump efficiency η_p , motor efficiency η_m is always less than 1.0 or 100% for an actual pump motor. The combination of pump efficiency η_p and motor efficiency η_m relates the ideal pump to the electrical energy input to the pump motor.

$$\eta_m \eta_p = \frac{W_{p, \text{ ideal}}}{W_{m, \text{ in}} C} \quad (1-35)$$

where:

η_m	=	motor efficiency (no units)
η_p	=	pump efficiency (no units)
$W_{p, \text{ ideal}}$	=	ideal work required by the pump (ft-lbf)
$W_{m, \text{ in}}$	=	electrical energy input to the pump motor (kw-hr)
C	=	conversion factor = 2.655×10^6 ft-lbf/kw-hr

A heat exchanger is designed to transfer heat between two working fluids. There are several heat exchangers used in power plant steam cycles. In the steam generator or boiler, the heat source (e.g., reactor coolant) is used to heat and vaporize the feedwater. In the condenser, the steam exhausting from the turbine is condensed before being returned to the steam generator. In addition to these two major heat exchangers, numerous smaller heat exchangers are used throughout the steam cycle. Two primary factors determine the rate of heat transfer and the temperature difference between the two fluids passing through the heat exchanger.

In the application of the first law general energy equation to a simple heat exchanger under steady flow conditions, it is found that the mass flow rates and enthalpies of the two fluids are related by the following relationship.

$$\dot{m}_1 (h_{\text{out},1} - h_{\text{in},1}) = -\dot{m}_2 (h_{\text{out},2} - h_{\text{in},2}) \quad (1-36)$$

where:

\dot{m}_1 = mass flow rate of the working fluid 1 (lbm/hr)

\dot{m}_2 = mass flow rate of the working fluid 2 (lbm/hr)

$h_{\text{out},1}$ = specific enthalpy of the working fluid 1 leaving the heat exchanger (Btu/lbm)

$h_{\text{in},1}$ = specific enthalpy of the working fluid 1 entering the heat exchanger (Btu/lbm)

$h_{\text{out},2}$ = specific enthalpy of the working fluid 2 leaving the heat exchanger (Btu/lbm)

$h_{\text{in},2}$ = specific enthalpy of the working fluid 2 entering the heat exchanger (Btu/lbm)

In the preceding sections we have discussed the Carnot cycle, cycle efficiencies, and component efficiencies. In this section we will apply this information to allow us to compare and evaluate various ideal and real cycles. This will allow us to determine how modifying a cycle will affect the cycle's available energy that can be extracted for work.

Since the efficiency of a Carnot cycle is solely dependent on the temperature of the heat source and the temperature of the heat sink, it follows that to improve a cycles' efficiency all we have to do is increase the temperature of the heat source and decrease the temperature of the heat sink. In the real world the ability to do this is limited by the following constraints.

1. For a real cycle the heat sink is limited by the fact that the "earth" is our final heat sink. And therefore, is fixed at about 60°F (520°R).
2. The heat source is limited to the combustion temperatures of the fuel to be burned or the maximum limits placed on nuclear fuels by their structural components (pellets, cladding etc.). In the case of fossil fuel cycles the upper limit is ~3040°F (3500°R). But even this temperature is not attainable due to the metallurgical restraints of the boilers, and therefore they are limited to about 1500°F (1960°R) for a maximum heat source temperature.

Using these limits to calculate the maximum efficiency attainable by an ideal Carnot cycle gives the following.

$$\eta = \frac{T_{\text{SOURCE}} - T_{\text{SINK}}}{T_{\text{SOURCE}}} = \frac{1960^{\circ}\text{R} - 520^{\circ}\text{R}}{1960^{\circ}\text{R}} = 73.5\%$$

This calculation indicates that the Carnot cycle, operating with ideal components under real world constraints, should convert almost 3/4 of the input heat into work. But, as will be shown, this ideal efficiency is well beyond the present capabilities of any real systems.

Heat Rejection

To understand why an efficiency of 73% is not possible we must analyze the Carnot cycle, then compare the cycle using real and ideal components. We will do this by looking at the T-s diagrams of Carnot cycles using both real and ideal components.

The energy added to a working fluid during the Carnot isothermal expansion is given by q_s . Not all of this energy is available for use by the heat engine since a portion of it (q_r) must be rejected to the environment. This is given by:

$$q_r = T_o \Delta s \text{ in units of Btu/lbm,} \quad (1-37)$$

where T_o is the average heat sink temperature of 520°R . The available energy (A.E.) for the Carnot cycle may be given as:

$$\text{A.E.} = q_s - q_r \quad (1-38)$$

Substituting equation 1-37 for q_r gives:

$$\text{A.E.} = q_s - T_o \Delta s \text{ in units of Btu/lbm.} \quad (1-39)$$

and is equal to the area of the shaded region labeled available energy in Figure 28 between the temperatures 1962° and 520°R . From Figure 28 it can be seen that any cycle operating at a temperature of less than 1962°R will be less efficient. Note that by developing materials capable of withstanding the stresses above 1962°R , we could greatly add to the energy available for use by the plant cycle.

From equation 1-37, one can see why the change in entropy can be defined as a measure of the energy unavailable to do work. If the temperature of the heat sink is known, then the change in entropy does correspond to a measure of the heat rejected by the engine.

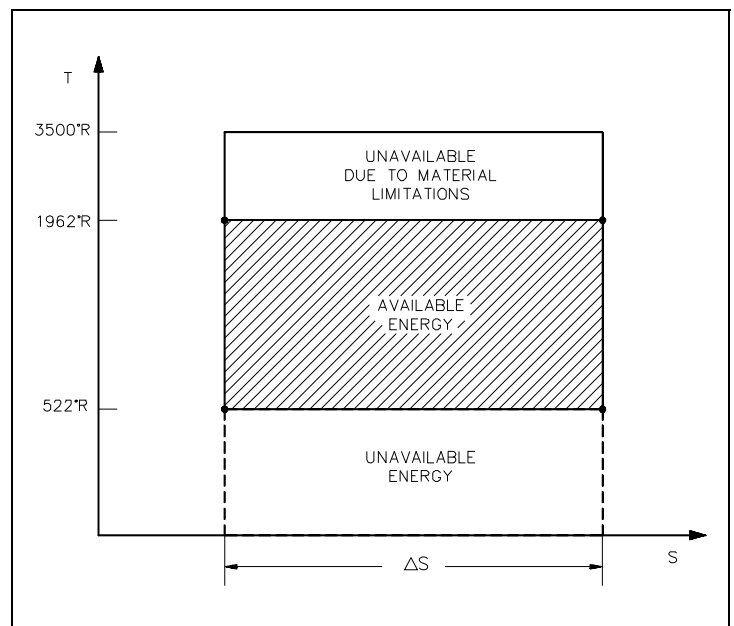


Figure 28 Carnot Cycle

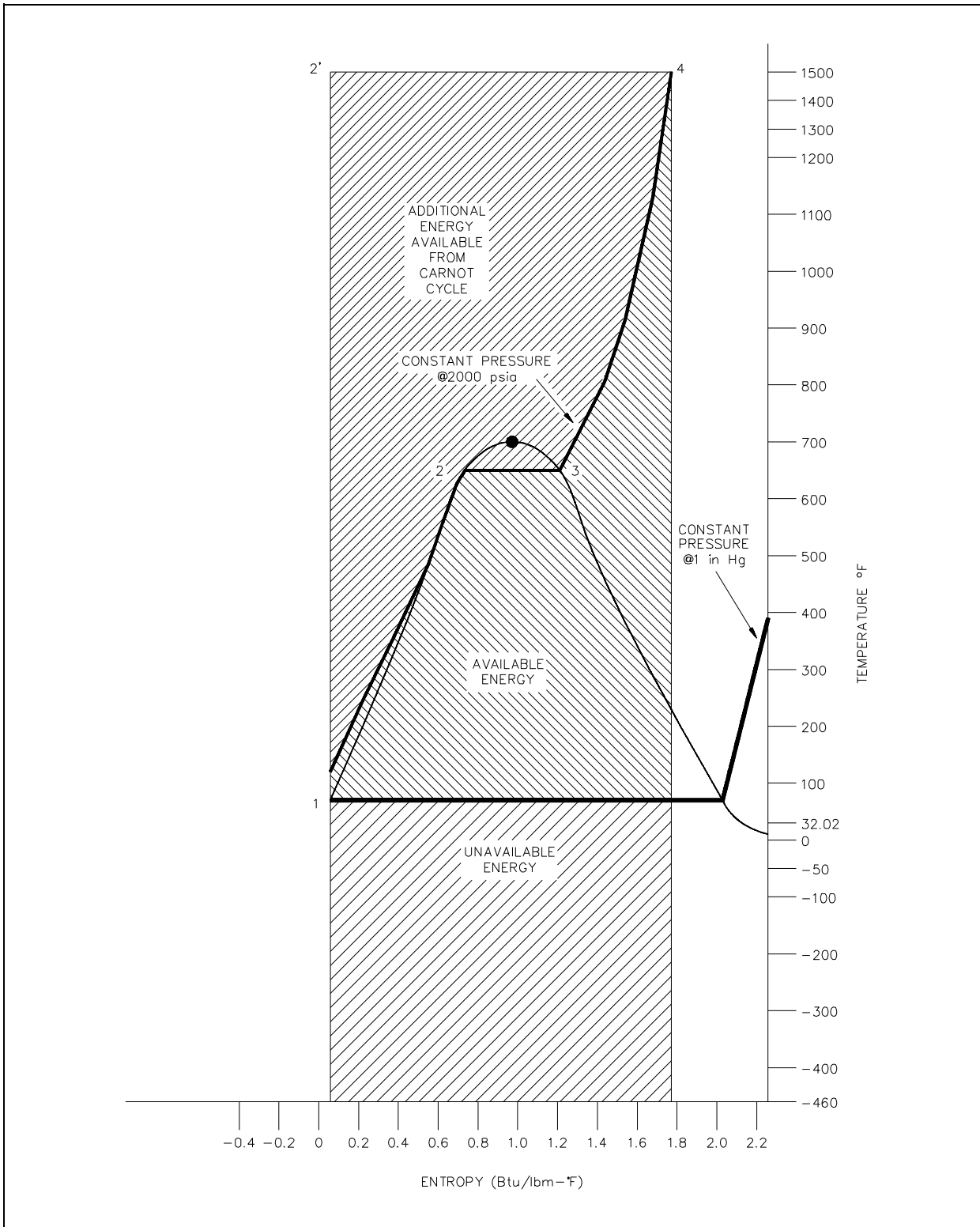


Figure 29 Carnot Cycle vs. Typical Power Cycle Available Energy

Figure 29 is a typical power cycle employed by a fossil fuel plant. The working fluid is water, which places certain restrictions on the cycle. If we wish to limit ourselves to operation at or below 2000 psia, it is readily apparent that constant heat addition at our maximum temperature of 1962°R is not possible (Figure 29, 2' to 4). In reality, the nature of water and certain elements of the process controls require us to add heat in a constant pressure process instead (Figure 29, 1-2-3-4). Because of this, the average temperature at which we are adding heat is far below the maximum allowable material temperature.

As can be seen, the actual available energy (area under the 1-2-3-4 curve, Figure 29) is less than half of what is available from the ideal Carnot cycle (area under 1-2'-4 curve, Figure 29) operating between the same two temperatures. Typical thermal efficiencies for fossil plants are on the order of 40% while nuclear plants have efficiencies of the order of 31%. Note that these numbers are less than 1/2 of the maximum thermal efficiency of the ideal Carnot cycle calculated earlier.

Figure 30 shows a proposed Carnot steam cycle superimposed on a T-s diagram. As shown, it has several problems which make it undesirable as a practical power cycle. First a great deal of pump work is required to compress a two phase mixture of water and steam from point 1 to the saturated liquid state at point 2. Second, this same isentropic compression will probably result in some pump cavitation in the feed system. Finally, a condenser designed to produce a two-phase mixture at the outlet (point 1) would pose technical problems.

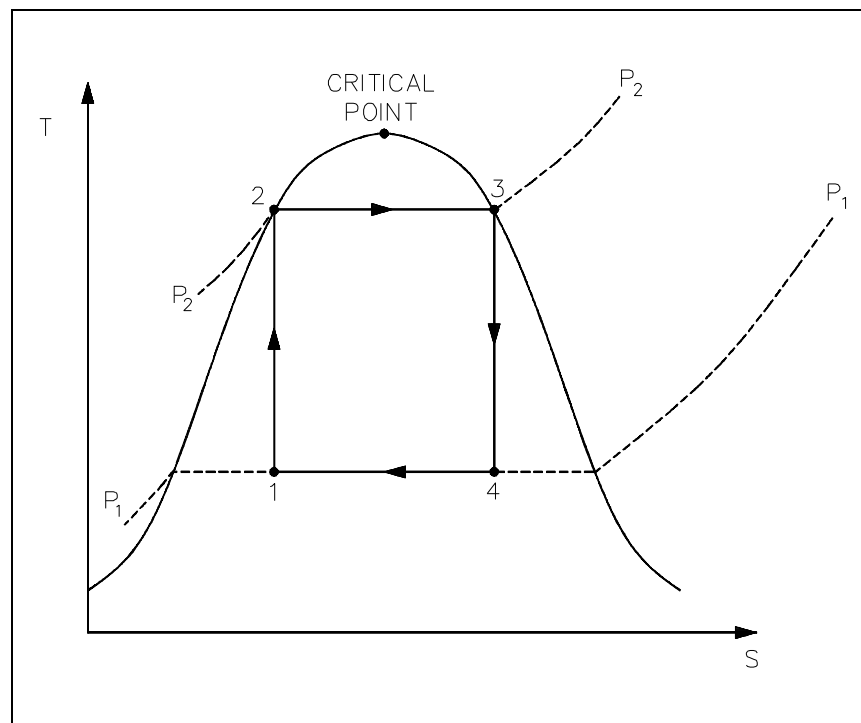


Figure 30 Ideal Carnot Cycle

Early thermodynamic developments were centered around improving the performance of contemporary steam engines. It was desirable to construct a cycle that was as close to being reversible as possible and would better lend itself to the characteristics of steam and process control than the Carnot cycle did. Towards this end, the Rankine cycle was developed.

The main feature of the Rankine cycle, shown in Figure 31, is that it confines the isentropic compression process to the liquid phase only (Figure 31 points 1 to 2). This minimizes the amount of work required to attain operating pressures and avoids the mechanical problems associated with pumping a two-phase mixture. The compression process shown in figure 31 between points 1 and 2 is greatly exaggerated*. In reality, a temperature rise of only 1°F occurs in compressing water from 14.7 psig at a saturation temperature of 212°F to 1000 psig.

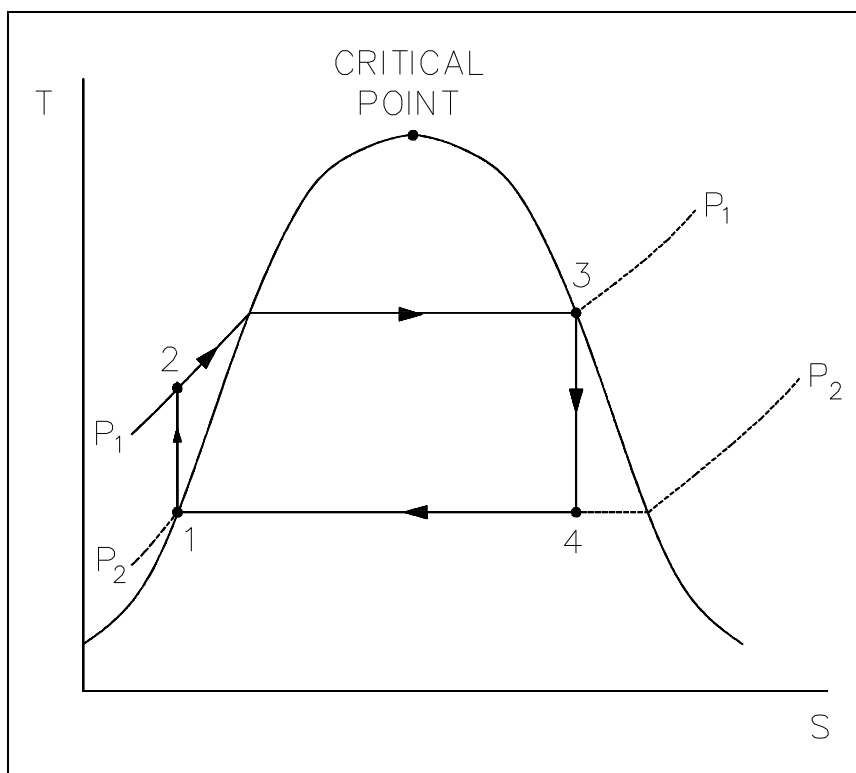


Figure 31 Rankine Cycle

** The constant pressure lines converge rapidly in the subcooled or compressed liquid region and it is difficult to distinguish them from the saturated liquid line without artificially expanding them away from it.*

In a Rankine cycle available and unavailable energy on a T-s diagram, like a T-s diagram of a Carnot cycle, is represented by the areas under the curves. The larger the unavailable energy, the less efficient the cycle.

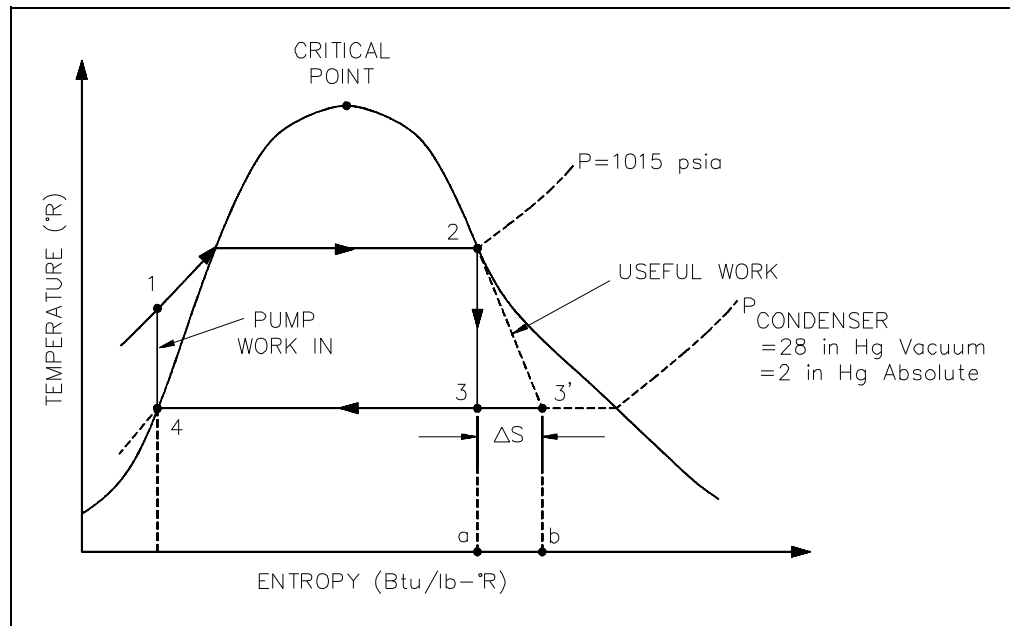


Figure 32 Rankine Cycle With Real v.s. Ideal

From the T-s diagram (Figure 32) it can also be seen that if an ideal component, in this case the turbine, is replaced with a non-ideal component, the efficiency of the cycle will be reduced. This is due to the fact that the non-ideal turbine incurs an increase in entropy which increases the area under the T-s curve for the cycle. But the increase in the area of available energy (3-2-3', Figure 32) is less than the increase in area for unavailable energy (a-3-3'-b, Figure 32).

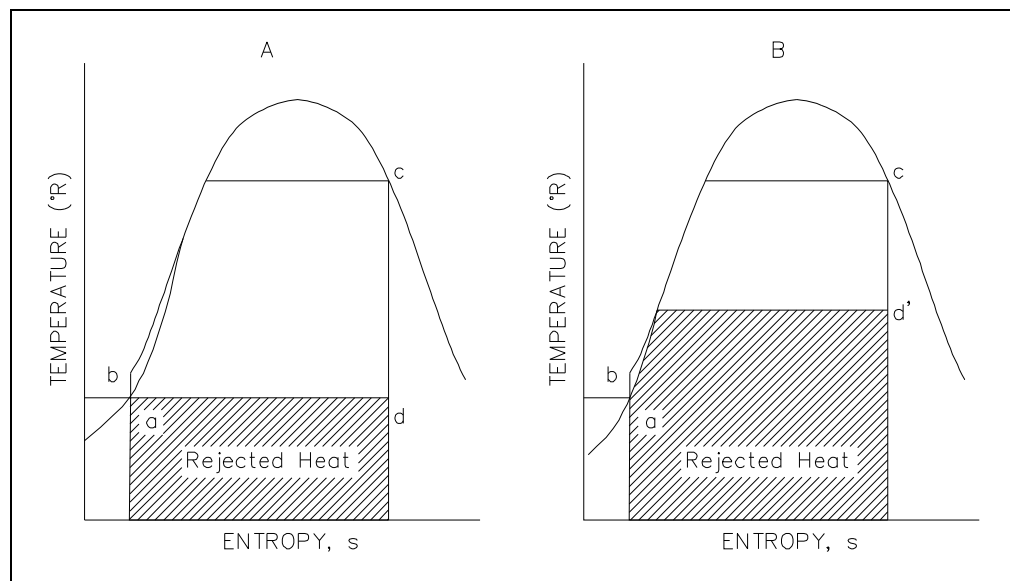


Figure 33 Rankine Cycle Efficiencies T-s

The same loss of cycle efficiency can be seen when two Rankine cycles are compared (see Figure 33). Using this type of comparison, the amount of rejected energy to available energy of one cycle can be compared to another cycle to determine which cycle is the most efficient, i.e. has the least amount of unavailable energy.

An h-s diagram can also be used to compare systems and help determine their efficiencies. Like the T-s diagram, the h-s diagram will show (Figure 34) that substituting non-ideal components in place of ideal components in a cycle, will result in the reduction in the cycles efficiency. This is because a change in enthalpy (h) always occurs when work is done or heat is added or removed in an actual cycle (non-ideal). This deviation from an ideal constant enthalpy (vertical line on the diagram) allows the inefficiencies of the cycle to be easily seen on a h-s diagram.

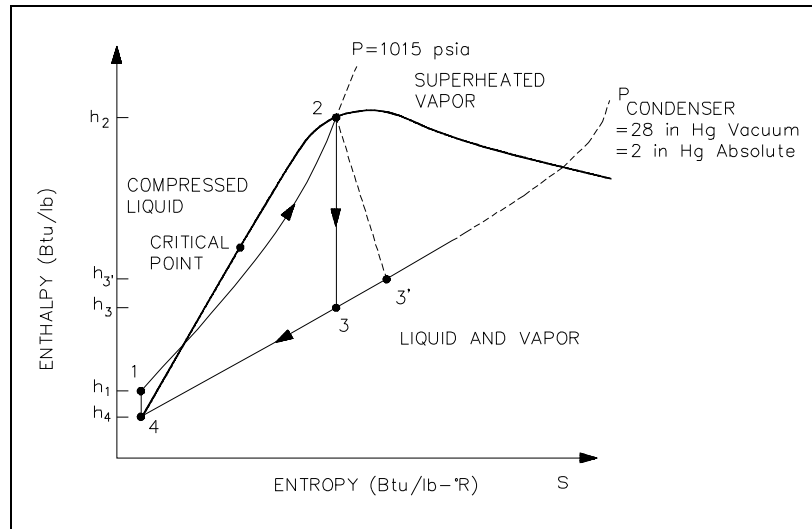


Figure 34 h-s Diagram

Typical Steam Cycle

Figure 35 shows a simplified version of the major components of a typical steam plant cycle. This is a simplified version and does not contain the exact detail that may be found at most power plants. However, for the purpose of understanding the basic operation of a power cycle, further detail is not necessary.

The following are the processes that comprise the cycle:

- 1-2: Saturated steam from the steam generator is expanded in the high pressure (HP) turbine to provide shaft work output at a constant entropy.
- 2-3: The moist steam from the exit of the HP turbine is dried and superheated in the moisture separator reheater (MSR).
- 3-4: Superheated steam from the MSR is expanded in the low pressure (LP) turbine to provide shaft work output at a constant entropy.

- 4-5: Steam exhaust from the turbine is condensed in the condenser in which heat is transferred to the cooling water under a constant vacuum condition.
- 5-6: The feedwater is compressed as a liquid by the condensate and feedwater pump and the feedwater is preheated by the feedwater heaters.
- 6-1: Heat is added to the working fluid in the steam generator under a constant pressure condition.

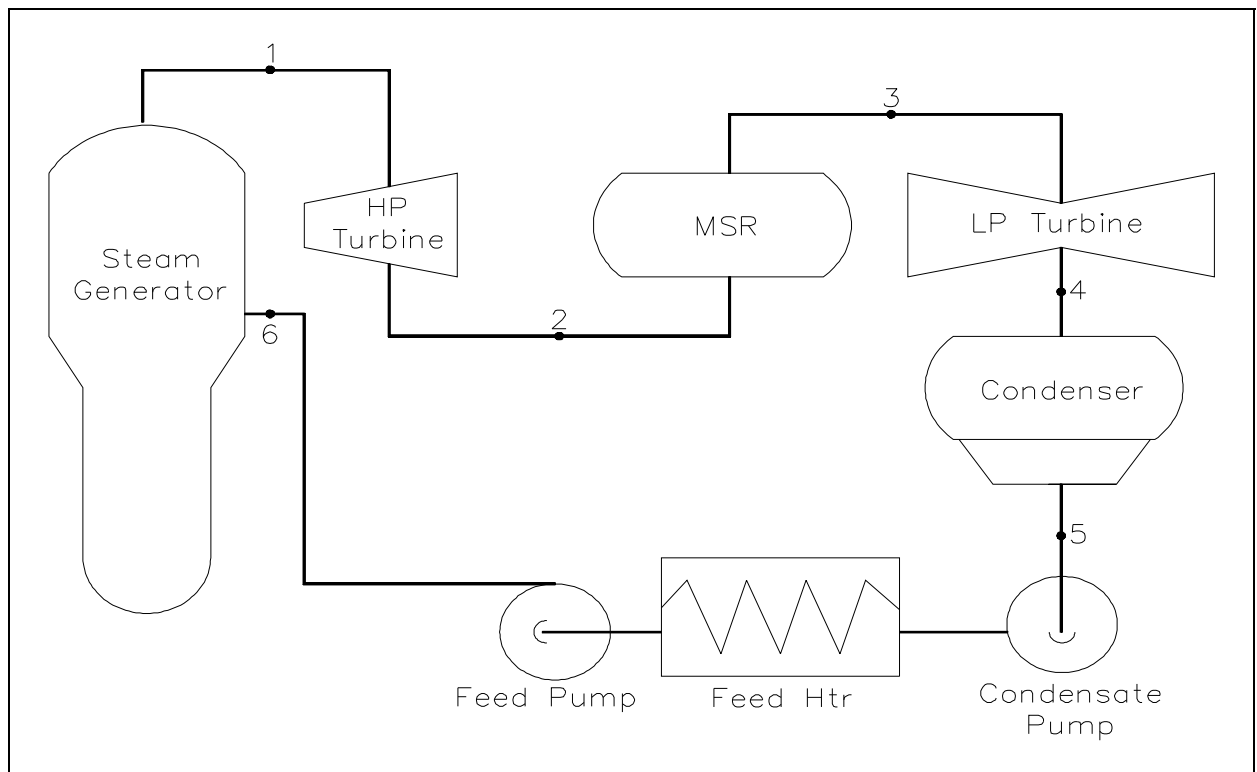


Figure 35 Typical Steam Cycle

The previous cycle can also be represented on a T-s diagram as was done with the ideal Carnot and Rankine cycles. This is shown in Figure 36. The numbered points on the cycle correspond to the numbered points on Figure 36.

It must be pointed out that the cycle we have just shown is an ideal cycle and does not exactly represent the actual processes in the plant. The turbine and pumps in an ideal cycle are ideal pumps and turbines and therefore do not exhibit an increase in entropy across them. Real pumps and turbines would exhibit an entropy increase across them.

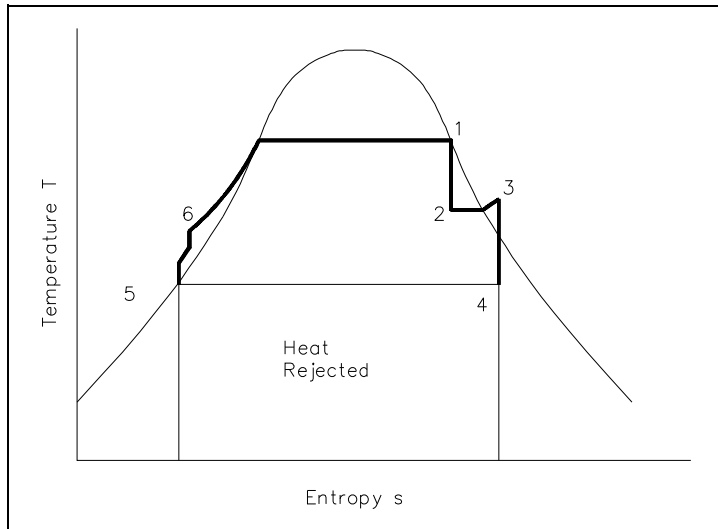


Figure 36 Steam Cycle (Ideal)

Figure 37 is a T-s diagram of a cycle which more closely approximates actual plant processes. The pumps and turbines in this cycle more closely approximate real pumps and turbines and thus exhibit an entropy increase across them. Additionally, in this cycle, a small degree of subcooling is evident in the condenser as shown by the small dip down to point 5. This small amount of subcooling will decrease cycle efficiency since additional heat has been removed from the cycle to the cooling water as heat rejected. This additional heat rejected must then be made up for in the steam generator. Therefore, it can be seen that excessive condenser subcooling will decrease cycle efficiency. By controlling the temperature or flow rate of the cooling water to the condenser, the operator can directly effect the overall cycle efficiency.

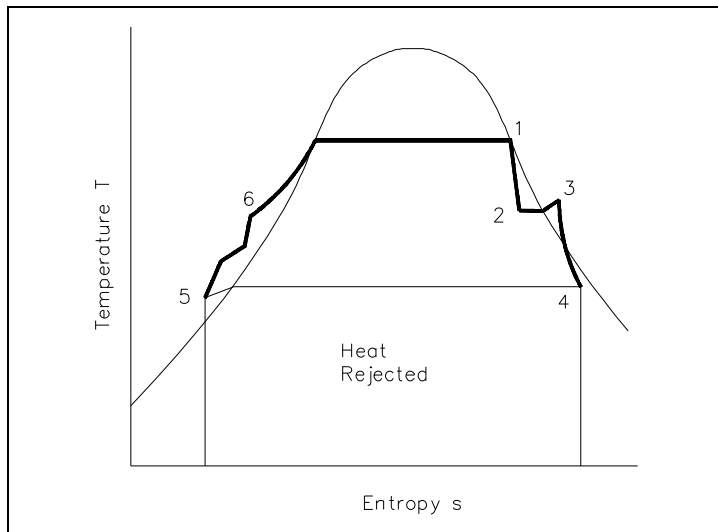


Figure 37 Steam Cycle (Real)

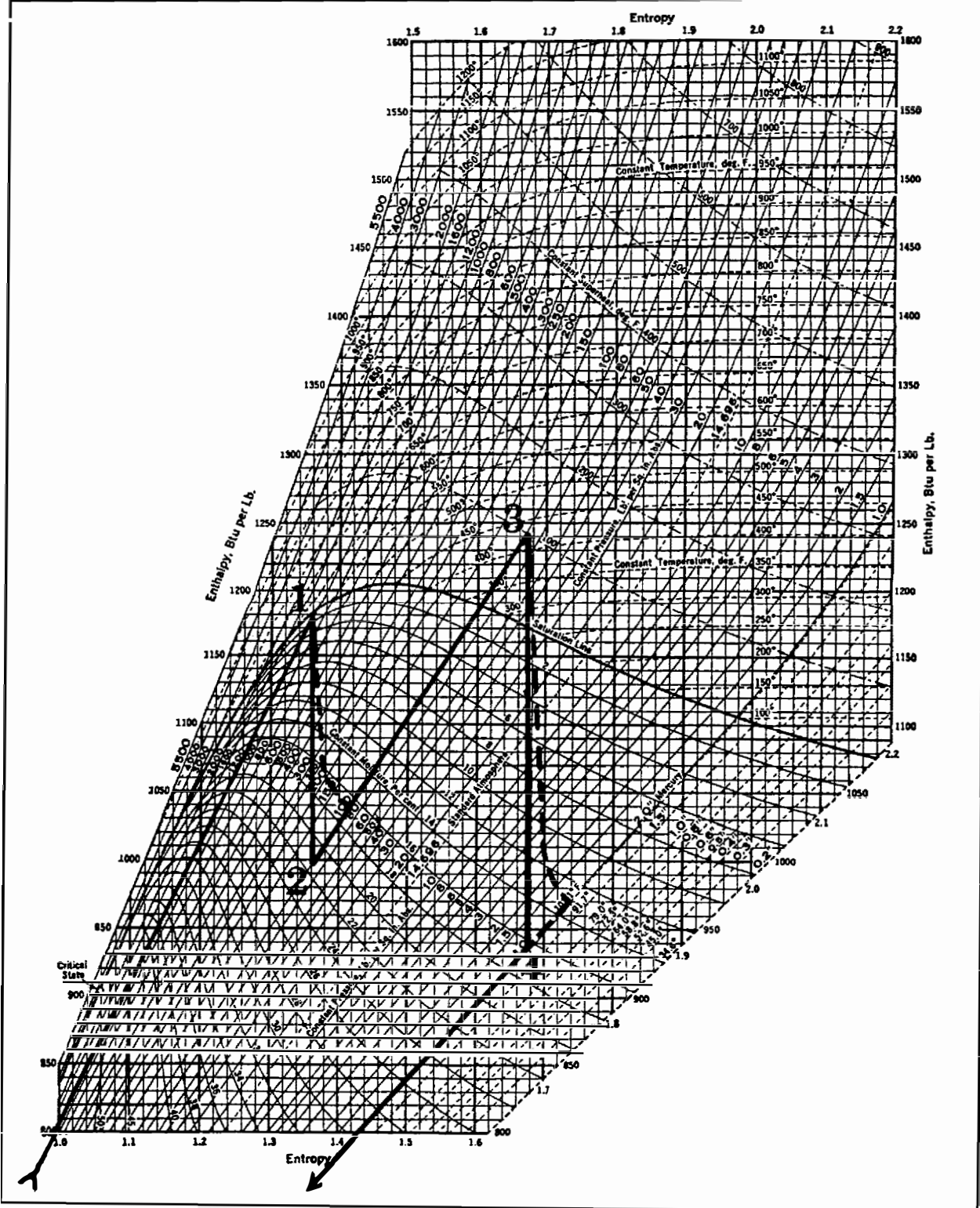


Figure 38 Mollier Diagram

It is sometimes useful to plot on the Mollier diagram the processes that occur during the cycle. This is done on Figure 38. The numbered points on Figure 38 correspond to the numbered points on Figures 35 and 36. Because the Mollier diagram is a plot of the conditions existing for water in vapor form, the portions of the plot which fall into the region of liquid water do not show up on the Mollier diagram. The following conditions were used in plotting the curves on Figure 38.

- Point 1: Saturated steam at 540°F
- Point 2: 82.5% quality at exit of HP turbine
- Point 3: Temperature of superheated steam is 440°F
- Point 4: Condenser vacuum is 1 psia

The solid lines on Figure 38 represent the conditions for a cycle which uses ideal turbines as verified by the fact that no entropy change is shown across the turbines. The dotted lines on Figure 38 represent the path taken if real turbines were considered, in which case an increase in entropy is evident.

Causes of Inefficiency

In the preceding sections, cycle and component efficiencies have been discussed, but the actual causes or reasons for the inefficiencies have not been explained. In this section we will compare some of the types and causes for the inefficiencies of real components and cycles to that of their "ideal" counterparts.

Components

In real systems, a percentage of the overall cycle inefficiency is due to the losses by the individual components. Turbines, pumps, and compressors all behave non-ideally due to heat losses, friction and windage losses. All of these losses contribute to the non-isentropic behavior of real equipment. As explained previously (Figures 24, 25) these losses can be seen as an increase in the system's entropy or amount of energy that is unavailable for use by the cycle.

Cycles

In real systems, a second source of inefficiencies is from the compromises made due to cost and other factors in the design and operation of the cycle. Examples of these types of losses are: In a large power generating station the condensers are designed to subcool the liquid by 8-10°F. This subcooling allows the condensate pumps to pump the water forward without cavitation. But, each degree of subcooling is energy that must be put back by reheating the water, and this heat (energy) does no useful work and therefore increases the inefficiency of the cycle. Another example of a loss due to a system's design is heat loss to the environment, i.e. thin or poor insulation. Again this is energy lost to the system and therefore unavailable to do work. Friction is another real world loss, both resistance to fluid flow and mechanical friction in machines. All of these contribute to the system's inefficiency.

Summary

The important information from this chapter is summarized below.

Second Law of Thermodynamics Summary

- Planck's statement of the Second Law of Thermodynamics is:

It is impossible to construct an engine that will work in a complete cycle and produce no other effect except the raising of a weight and the cooling of a heat reservoir.

- The Second Law of Thermodynamics demonstrates that the maximum possible efficiency of a system is the Carnot efficiency written as:

$$\eta = (T_H - T_C)/T_H$$

- The maximum efficiency of a closed cycle can be determined by calculating the efficiency of a Carnot cycle operating between the same value of high and low temperatures.
- The efficiency of a component can be calculated by comparing the work produced by the component to the work that would have been produced by an ideal component operating isentropically between the same inlet and outlet conditions.
- An isentropic expansion or compression process will be represented as a vertical line on a T-s or h-s diagram. A real expansion or compression process will look similar, but will be slanted slightly to the right.
- Efficiency will be decreased by:

Presence of friction
Heat losses
Cycle inefficiencies

COMPRESSION PROCESSES

Compression and pressurization processes are very common in many types of industrial plants. These processes vary from being the primary function of a piece of equipment, such as an air compressor, to an incidental result of another process, such as filling a tank with water without first opening the valve.

- EO 1.32** **Apply the ideal gas laws to SOLVE for the unknown pressure, temperature, or volume.**
- EO 1.33** **DESCRIBE when a fluid may be considered to be incompressible.**
- EO 1.34** **CALCULATE the work done in constant pressure and constant volume processes.**
- EO 1.35** **DESCRIBE the effects of pressure changes on confined fluids.**
- EO 1.36** **DESCRIBE the effects of temperature changes on confined fluids.**
-

Boyle's and Charles' Laws

The results of certain experiments with gases at relatively low pressure led Robert Boyle to formulate a well-known law. It states that:

the pressure of a gas expanding at constant temperature varies inversely to the volume, or

$$(P_1)(V_1) = (P_2)(V_2) = (P_3)(V_3) = \text{constant.} \quad (1-40)$$

Charles, also as the result of experimentation, concluded that:

the pressure of a gas varies directly with temperature when the volume is held constant, and the volume varies directly with temperature when the pressure is held constant, or

$$\frac{V_1}{V_2} = \frac{T_1}{T_2} \quad \text{or} \quad \frac{P_1}{P_2} = \frac{T_1}{T_2}. \quad (1-41)$$

Ideal Gas Law

By combining the results of Charles' and Boyle's experiments, the relationship

$$\frac{Pv}{T} = \text{constant} \quad (1-42)$$

may be obtained. The constant in the above equation is called the ideal gas constant and is designated by R ; thus the ideal gas equation becomes

$$Pv = RT \quad (1-43)$$

where the pressure and temperature are absolute values. The values of the ideal gas constant (R) for several of the more common gases are given in Figure 39.

Gas	Chemical Symbol	Molecular Weight	Gas Constant ft-lbf/lbm ^o R	Specific Heat Btu/lbm		Specific Heat Ratio
				c_p	c_v	
Air		M 28.95	R 53.35	0.172	0.240	1.40
Carbon dioxide	CO ₂	44.00	35.13	0.160	0.205	1.28
Hydrogen	H ₂	2.016	766.80	2.44	3.42	1.40
Nitrogen	N ₂	28.02	55.16	0.176	0.247	1.40
Oxygen	O ₂	32.0	48.31	0.155	0.217	1.40
Steam	H ₂ O	18.016	85.81	0.36	0.46	1.28

Steam at pressures less than 1 psia behaves very nearly as a perfect gas.

Figure 39 Ideal Gas Constant Values

The individual gas constant (R) may be obtained by dividing the universal gas constant (R_o) by the molecular weight (MW) of the gas, $R = \frac{R_o}{MW}$. The units of R must always be consistent with the units of pressure, temperature, and volume used in the gas equation. No real gases follow the ideal gas law or equation completely. At temperatures near a gases boiling point, increases in pressure will cause condensation to take place and drastic decreases in volume. At very high pressures, the intermolecular forces of a gas are significant. However, most gases are in approximate agreement at pressures and temperatures above their boiling point.

The ideal gas law is utilized by engineers working with gases because it is simple to use and approximates real gas behavior. Most physical conditions of gases used by man fit the above description. Perhaps the most common use of gas behavior studied by engineers is that of the compression process using ideal gas approximations. Such a compression process may occur at constant temperature ($pV = \text{constant}$), constant volume, or adiabatic (no heat transfer). Whatever the process, the amount of work that results from it depends upon the process, as brought out in the discussion on the First Law of Thermodynamics. The compression process using ideal gas considerations results in work performed on the system and is essentially the area under a P-V curve. As can be seen in Figure 40, different amounts of work result from different ideal gas processes such as constant temperature and constant pressure.

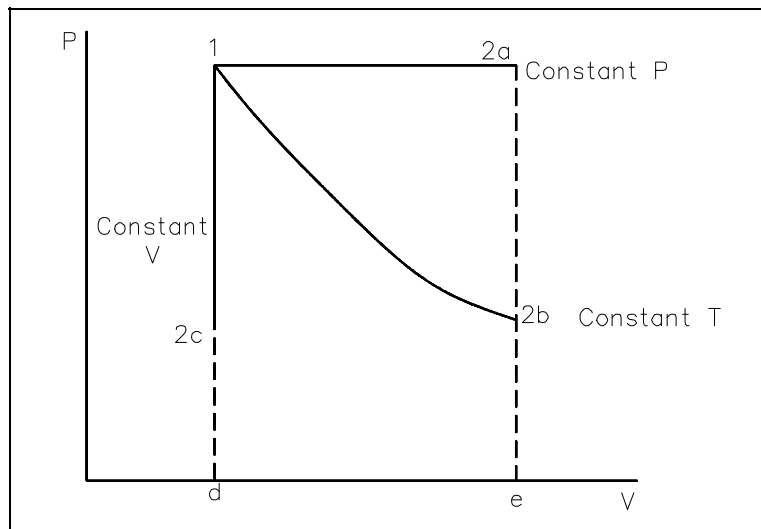


Figure 40 Pressure-Volume Diagram

Fluid

A *fluid* is any substance that conforms to the shape of its container. It may be either a liquid or a gas.

Compressibility of Fluids

Usually a fluid may be considered incompressible when the velocity of the fluid is greater than one-third of the speed of sound for the fluid, or if the fluid is a liquid. The treatment of a fluid that is considered incompressible is easy because the density is assumed to be constant, giving a simple relationship for the state of the substance. The variation of density of the fluid with changes in pressure is the primary factor considered in deciding whether a fluid is incompressible.

Fluids that are compressible have much more complex equations to deal with, due to density changes, and have property relationships that vary more rapidly than incompressible fluids. In addition, fixing the state of a liquid can be done easily by knowing its temperature and pressure. Once the substance becomes a gas, the process becomes more difficult.

Constant Pressure Process

To determine the work done in a constant pressure process, the following equation is used:

$$W_{1-2} = P(\Delta V) \quad (1-44)$$

Constant Volume Process

The solution of Equation 1-45 for a constant volume process is also not difficult. The work done in a constant volume process is the product of the volume and the change in pressure.

$$W_{1-2} = V(\Delta P) \quad (1-45)$$

In addition to gases, Equation 1-45 also applies to liquids. The power requirement for pumps that move incompressible liquids (such as water) can be determined from Equation 1-44. Replacing the volume (V) with the product of the specific volume and the mass yields Equation 1-45.

$$W_{1-2} = m\nu(\Delta P) \quad (1-46)$$

Taking the time rate of change of both sides of Equation 1-46 determines the power requirements of the pump.

$$\dot{W}_{1-2} = \dot{m}\nu(\Delta P) \quad (1-47)$$

Effects of Pressure Changes on Fluid Properties

The predominant effect of an increase in pressure in a compressible fluid, such as a gas, is an increase in the density of the fluid. An increase in the pressure of an incompressible fluid will not have a significant effect on the density. For example, increasing the pressure of 100 °F water from 15 psia to 15,000 psia will only increase the density by approximately 6%. Therefore, in engineering calculations, it is assumed that incompressible fluids' density remain constant.

Effects of Temperature Changes on Fluid Properties

An increase in temperature will tend to decrease the density of any fluid. If the fluid is confined in a container of fixed volume, the effect of a temperature change will depend on whether the fluid is compressible.

If the fluid is a gas, it will respond to a temperature change in a manner predicted by the ideal gas laws. A 5% increase in absolute temperature will result in a 5% increase in the absolute pressure.

If the fluid is an incompressible liquid in a closed container, an increase in the temperature will have a tremendously greater and potentially catastrophic effect. As the fluid temperature increases, it tries to expand, but expansion is prevented by the walls of the container. Because the fluid is incompressible, this results in a tremendous increase in pressure for a relatively minor temperature change. The change in specific volume for a given change in temperature is not the same at various beginning temperatures. Resultant pressure changes will vary. A useful thumb rule for water is that pressure in a water-solid system will increase about 100 psi for every 1 °F increase in temperature.

Summary

The important information from this chapter is summarized below.

Compression Processes Summary

- The ideal gas law can be used to determine how the properties of pressure, temperature, and volume will be related during compression processes.

$$Pv = R T$$

- A fluid may be considered incompressible if one of two conditions is true:

The fluid is a liquid.

The fluid is a gas with a velocity greater than one-third of the speed of sound in the gas.

- The work for certain types of processes can be determined as follows:

Constant pressure process $W_{1-2} = P(\Delta V)$

Constant volume process $W_{1-2} = V(\Delta P)$

Appendix A

Thermodynamics

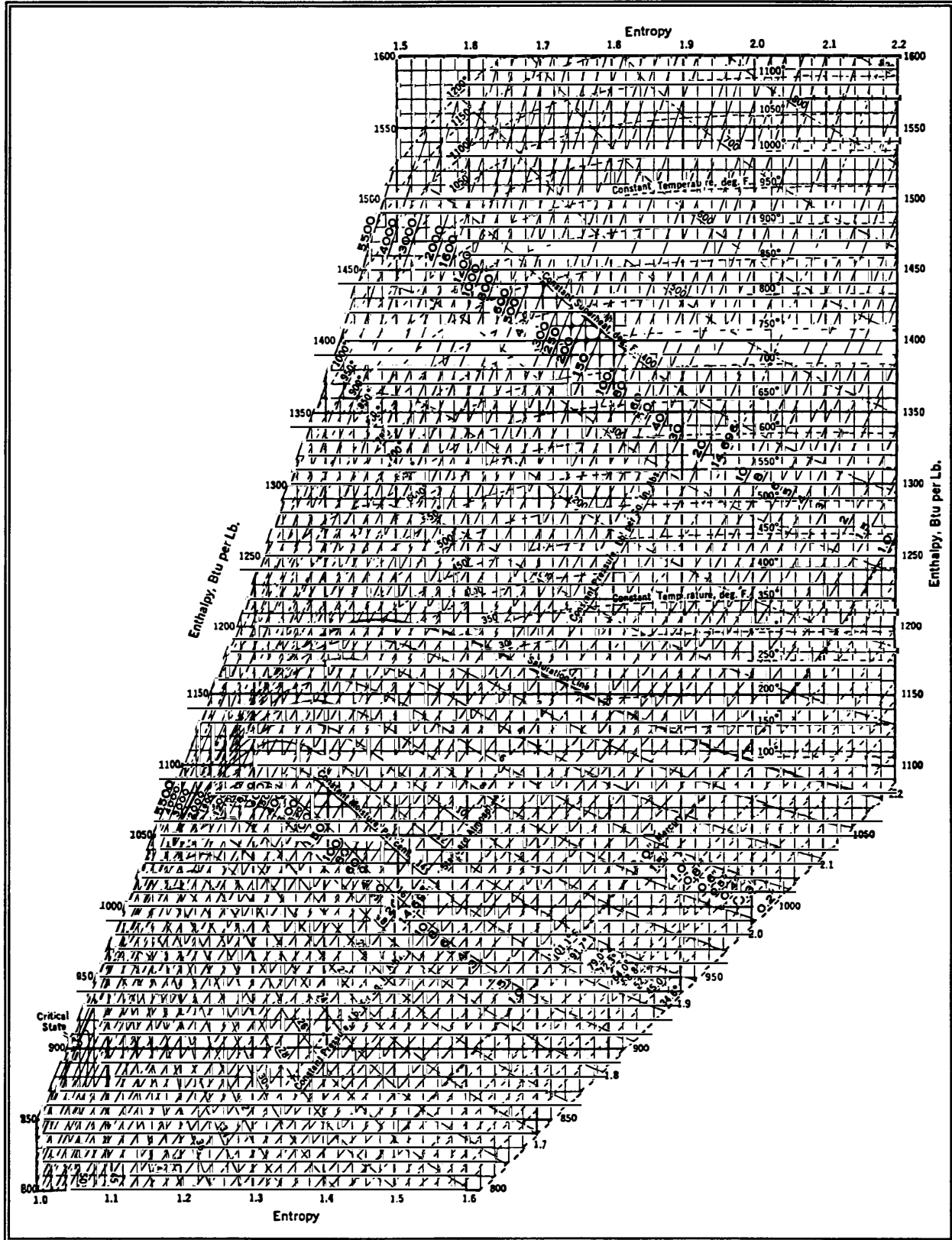


Figure A-1

Saturated Steam: Pressure Table

Abs Press. Lb/Sq In. p	Temp Fahr t	Specific Volume			Enthalpy			Entropy			Abs Press. Lb/Sq In. p
		Sat. Liquid v _f	Evap v _{fg}	Sat. Vapor v _g	Sat. Liquid h _f	Evap h _{fg}	Sat. Vapor h _g	Sat. Liquid s _f	Evap s _{fg}	Sat. Vapor s _g	
200.0	381.80	0.01839	2.2689	2.2873	355.5	842.8	1198.3	0.5438	1.0016	1.5454	200.0
210.0	385.91	0.01844	2.16373	2.18217	359.9	839.1	1199.0	0.5490	0.9923	1.5413	210.0
220.0	389.88	0.01850	2.06779	2.08629	364.2	835.4	1199.6	0.5540	0.9834	1.5374	220.0
230.0	393.70	0.01855	1.97991	1.99846	368.3	831.8	1200.1	0.5588	0.9748	1.5336	230.0
240.0	397.39	0.01860	1.89909	1.91769	372.3	828.4	1200.6	0.5634	0.9665	1.5299	240.0
250.0	400.97	0.01865	1.82452	1.84317	376.1	825.0	1201.1	0.5679	0.9585	1.5264	250.0
260.0	404.44	0.01870	1.75548	1.77418	379.9	821.6	1201.5	0.5722	0.9508	1.5230	260.0
270.0	407.80	0.01875	1.69137	1.71013	383.6	818.3	1201.9	0.5764	0.9433	1.5197	270.0
280.0	411.07	0.01880	1.63169	1.65049	387.1	815.1	1202.3	0.5805	0.9361	1.5166	280.0
290.0	414.25	0.01885	1.57597	1.59482	390.6	812.0	1202.6	0.5844	0.9291	1.5135	290.0
300.0	417.35	0.01889	1.52384	1.54274	394.0	808.9	1202.9	0.5882	0.9223	1.5105	300.0
350.0	431.73	0.01912	1.30642	1.32554	409.8	794.2	1204.0	0.6059	0.8909	1.4968	350.0
400.0	444.60	0.01934	1.14162	1.16095	424.2	780.4	1204.6	0.6217	0.8630	1.4847	400.0

Saturated Steam: Temperature Table

Temp Fahr t	Abs Press Lb per Sq In. p	Specific Volume			Enthalpy			Entropy			Temp Fahr t
		Sat. Liquid v _f	Evap v _{fg}	Sat. Vapor v _g	Sat. Liquid h _f	Evap h _{fg}	Sat. Vapor h _g	Sat. Liquid s _f	Evap s _{fg}	Sat. Vapor s _g	
460.0	466.87	0.01961	0.97463	0.99424	441.5	763.2	1204.8	0.6405	0.8299	1.4704	460.0
464.0	485.56	0.01969	0.93588	0.95557	446.1	758.6	1204.7	0.6454	0.8213	1.4667	464.0
468.0	504.83	0.01976	0.89885	0.91862	450.7	754.0	1204.6	0.6502	0.8127	1.4629	468.0
472.0	524.67	0.01984	0.86345	0.88329	455.2	749.3	1204.5	0.6551	0.8042	1.4592	472.0
476.0	545.11	0.01992	0.82958	0.84950	459.9	744.5	1204.3	0.6599	0.7956	1.4555	476.0
480.0	566.15	0.02000	0.79716	0.81717	464.5	739.6	1204.1	0.6648	0.7871	1.4518	480.0
484.0	587.81	0.02009	0.76613	0.78622	469.1	734.7	1203.8	0.6696	0.7785	1.4481	484.0
488.0	610.10	0.02017	0.73641	0.75658	473.8	729.7	1203.5	0.6745	0.7700	1.4444	488.0
492.0	633.03	0.02026	0.70794	0.72820	478.5	724.6	1203.1	0.6793	0.7614	1.4407	492.0
496.0	656.61	0.02034	0.68065	0.70100	483.2	719.5	1202.7	0.6842	0.7528	1.4370	496.0

Superheated Steam

Abs Press. Lb/Sq In. (Sat. Temp)	Sat. Water	Sat. Steam	Temperature – Degrees Fahrenheit														
			450	500	550	600	650	700	800	900	1000	1100	1200	1300	1400	1500	
400 (444.60)	Sh		5.40	55.40	105.40	155.40	205.40	255.40	355.40	455.40	555.40	655.40	755.40	855.40	955.40	1055.40	
	v	0.01934	1.1610	1.1738	1.2841	1.3836	1.4763	1.5646	1.6499	1.8151	1.9759	2.1339	2.2901	2.4450	2.5987	2.7515	2.9037
	h	424.17	1204.6	1208.8	1245.1	1277.5	1307.4	1335.9	1363.4	1417.0	1470.1	1523.3	1576.9	1631.2	1686.2	1741.9	1798.2
420 (449.40)	s	0.6217	1.4847	1.4894	1.5282	1.5611	1.5901	1.6163	1.6406	1.6850	1.7255	1.7632	1.7988	1.8325	1.8647	1.8955	1.9250
	Sh		60	50.60	100.60	150.60	200.60	250.60	350.60	450.60	550.60	650.60	750.60	850.60	950.60	1050.60	
	v	0.01942	1.1057	1.1071	1.2148	1.3113	1.4007	1.4856	1.5676	1.7258	1.8795	2.0304	2.1795	2.3273	2.4739	2.6196	2.7647
440 (454.03)	h	429.56	1204.7	1205.2	1242.4	1275.4	1305.8	1334.5	1362.3	1416.2	1469.4	1522.7	1576.4	1630.8	1685.8	1741.6	1798.0
	s	0.6276	1.4802	1.4808	1.5206	1.5542	1.5835	1.6100	1.6345	1.6791	1.7197	1.7575	1.7932	1.8269	1.8591	1.8899	1.9195
	Sh		45.97	95.97	145.97	195.97	245.97	345.97	445.97	545.97	645.97	745.97	845.97	945.97	1045.97		
440 (454.03)	v	0.01950	1.0554	1.1517	1.2454	1.3319	1.4138	1.4926	1.6445	1.7918	1.9363	2.0790	2.2203	2.3605	2.4998	2.6384	
	h	434.77	1204.8	1239.7	1273.4	1304.2	1333.2	1361.1	1415.3	1468.7	1522.1	1575.9	1630.4	1685.5	1741.2	1797.7	
	s	0.6332	1.4759	1.5132	1.5474	1.5772	1.6040	1.6286	1.6734	1.7142	1.7521	1.7878	1.8216	1.8538	1.8847	1.9143	

Figure A-2

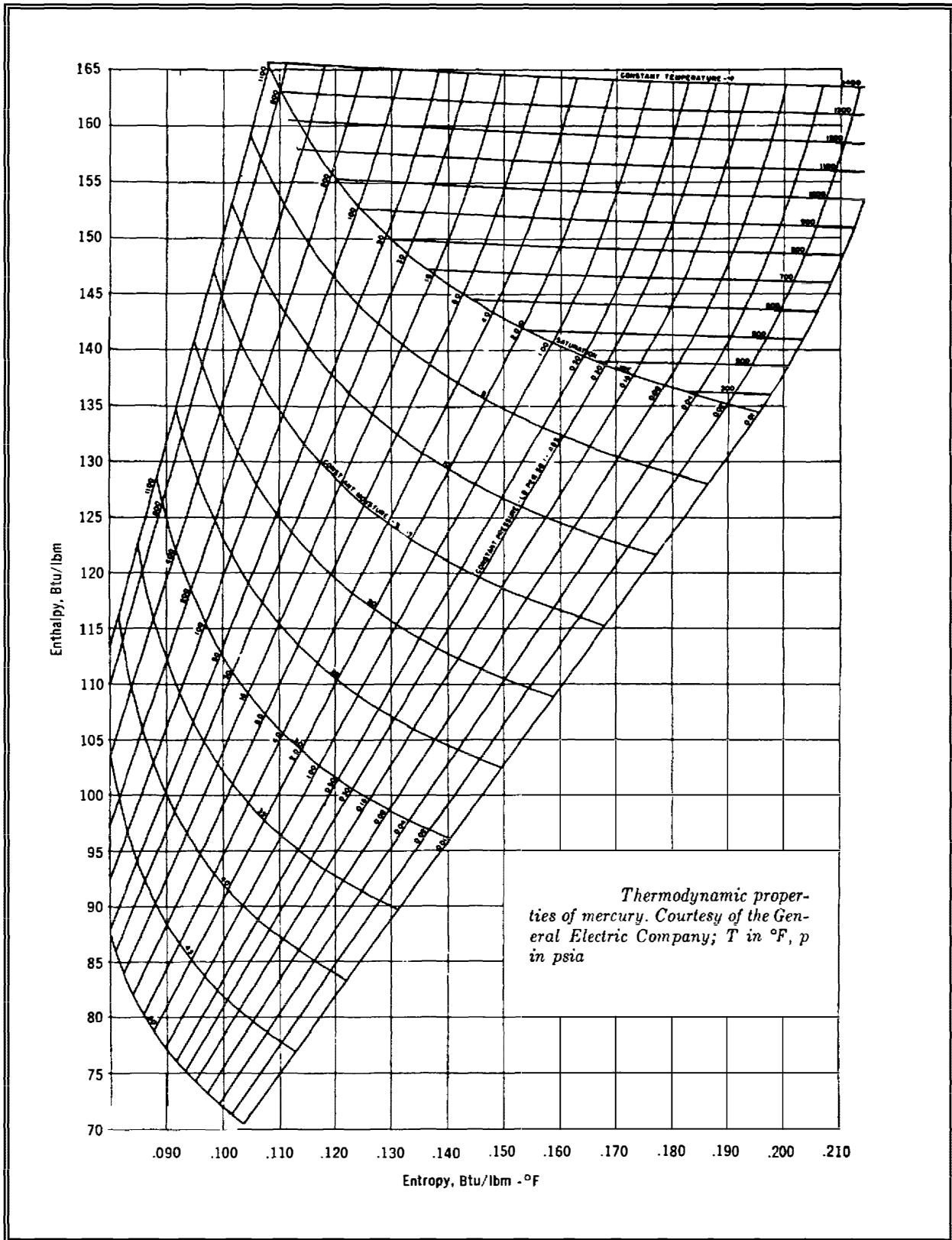
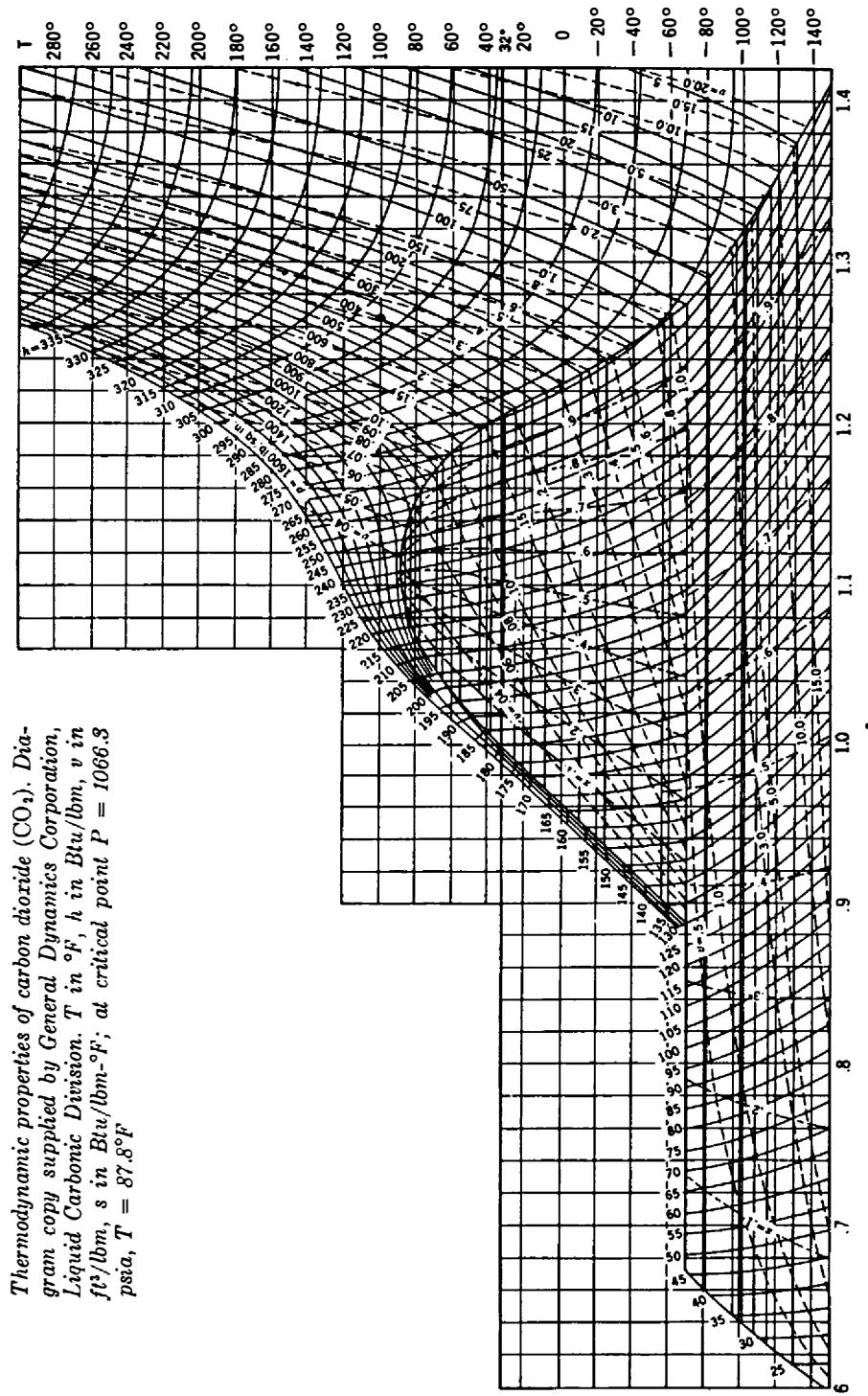


Figure A-3



Thermodynamic properties of carbon dioxide (CO₂). Diagram copy supplied by General Dynamics Corporation, Liquid Carbonic Division. T in °F, h in Btu/lbm, v in ft³/lbm, s in Btu/lbm-°F; at critical point P = 1066.8 psia, T = 87.8°F

Figure A-4